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Performance Analysis of STAR-RIS-CR-NOMA Based Consumer IoT Networks for Resilient Industry 5.0

Xingwang Li, *Senior Member, IEEE*, Xuesong Gao, Liang Yang, Hongwu Liu, *Senior Member, IEEE*, Ji Wang, *Member, IEEE*, Khaled M. Rabie, *Senior Member, IEEE*, Dawei Qiao

Abstract—The arrival of the sixth generation (6G) wireless communication will intensify the developments of the Internet of Things (IoT) for widely applications in resilient industry 5.0. Driving the development of the intelligent consumer industry, consumer electronic devices have progressively become indispensable components of the constantly rising IoT. However, the steady rise of consumer IoT intelligent terminals has led to large-scale connections, spectrum scarcity, and energy consumption emerging as crucial challenges for the future wireless communication in resilient industry 5.0. To mitigate the aforementioned issues, a novel simultaneously transmitting and reflecting reconfigurable intelligent surface (STAR-RIS) assisted cognitive radio (CR)-non-orthogonal multiple access (NOMA) network are proposed. Specifically, we comprehensively elaborate on systems performance in terms of outage probability (OP), ergodic rate (ER) and energy efficiency (EE). Furthermore, the asymptotic OP and ER of the primary and secondary consumer electronic devices under the high signal-to-noise ratio (SNR) regions are investigated to undertake a thorough analysis. We find that the outage and ER performance gradually increase with the transmit SNR, and tend to a fixed value at high SNR regions. In addition, increasing the number of STAR-RIS components will enhance the reliable, ER and EE performance of the considered systems. Finally, the accuracy of analysis and the superiority of the proposed scheme are verified through Monte Carlo simulations.

Index Terms—Cognitive radio (CR), non-orthogonal multiple access (NOMA), resilient industry 5.0, simultaneously transmitting and reflecting reconfigurable intelligent surface (STAR-RIS).

I. INTRODUCTION

The persistent prosperity of the Internet of Things (IoT) in resilient industry 5.0 is being driven by the development of the upcoming sixth generation (6G) wireless communication. As

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an emerging industry of the IoT, consumer electronic devices have played a pivotal role in advancing and popularizing intelligent terminals for consumers. The applications have expanded to various fields such as smart home, smart wearables, smart education, smart factory [1, 2]. In resilient industry 5.0, the pervasive utilization of consumer IoT intelligent terminals has resulted in large scale connectivity, high cost hardware, and energy consumption issues. To this end, several promising techniques are proposed, such as simultaneously transmitting and reflecting reconfigurable intelligent surface (STAR-RIS) [3], non-orthogonal multiple access (NOMA) [4] and cognitive radio (CR) [5].

Reconfigurable intelligent surface (RIS) has triggered an upsurge in research because of the ability to configure smart radio environments. RIS is a metasurface comprising plenty of inexpensive reflective elements that dynamically adjust the amplitude and phase of the reflective elements to achieve the desired path effect [6, 7]. However, the conventional RIS requires the transmitter and receiver being located on the same side, which inevitably creates blind spots behind the RIS, severely restricting its deployment flexibility and coverage range. In order to surmount this drawback, STAR-RIS was proposed in [8]. Unlike RIS, STAR-RIS has the capable to cover the entire space, achieving 360° full coverage [9]. Time switching, energy splitting and mode switching are the three representative protocols for STAR-RIS [10]. In [11], the authors modeled a STAR-RIS-NOMA network and explored its bit error performance under the imperfect successive interference cancellation (SIC) condition. To achieve maximum energy efficiency, Wang *et al.* in [12] alternately optimized the phase shift and beamforming vectors of the multi-user STAR-RIS-NOMA networks. In [13], the authors integrated cooperative dual RIS with STAR-RIS for the sake of communication in massive multiple input multiple output (MIMO) configurations.

The unprecedented prosperity of the consumer IoT within resilient industry 5.0 has resulted in a persistent escalation in the quantity of terminal connections. Fortunately, NOMA is propositioned as a potential candidate scheme for 6G due to the ability to achieve large scale connections [14]. NOMA, unlike traditional orthogonal multiple access (OMA), permits numerous users to access the same resource block at once, such as time/frequency/code domain resources [15]. It can significantly improve the resource utilization of communica-

tion systems. At the transmitter, different transmit power is allocated according to the channel strength to achieve fairness among users, and signal separation is achieved at the receiver by means of the SIC technique [16]. To assess the performance of the system under consideration, Xu *et al.* in [17] provided a full-duplex network-coded cooperative NOMA model and derived the outage probability (OP) expressions. Zhang *et al.* in [18] introduced a novel low complexity scheme for the NOMA-unmanned aerial vehicle (UAV) networks in order to maximize the sum rate. Ding *et al.* in [19] offered a universal hybrid NOMA assisted mobile edge computing offloading scheme and established a multi-objective optimization issue with the objective of reducing energy consumption. To improve energy efficiency (EE), the authors in [20] combined incremental relaying with near user in the considered NOMA network, achieving an increase in throughput for far user.

In parallel, CR has been extensively investigated as a favorable technique to address the problem of spectrum resource scarcity [21]. The three typical modes of spectrum sharing in CR are interweave, overlay and underlay [22]. The CR network is split into the primary network (PN) with authorized primary users (PU) and the secondary network (SN) with unauthorized secondary users (SU). In CR network, SU can utilize the authorized frequency band of the PU and share spectrum resources with PU without affecting the quality of service (QoS) of the PU [23]. In overlay CR, the SN uses part of energy to transmit its own signals, while the remainder is used to help the PN transmit signals in exchange for the utilization of authorized frequency bands [24]. This mode enables synchronous transmission between the primary and secondary networks, while concurrently enhancing the performance of the PN. In [25], the authors presented an overlay CR-NOMA system and comprehensively assessed the reliability by calculating the expression of OP for primary and secondary users. To maximize average effective spectrum efficiency, Lu *et al.* in [26] proposed an optimization for a short packet covert communication in interweave CR. Further, the authors in [27] suggested a distributed transmit power control scheme for an underlay CR system to maximize spectrum efficiency.

In consideration of the aforementioned analysis, the combination of STAR-RIS, NOMA, and CR can achieve 360° full space coverage, which effectively improves spectrum utilization and communication QoS while achieving low power consumption. In [28], the authors proposed a coordinated direct and relay transmission based underlay CR-NOMA network, and the OP and throughput of users under imperfect SIC condition were investigated. Furthermore, the authors in [29] designed a hybrid transmission protocol and a user selection scheme for the multi-user underlay NOMA network. The authors in [30] optimized the system throughput for an UAV-assisted cooperative CR-NOMA network to attain the best performance under the imperfect SIC condition. In addition, the authors in [31] provided a general analysis framework in order to assess the coverage probability and ER of the STAR-RIS-NOMA networks. To reduce the average number of the lost data packets, the authors in [32] devised a new algorithm for the uplink energy harvesting-CR-NOMA networks. Li *et*

al. in [3] modeled a STAR-RIS assisted NOMA network with an illegal eavesdropper under the residual hardware impairments conditions. Further, with the aim of solving the secure communication problem brought on by the presence of eavesdroppers, the authors in [33] devised a secure communication strategy for the STAR-RIS-NOMA networks to maximize the secrecy rate.

A. Motivation and Contributions

The development of consumer IoT is in full bloom, which has penetrated into various fields of life, such as smart homes, healthcare, intelligent transportation, environmental monitoring, etc. The major objective of this paper is to assist future consumer IoT networks achieve spectrum and massive connectivity in resilient industry 5.0. Although there is a significant amount of literature available on STAR-RIS, CR and NOMA, the integration of the three techniques is still in its infancy. In [34], the authors presented a novel beamforming design scheme for the RIS-aided in band full-duplex consumer IoT networks. However, NOMA, STAR-RIS and CR were not taken into account. The authors in [35] introduced a NOMA-enabled backscatter network in automotive industry 5.0 and designed a framework to maximize the EE. The downside is that there is no mention of STAR-RIS and CR technologies. To maximize the EE, Fang *et al.* in [36] designed an algorithm for the STAR-RIS-MIMO-NOMA systems. However, it should be noted that the above literature did not take into account the potential benefits of utilizing CR technology. Guo *et al.* in [37] investigated a STAR-RIS empowered non-terrestrial vehicle network with NOMA and evaluate the outage performance of all secondary vehicles. To tackle the critical security challenges faced by communication, the authors in [38] developed an artificial intelligence-based framework for the underlay CR-NOMA networks to maximize the secrecy EE. Liang *et al.* in [39] proposed a RIS assisted CR-NOMA model aimed at maximizing the EE while ensuring the QoS for PUs. However, STAR-RIS was not taken into account.

Motivated by the numerous benefits offered by STAR-RIS, CR and NOMA, we present the novel STAR-RIS assisted overlay CR-NOMA based consumer IoT networks for resilient industry 5.0. To assess the performance of the proposed system, we derive the analytical expressions of the OP, ER and EE. The main contributions of this paper are given as follows:

- We investigate the performance of the passive STAR-RIS assisted overlay CR-NOMA based consumer IoT networks for resilient industry 5.0 under the Nakagami- m fading channels. The secondary transmitter assists the primary network transmission for access to the licensed bands. Due to the long distance between the secondary transmitter and consumer IoT devices, STAR-RIS is introduced to assist in the transmission of their messages.
- We calculate the analytical expressions of OP for the primary and secondary devices. The asymptotic performance of the devices under high signal-to-noise ratios (SNR) regions and the diversity orders are discussed. Based on the derived expressions, the reliable performance and the

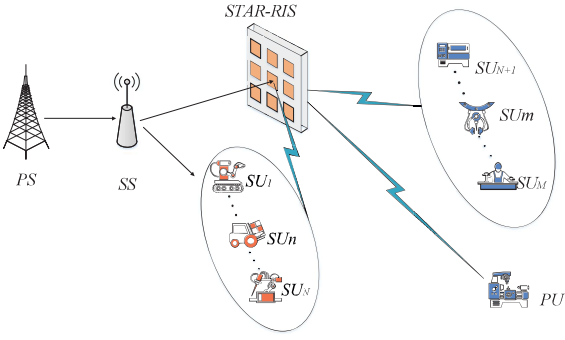


Fig. 1: The proposed system model in a resilient industry 5.0 environment

impact of the elements' number in STAR-RIS on the reliability of the considered system are assessed.

- The analytical expressions of ER for primary and secondary devices are deduced. The ER performance of the consumer electronic devices at high SNR regions is also investigated to gain insight into the STAR-RIS assisted CR-NOMA networks. In addition, the impact of the elements' numbers in STAR-RIS and the power allocation coefficients on the ER are analyzed.
- The EE for STAR-RIS assisted overlay CR-NOMA based consumer IoT networks in delay-tolerant transmission mode is analyzed. EE increase with the transmit SNR and the elements' number in STAR-RIS. Finally, we proved the superiority of the proposed networks through the Monte Carlo simulations.

B. Organization and Notations

The remainder of this paper is structured as follows. Section II describes the STAR-RIS assisted overlay CR-NOMA based consumer IoT networks for resilient industry 5.0. Section III infers the analytical expressions of OP, the outage behavior of devices under high SNR regions and diversity order. Section IV explores the ER, the asymptotic ER under high SNR regions and EE. Section V confirms the correctness of the analysis through Monte Carlo simulation. Section VI summarizes the full paper.

The following are the meanings of the characters referenced in this paper. $E(x)$ represents the expectation of the random variable x , $diag(\cdot)$ is a diagonal matrix. $\mathcal{CN}(\mu, \sigma^2)$ denotes the complex Gaussian random variable with mean μ and variance σ^2 . $\Gamma(\cdot)$ and $\gamma(\cdot)$ represent the gamma function and lower incomplete gamma function, respectively. $f_x(\cdot)$ and $F_x(\cdot)$ represent the probability density function (PDF) and the cumulative distribution function (CDF) of x .

II. SYSTEM MODEL

Fig. 1 depicts a simultaneously transmitting and reflecting reconfigurable intelligent surface (STAR-RIS) assisted cognitive radio (CR)-non-orthogonal multiple access (NOMA) network in resilient industry 5.0, which comprises a primary station (PS), a secondary transmitter (SS), a STAR-RIS, M secondary consumer Internet of Things (IoT) devices and a

primary consumer IoT device. It is assumed that there is no direct link between the PS and PU owing to severe fading or blockage [3], so the CR is introduced to assist the primary network in communication. Since SS is far away from devices, the STAR-RIS is installed to facilitate the transmission of messages between them. $SU_i, i \in \{1, \dots, N\}$ is situated on the front side of the STAR-RIS, which can pick up signals from both SS and STAR-RIS reflections. $SU_i, i \in \{N+1, \dots, M\}$ and PU are situated on the back side of STAR-RIS and can only receive the information transmitted by STAR-RIS. The channel coefficients for the links of PS-SS, SS-STAR-RIS, STAR-RIS- SU_n ($1 \leq n \leq N$), SS- SU_n , STAR-RIS- SU_m ($N+1 \leq m \leq M$), and STAR-RIS-PU can be represented as h_{ss} , $\mathbf{h}_{sr} \in \mathbb{C}^{1 \times L_r}$, $\mathbf{h}_{rn} \in \mathbb{C}^{L_r \times 1}$, h_{sn} , $\mathbf{h}_{rm} \in \mathbb{C}^{1 \times L_t}$, and $\mathbf{h}_{rp} \in \mathbb{C}^{L_t \times 1}$, respectively.

Without loss of generality, we presumptively believe that the channel gain from SS to $SU_i, i \in \{1, \dots, N\}$ and from STAR-RIS to $SU_i, i \in \{N+1, \dots, M\}$ is $|h_{su_1}|^2 \geq |h_{su_2}|^2 \geq \dots \geq |h_{su_N}|^2$ and $|h_{ru_{N+1}}|^2 \geq |h_{ru_{N+2}}|^2 \geq \dots \geq |h_{ru_M}|^2 \geq |h_{rp}|^2$, respectively. $\Phi_T = diag(\sqrt{\beta_1^t} e^{j\theta_1^t}, \dots, \sqrt{\beta_N^t} e^{j\theta_N^t}, \dots, \sqrt{\beta_N^t} e^{j\theta_N^t})$ and $\Phi_R = diag(\sqrt{\beta_1^r} e^{j\theta_1^r}, \dots, \sqrt{\beta_N^r} e^{j\theta_N^r}, \dots, \sqrt{\beta_N^r} e^{j\theta_N^r})$ are the transmitting and reflecting phase shifting matrices of the STAR-RIS, respectively. $\beta_n^t, \beta_n^r \in [0, 1]$ and $\theta_n^r, \theta_n^t \in [0, 2\pi]$ represent the amplitude and phase shift of the n -th element of the STAR-RIS¹. The following assumptions are considered: 1) both the PS, SS and the consumer electronic devices are equipped with a single antenna; 2) the element number in STAR-RIS is L ; 3) all channels are subject to Nakagami- m fading channels, i.e., $h_{ss} \sim Nakagami(m_{ss}, 1)$, $h_{su_i} \sim Nakagami(m_{su_i}, 1)$, $h_{sr,n} \sim Nakagami(m_{sr}, 1)$, $h_{ru_i,n} \sim Nakagami(m_{ru_i}, 1)$.

To facilitate hardware deployment, STAR-RIS adopts mode switching and the L elements are divided into two parts, one serving $SU_i, i \in \{1, \dots, N\}$ and the other serving $SU_i, i \in \{N+1, \dots, M\}$. L_r elements of the STAR-RIS completely reflect messages on the reflection links, while the remaining L_t elements transmit messages on the transmission link, $L_r + L_t = L$. According to the mode switching protocol in [40], we set the amplitude parameter to $\beta_k^t = 0$ and $\beta_n^r = 1$ when the L_r elements in reflection mode, and vice versa. We have $\beta_n^t = 1$ and $\beta_n^r = 0$ when L_t elements in transmission mode. STAR-RIS has full reflection and full transmission two modes in mode switching by adjusting the amplitude coefficient, which brings it the advantage of being simple to deploy.

The received message at SS from PS is given by

$$y_{ss} = h_{ps} \sqrt{d_{ps}^{-\alpha_{ps}}} P_p x_p + n_s, \quad (1)$$

where P_p indicates the transmit power of the PS, x_p refers to the normalized message of PU with $E(|x_p|^2) = 1$, d_{ps} and α_{ps} show the distance and path loss exponent for the PS-SS link, and $n_s \sim \mathcal{CN}(0, N_0)$ represents the complex additive white Gaussian noise (AWGN).

¹The discussion of STAR-RIS-CR-NOMA network in this paper is based on optimal conditions as in [16], and the performance of the system in the presence of non-optimal phase noise condition will be further studied in the future.

The SS sends the superposed message to the PU and secondary devices. $SU_i, i \in \{1, \dots, N\}$ receives messages from SS and STAR-RIS reflections, which can be written as

$$y_{su_n} = \left(h_{sn} \sqrt{d_{sn}^{-\alpha_{sn}}} + \mathbf{h}_{sr} \Phi_T \mathbf{h}_{rn} \sqrt{d_{sr}^{-\alpha_{sr}}} \sqrt{d_{rn}^{-\alpha_{rn}}} \right) \quad (2)$$

$$\times \left(\sqrt{a_1 P_s} x_p + \sqrt{a_2 P_s} \sum_{i=1}^M \sqrt{b_i} x_{s,i} \right) + n_n,$$

where d_{sn}, d_{sr}, d_{rn} and $\alpha_{sn}, \alpha_{sr}, \alpha_{rn}$ denote the distances and path loss exponents for the links of SS- SU_n , SS-STAR-RIS and STAR-RIS- SU_n , respectively. n_n denotes AWGN and it follows $n_n \sim \mathcal{CN}(0, N_0)$. a_1 and a_2 refer to the power allocation parameters for the primary and secondary message satisfying $a_1 > a_2, a_1 + a_2 = 1$. $x_{s,i}$ and b_i denote the message and the power allocation parameters for the i -th secondary devices, subject to $\sum_{i=1}^M b_i = 1, b_1 < \dots < b_n \dots < b_N < b_{N+1} \dots < b_m \dots < b_M$.

The received messages at SU_m from STAR-RIS can be written as

$$y_{su_m} = \mathbf{h}_{sr} \Phi_T \mathbf{h}_{rm} \sqrt{d_{sr}^{-\alpha_{sr}}} \sqrt{d_{rm}^{-\alpha_{rm}}} \quad (3)$$

$$\times \left(\sqrt{a_1 P_s} x_p + \sqrt{a_2 P_s} \sum_{i=1}^M \sqrt{b_i} x_{s,i} \right) + n_m.$$

The received message at PU can be given by

$$y_{rp} = \mathbf{h}_{sr} \Phi_T \mathbf{h}_{rp} \sqrt{d_{sr}^{-\alpha_{sr}}} \sqrt{d_{rp}^{-\alpha_{rp}}} \quad (4)$$

$$\times \left(\sqrt{a_1 P_s} x_p + \sqrt{a_2 P_s} \sum_{i=1}^M \sqrt{b_i} x_{s,i} \right) + n_p,$$

where d_{rm}, d_{rp} and α_{rm}, α_{rp} denote the distances and path loss exponents for the links of STAR-RIS- SU_m and STAR-RIS-PU, respectively. n_m and n_p denote AWGN with mean power N_0 .

A. Received signal-to-interference-plus-noise (SINR)

Based on the above analysis, the SINR for decoding x_p at SS can be represented as

$$\gamma_{ss}^{x_p} = \frac{|h_{ss}|^2 d_{ss}^{-\alpha_{ss}} P_p}{N_0}. \quad (5)$$

The SINR of decoding x_p at the PU can be expressed as

$$\gamma_{pu} = \frac{|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rp}|^2 d_{sr}^{-\alpha_{sr}} d_{rp}^{-\alpha_{rp}} a_1 P_s}{|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rp}|^2 d_{sr}^{-\alpha_{sr}} d_{rp}^{-\alpha_{rp}} a_2 \sum_{i=1}^M b_i P_s + N_0}. \quad (6)$$

The SINR for SU_m to decode PU's message x_p , SU_{j_1} 's message $x_{j_1}, j_1 \geq m$ and its own message are respectively written as

$$\gamma_{su_m, p} = \frac{|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rp}|^2 d_{sr}^{-\alpha_{sr}} d_{rp}^{-\alpha_{rp}} a_1 P_s}{|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rp}|^2 d_{sr}^{-\alpha_{sr}} d_{rp}^{-\alpha_{rp}} a_2 \sum_{i=1}^M b_i P_s + N_0}, \quad (7)$$

$$\gamma_{su_m, j_1} = \frac{|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rm}|^2 d_{sr}^{-\alpha_{sr}} d_{rm}^{-\alpha_{rm}} a_2 b_{j_1} P_s}{|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rm}|^2 d_{sr}^{-\alpha_{sr}} d_{rm}^{-\alpha_{rm}} P_s \Delta_1 + N_0}, \quad (8)$$

$$\gamma_{su_m} = \frac{|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rm}|^2 d_{sr}^{-\alpha_{sr}} d_{rm}^{-\alpha_{rm}} a_2 b_m P_s}{|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rm}|^2 d_{sr}^{-\alpha_{sr}} d_{rm}^{-\alpha_{rm}} P_s \Delta_2 + N_0}, \quad (9)$$

where $\Delta_1 = \sum_{q=1}^{j_1-1} a_2 b_q$ and $\Delta_2 = \sum_{q=1}^{m-1} a_2 b_q$.

The SINR for SU_n to decode PU's message x_p , SU_{j_2} 's message $x_{j_2}, n \leq j_2 \leq N$ and its own message be given by

$$\gamma_{su_n, p} = \frac{|h_{sn} + \mathbf{h}_{sr} \Phi_R \mathbf{h}_{rn}|^2 d_{sn}^{-2\alpha_{sn}} a_1 P_s}{|h_{sn} + \mathbf{h}_{sr} \Phi_R \mathbf{h}_{rn}|^2 d_{sn}^{-2\alpha_{sn}} a_2 \sum_{i=1}^M b_i P_s + N_0}, \quad (10)$$

$$\gamma_{su_n, j_2} = \frac{|h_{sn} + \mathbf{h}_{sr} \Phi_R \mathbf{h}_{rn}|^2 d_{sn}^{-2\alpha_{sn}} a_2 b_{j_2} P_s}{|h_{sn} + \mathbf{h}_{sr} \Phi_R \mathbf{h}_{rn}|^2 d_{sn}^{-2\alpha_{sn}} P_s \Delta_3 + N_0}, \quad (11)$$

$$\gamma_{su_n} = \frac{|h_{sn} + \mathbf{h}_{sr} \Phi_R \mathbf{h}_{rn}|^2 d_{sn}^{-2\alpha_{sn}} a_2 b_n P_s}{|h_{sn} + \mathbf{h}_{sr} \Phi_R \mathbf{h}_{rn}|^2 d_{sn}^{-2\alpha_{sn}} P_s \Delta_4 + N_0}, \quad (12)$$

where $\Delta_3 = \sum_{q=1}^{j_2-1} a_2 b_q$ and $\Delta_4 = \sum_{q=1}^{n-1} a_2 b_q$.

B. Channel Statistics of SU_m

The channel statistic by the moment matching method is obtained for analyzing the outage behavior of SU_m .

Lemma 1. Let $Y = \sum_{l=1}^{L_t} |h_{sr}| |h_{rm}|$, the distribution of Y can be approximated as $Y \sim \Gamma(K_Y, \theta_Y)$ and the analytical expression of the PDF for the cascaded channel Y can be written as [16]

$$f_Y(x) = \frac{1}{\theta_Y^{K_Y} \Gamma(K_Y)} x^{K_Y-1} e^{-\frac{x}{\theta_Y}}, \quad (13)$$

where $K_Y = \frac{L_t \mu_m^2}{1 - \mu_m^2}$, $\theta_Y = \frac{1 - \mu_m^2}{\mu_m}$ and $\mu_m = E[|h_{sr}| |h_{rm}|] = \left(\frac{1}{m_{sr} m_{rm}} \right)^{\frac{1}{2}} \frac{\Gamma(m_{sr} + \frac{1}{2}) \Gamma(m_{rm} + \frac{1}{2})}{\Gamma(m_{sr}) \Gamma(m_{rm})}$.

The channel statistic of the PU is the same as SU_m .

C. Channel Statistics of SU_n

The series form of Laguerre polynomials is adopted to acquire the channel statistic and the results will be applied to discuss the outage behavior for SU_n .

Lemma 2. Let $X = |h_{sr}| |h_{rn}|$, the PDF for the cascaded channel X is given as

$$f_X(z) = \frac{z^{\frac{m_{sr} + m_{rn}}{2}} - 1}{\Gamma(m_{sr}) \Gamma(m_{rn})} K_{m_{rn} - m_{sr}}(2\sqrt{z}). \quad (14)$$

Let $S = \sum_{l=1}^{L_r} |h_{sr}| |h_{rn}|$. Since it is quite difficult to acquire the PDF of S from (14), we obtain the PDF of S through the series form of Laguerre polynomials [41]

$$f_S(x) \approx \frac{x^{\varphi_n}}{\phi_n^{\varphi_n + 1} \Gamma(\varphi_n + 1)} e^{-\frac{x}{\phi_n}}, \quad (15)$$

where $\varphi_n = \frac{\mu_n^2 L_r}{V_n} - 1$, $V_n = 1 - \mu_n^2$, $\phi_n = \frac{V_n}{\mu_n}$ and $\mu_n = E[|h_{sr}| |h_{rn}|] = \left(\frac{1}{m_{sr} m_{rn}} \right)^{\frac{1}{2}} \frac{\Gamma(m_{sr} + \frac{1}{2}) \Gamma(m_{rn} + \frac{1}{2})}{\Gamma(m_{sr}) \Gamma(m_{rn})}$.

III. OUTAGE PROBABILITY ANALYSIS

The reliability of the STAR-RIS assisted overlay CR-NOMA based consumer IoT networks for resilient industry 5.0 are evaluated in this section. Specifically, the analytical

expressions for the outage probability (OP) and the asymptotic behavior of consumer electronic devices in high SNR regions are derived. To gain more insight into the network, the diversity orders are discussed.

A. The Outage Probability of PU

The PU will not be in outage only when both the SS and PU decode the message x_p successfully. Thus, the OP of the PU can be indicated as

$$P_{out}^{PU} = 1 - \Pr(\gamma_{ss}^{x_p} > \gamma_{th}^{x_p}, \gamma_{pu} > \gamma_{th}^{x_p}), \quad (16)$$

where $\gamma_{th}^{x_p} = 2^{R_{th}^{x_p}} - 1$ is the target SNR and $R_{th}^{x_p}$ is the target rate of detecting the message x_p .

Theorem 1. For the STAR-RIS-CR-NOMA network, the OP of PU under the Nakagami- m fading channels is given by

$$P_{out}^{PU} = 1 - \theta_0 \left(\frac{1}{\theta_p} \right)^{-K_p} \frac{1}{\Gamma(K_p) \theta_p^{K_p}} \Gamma \left(K_p, \frac{\sqrt{\theta_1}}{\theta_p} \right), \quad (17)$$

where $\theta_0 = e^{-A} \sum_{m=0}^{m_{ss}-1} \frac{A^m}{m!}$, $A = \frac{m_{ss} \gamma_{th}^{x_p} N_0}{\Omega_{ss} P_p d_{sr}^{-\alpha_{ss}}}$, $\theta_1 = \frac{\gamma_{th}^{x_p} N_0}{d_{sr}^{-\alpha_{sr}} d_{rp}^{-\alpha_{rp}} P_s (a_1 - \gamma_{th}^{x_p} a_2)}$.

Proof: Please see Appendix A. ■

Corollary 1. To get a clear exploration of the reliable performance, the asymptotic OP under the high SNR regions for PU can be given by

$$P_{out,\infty}^{PU} = 1 - \theta_0 \left(\frac{1}{\theta_p} \right)^{-K_p} \frac{1}{\Gamma(K_p) \theta_p^{K_p}} \Gamma \left(K_p, \frac{\sqrt{\theta_1'}}{\theta_p} \right), \quad (18)$$

where $\theta_1' = \frac{\gamma_{th}^{x_p}}{d_{sr}^{-\alpha_{sr}} d_{rp}^{-\alpha_{rp}} (a_1 - \gamma_{th}^{x_p} a_2)}$.

Proof: Bring the transmit SNR $\gamma = \frac{P_s}{N_0}$, $\gamma \rightarrow \infty$ to (17), we can obtain (18). ■

B. The Outage Probability of SU_m

The following conditions must be met by SU_m in order to avoid outage behavior: 1) SS decodes the message x_p successfully; 2) SU_m decodes the message x_p of the primary device successfully; 3) SU_m successfully decodes the message x_{j_1} of SU_{j_1} ; 4) SU_m decodes its own message successfully. Therefore, its OP is given as

$$P_{out}^m = 1 - \Pr(E_{ss,p}) \Pr(E_{sm,p} \cap E_{sm,1} \cap \dots \cap E_{sm,n}), \quad (19)$$

where $E_{ss,p} = \{\gamma_{ss}^{x_p} > \gamma_{th}^{x_p}\}$, $E_{sm,p} = \{\gamma_{sum,p} > \gamma_{th}^{x_p}\}$ and $E_{sm,j_1} = \{\gamma_{sum,j_1} > \gamma_{th}^{x_{j_1}}\}$. $E_{ss,p}$ and $E_{sm,p}$ denote that the SS and SU_m decode the message x_p of the PU successfully. E_{sm,j_1} means that the SU_m successfully decodes the message x_{j_1} of the SU_{j_1} , while $\gamma_{th}^{x_{j_1}} = 2^{R_{th}^{x_{j_1}}} - 1$ represents the target SNR of detecting the message x_{j_1} .

Theorem 2. The analytic expression of the OP for SU_m can

be given by

$$P_{out}^m = 1 - \theta_0 \left(\frac{1}{\theta_x} \right)^{-2K_x} \left(\frac{1}{\Gamma(K_x) \theta_x^{K_x}} \right)^2 \Gamma \left(K_x, \frac{\sqrt{\theta_2}}{\theta_x} \right) \times \Gamma \left(K_x, \frac{\sqrt{\theta_3}}{\theta_x} \right), \quad (20)$$

where $\theta_2 = \frac{\gamma_{th}^{x_p} N_0}{d_{sr}^{-\alpha_{sr}} d_{rm}^{-\alpha_{rm}} P_s (a_1 - \gamma_{th}^{x_p} a_2)}$, $\theta_3 = \frac{\gamma_{th}^{j_1} N_0}{d_{sr}^{-\alpha_{sr}} d_{rm}^{-\alpha_{rm}} P_s (a_2 b_{j_1} - \gamma_{th}^{j_1} \Delta_1)}$, $\theta_3^* = \max_{1 \leq j_1 \leq M} \theta_3$.

Proof: According to (13) and (19), (20) will be acquired. ■

Corollary 2. The asymptotic expression of OP for SU_m under high SNR regions can be represented as

$$P_{out,\infty}^m = 1 - \theta_0 \left(\frac{1}{\theta_x} \right)^{-2K_x} \left(\frac{1}{\Gamma(K_x) \theta_x^{K_x}} \right)^2 \Gamma \left(K_x, \frac{\sqrt{\theta_2'}}{\theta_x} \right) \times \Gamma \left(K_x, \frac{\sqrt{\theta_3'}}{\theta_x} \right), \quad (21)$$

where $\theta_2' = \frac{\gamma_{th}^{x_p}}{d_{sr}^{-\alpha_{sr}} d_{rm}^{-\alpha_{rm}} (a_1 - \gamma_{th}^{x_p} a_2)}$, $\theta_3' = \frac{\gamma_{th}^{j_1}}{d_{sr}^{-\alpha_{sr}} d_{rm}^{-\alpha_{rm}} (a_2 b_{j_1} - \gamma_{th}^{j_1} \Delta_1)}$ and $\theta_3'^* = \max_{1 \leq j_1 \leq M} \theta_3'$.

Proof: Bring $\gamma = \frac{P_s}{N_0}$, $\gamma \rightarrow \infty$ to (20), we can obtain (21). ■

C. The Outage Probability of SU_n

To avoid outage at SU_n , the following conditions need to be met: 1) SS can decode the message x_p of the PU successfully; 2) SU_n decodes the message x_p successfully; 3) SU_n successfully decodes the message x_{j_2} of the SU_{j_2} ; 4) SU_n successfully decodes its own message. Accordingly, the OP of SU_n is given by

$$P_{out}^n = 1 - \Pr(E_{ss,p}) \Pr(E_{sn,p} \cap E_{sn,1} \cap \dots \cap E_{sn,n}), \quad (22)$$

where $E_{sn,p} = \{\gamma_{sun,p} > \gamma_{th}^{x_p}\}$ and $E_{sn,j_1} = \{\gamma_{sun,j_2} > \gamma_{th}^{x_{j_1}}\}$. $E_{sn,p}$ denotes the case when SU_n decodes the message x_p of the primary device successfully, while E_{sn,j_2} represents the case when SU_n successfully decodes the message x_{j_2} of the SU_{j_2} . Finally, $\gamma_{th}^{x_{j_2}} = 2^{R_{th}^{x_{j_2}}} - 1$ represents the target SNR of devices SU_{j_2} for detecting the message x_{j_2} .

Theorem 3. The analytic expression of the OP for SU_n under the Nakagami- m fading channel can be represented as

$$P_{out}^n = 1 - \theta_0 (1 - \Delta_5 \times \Delta_6 - \Delta_7 \times \Delta_8 \times \Delta_9) \times (1 - \Delta_5 \times \Delta_{10} - \Delta_{11} \times \Delta_{12} \times \Delta_{13}), \quad (23)$$

where $\Delta_5 = \frac{1}{\phi_n^{\varphi_n+1} \Gamma(\varphi_n+1)} \left(\frac{1}{\phi_n} \right)^{-\varphi_n-1}$, $\Delta_6 = \gamma \left(\varphi_n + 1, \frac{\sqrt{\theta_4}}{\phi_n} \right)$, $\Delta_7 = e^{-\sqrt{\theta_4}} (m_{ss} - 1)!$, $\Delta_8 = \sum_{k=0}^{m_{ss}-1} \sum_{n=0}^{k_1} \binom{k_1}{n} \frac{(\sqrt{\theta_4})^{k_1-n}}{k_1!} \left(\frac{1}{\phi_n} - 1 \right)^{-(n+\varphi_n)-1}$, $\Delta_9 = \gamma \left(n + \varphi_n + 1, \sqrt{\theta_4} \left(\frac{1}{\phi_n} - 1 \right) \right)$, $\Delta_{10} =$

$$\gamma \left(\varphi_n + 1, \frac{\sqrt{\theta_5^*}}{\phi_n} \right), \Delta_{11} = e^{-\sqrt{\theta_5^*}} (m_{ss} - 1)!, \Delta_{12} = \sum_{k=0}^{m_{ss}-1} \sum_{n=0}^{k_1} \binom{k_1}{n} \frac{(\sqrt{\theta_5^*})^{k_1-n}}{k_1!} \left(\frac{1}{\phi_n} - 1 \right)^{-(n+\varphi_n)-1},$$

$$\Delta_{13} = \gamma \left(n + \varphi_n + 1, \sqrt{\theta_5^*} \left(\frac{1}{\phi_n} - 1 \right) \right), \theta_4 = \frac{\gamma_{th}^{x_p} N_0}{d_{sn}^{-2\alpha_{sn}} P_s \left(a_1 - \gamma_{th}^{x_p} a_2 \sum_{i=1}^M b_i \right)}, \theta_5 = \frac{\gamma_{th}^{j_2} N_0}{d_{sn}^{-2\alpha_{sn}} P_s \left(a_2 b_{j_2} - \Delta_3 \right)} \text{ and}$$

$$\theta_5^* = \max_{N+1 \leq j_2 \leq M} \theta_5.$$

Proof: Please see Appendix B. ■

Corollary 3. At high SNR regions, the asymptotic expression of OP for SU_n can be represented as

$$P_{out,\infty}^n = 1 - \theta_0 (1 - \Delta_{13} \times \Delta'_{14} - \Delta'_{15} \times \Delta'_{16} \times \Delta'_{17}) \times (1 - \Delta_5 \times \Delta'_{10} - \Delta'_{11} \times \Delta'_{12} \times \Delta'_{13}), \quad (24)$$

where $\Delta'_6 = \gamma \left(\varphi_n + 1, \frac{\sqrt{\theta'_4}}{\phi_n} \right)$,

$$\Delta'_7 = \sum_{k=0}^{m_{ss}-1} \sum_{n=0}^{k_1} \binom{k_1}{n} \frac{e^{-\sqrt{\theta'_4}} (\sqrt{\theta'_4})^{k_1-n}}{k_1!} \left(\frac{1}{\phi_n} - 1 \right)^{-(n+\varphi_n)-1},$$

$$\Delta'_9 = \gamma \left(n + \varphi_n + 1, \sqrt{\theta'_4} \left(\frac{1}{\phi_n} - 1 \right) \right), \Delta'_{10} = \gamma \left(\varphi_n + 1, \frac{\sqrt{\theta_5^{*'}}}{\phi_n} \right), \Delta'_{11} = e^{-\sqrt{\theta_5^{*'}}} (m_{ss} - 1)!, \Delta'_{12} = \sum_{k=0}^{m_{ss}-1} \sum_{n=0}^{k_1} \binom{k_1}{n} \frac{(\sqrt{\theta_5^{*'}})^{k_1-n}}{k_1!} \left(\frac{1}{\phi_n} - 1 \right)^{-(n+\varphi_n)-1},$$

$$\Delta'_{13} = \gamma \left(n + \varphi_n + 1, \sqrt{\theta_5^{*'}} \left(\frac{1}{\phi_n} - 1 \right) \right), \theta'_4 = \frac{\gamma_{th}^{x_p}}{d_{sn}^{-2\alpha_{sn}} \left(a_1 - \gamma_{th}^{x_p} a_2 \sum_{i=1}^M b_i \right)}, \theta'_5 = \frac{\gamma_{th}^{j_2}}{d_{sn}^{-2\alpha_{sn}} \left(a_2 b_{j_2} - \gamma_{th}^{j_2} \Delta_3 \right)} \text{ and}$$

$$\theta_5^{*' } = \max_{1 \leq j_2 \leq M} \theta'_5.$$

Proof: Bring $\gamma = \frac{P_s}{N_0}$, $\gamma \rightarrow \infty$ to (23), we can obtain (24). ■

D. Diversity Order

We investigate the diversity orders for the consumer electronic devices to further understand the STAR-RIS assisted CR-NOMA systems. The following is the definition of the diversity order:

$$d = - \lim_{\gamma \rightarrow \infty} \frac{\log(P_{out}^\infty)}{\log \gamma}, \quad (25)$$

where $\gamma = \frac{P_s}{N_0}$.

Corollary 4. The diversity orders of PU, SU_m , SU_{j_1} , SU_n and SU_{j_2} can be represented as

$$d_{PU} = d_{SU_m} = d_{SU_{j_1}} = d_{SU_n} = d_{SU_{j_2}} = 0. \quad (26)$$

Proof: According to (18), (21) and (24), the result of (26) can be acquired. ■

Remark 1. From Corollaries 1-4, and Theorems 1-3, it can be observed that the OP decreases with the transmit SNR, while the reliability of the STAR-RIS assisted CR-NOMA networks increases and finally approaching a constant at high SNR regions. This means there are error floors, which leads

to the diversity orders of 0. In addition, the reliability of the considered network for resilient industry 5.0 gradually increases with the elements' numbers of STAR-RIS.

IV. ERGODIC RATE ANALYSIS

In this section, the ergodic rate (ER) performance of the STAR-RIS assisted overlay CR-NOMA networks are explored. Specifically, we derive the analytical expressions of ER and the asymptotic ER for the devices at high SNR regions to acquire a more profound comprehension of the system.

A. The Ergodic Rate of PU

Based on the previous analysis, the ER of PU can be derived as

$$R_{PU} = E [\log_2 (1 + \gamma_{pu})]. \quad (27)$$

Unfortunately, it is extremely difficult to acquire the exact expression, so we look for approximate but exact values instead.

Theorem 4. The ER for PU in the STAR-RIS assisted CR-NOMA networks is given by

$$R_{PU} = \frac{(N_t (1 - \mu_{pu}^2) + \mu_{pu}^2) d_{sr}^{-a_{sr}} d_{rpu}^{-a_{rp}} \alpha_1 P_s}{(N_t (1 - \mu_{pu}^2) + \mu_{pu}^2) d_{sr}^{-a_{sr}} d_{rpu}^{-a_{rp}} \alpha_2 \sum_{i=1}^M b_i P_s + N_0}. \quad (28)$$

Proof: Please see Appendix C. ■

Corollary 5. The asymptotic expression of ER for PU at high SNR regions can be represented as

$$R_{PU,\infty} = \frac{\alpha_1}{\alpha_2 \sum_{i=1}^M b_i}. \quad (29)$$

B. The Ergodic Rate of SU_m

The analytical expression of the ER for SU_m can be represented as

$$R_m = E [\log_2 (1 + \gamma_{su_m})]. \quad (30)$$

Similarly, we apply Jensen's inequality to calculate the approximate value of the ER for the SU_m .

Theorem 5. For the STAR-RIS-CR-NOMA networks, the ER for SU_m under the Nakagami- m fading channels is given by

$$R_m = \frac{(L_t (1 - \mu_m^2) + \mu_m^2) d_{sr}^{-a_{sr}} d_{rm}^{-a_{rm}} \alpha_2 b_m P_s}{(L_t (1 - \mu_m^2) + \mu_m^2) d_{sr}^{-a_{sr}} d_{rm}^{-a_{rm}} P_s \Delta_2 + N_0}. \quad (31)$$

Corollary 6. The asymptotic expression of ER for SU_m at high SNR regions can be given by

$$R_{m,\infty} = \frac{\alpha_2 b_m}{\Delta_2}. \quad (32)$$

C. The Ergodic Rate of SU_n

The ER for SU_n can be written as

$$R_n = E [\log_2 (1 + \gamma_{su_n})]. \quad (33)$$

Theorem 6. Under Nakagami- m fading channel, the ER for the SU_n is given by

$$R_n = \frac{K_Z \theta_Z d_{sn}^{-2\alpha_{sn}} a_2 b_n P_s}{K_Z \theta_Z d_{sn}^{-2\alpha_{sn}} P_s \Delta_4 + N_0}, \quad (34)$$

where $K_Z = \frac{\mu_Z^2}{\mu_Z^{(2)} - \mu_Z^2}$, $\theta_Z = \frac{\mu_Z^{(2)} - \mu_Z^2}{\mu_Z^2}$, $\mu_Z = \frac{\Gamma(m_{sn}+1)}{m_{sn}\Gamma(m_{sn})} + \frac{\Gamma(L_r K_S + 2)\theta_S^2}{\Gamma(L_r K_S)} + \frac{2\Gamma(m_{sn} + \frac{1}{2})\Gamma(L_r K_S + 1)\theta_S}{(m_{sn})^{\frac{1}{2}}\Gamma(m_{sn})\Gamma(L_r K_S)}$, $\mu_Z^{(2)} = \frac{\Gamma(m_{sn}+2)}{m_{sn}^2\Gamma(m_{sn})} + \frac{\Gamma(L_r K_S + 4)\theta_S^4}{\Gamma(L_r K_S)} + \frac{6\Gamma(m_{sn}+1)\Gamma(L_r K_S + 2)\theta_S^2}{m_{sn}\Gamma(m_{sn})\Gamma(L_r K_S)} + \frac{4\Gamma(m_{sn} + \frac{3}{2})\Gamma(L_r K_S + 1)\theta_S}{(m_{sn})^{\frac{3}{2}}\Gamma(m_{sn})\Gamma(L_r K_S)} + \frac{4\Gamma(m_{sn} + \frac{1}{2})\Gamma(L_r K_S + 3)\theta_S^3}{(m_{sn})^{\frac{1}{2}}\Gamma(m_{sn})\Gamma(L_r K_S)}$, $K_S = \frac{\mu_n^2}{\mu_n^{(2)} - \mu_n^2}$ and $\theta_S = \frac{\mu_n^{(2)} - \mu_n^2}{\mu_n^2}$.

Proof: Please see Appendix D. ■

Corollary 7. The asymptotic ER for SU_n at high SNR regions is written as

$$R_{n,\infty} = \frac{\alpha_2 b_n}{\Delta_4}. \quad (35)$$

D. Energy efficiency

Energy efficiency (EE) is one of the key metrics to evaluate the performance of wireless communication systems. Generally speaking, delay-limited and delay-tolerant are its two transmission modes. The delay-tolerant transmission mode can be defined as the sum data rate divided by the total power consumption [42]. The following is the definition expression:

$$\eta = \frac{\text{Total data rate}}{\text{Total energy consumption}} \text{ (bit/Joule)}, \quad (36)$$

The expression for the EE of the proposed system is represented as

$$\eta = \frac{R_{total}}{P_p + P_s + P_{STAR-RIS} + P_c}. \quad (37)$$

where $R_{total} = R_{PU} + R_m + R_n$, $P_{STAR-RIS}$ and P_c represent the hardware static dissipated power at the STAR-RIS and the constant circuit power consumption, respectively.

Remark 2. From **Corollaries 5-7**, and **Theorems 4-6**, we can find that the ER increases with the P_s , and the ER performance of the STAR-RIS-CR-NOMA networks increases and finally approaching a constant in high SNR regions. In addition, the ER performance of the considered network keeps increasing with the element number of STAR-RIS.

V. NUMERICAL RESULTS

We confirm the accuracy of the calculation by means of 10^5 Monte Carlo simulation experiments [3]. The corresponding simulation parameters are presented in Table I unless otherwise noted. We assume the same parameters in the NOMA and OMA scenarios to ensure the fairness of the comparison. In addition, we set $M = 4$, $n = 1$, $j_2 = 2$, $m = 3$ and $j_1 = 4$, $L_r = L_t = 10$ [43].

Fig. 2 plots the OP versus the transmit SNR for the consumer electronic devices. It can be observed that the OP decreases with the SNR and finally converges to a constant value. The results show that the reliability increases with SNR and achieves a saturation state at high SNR regions. It indicates

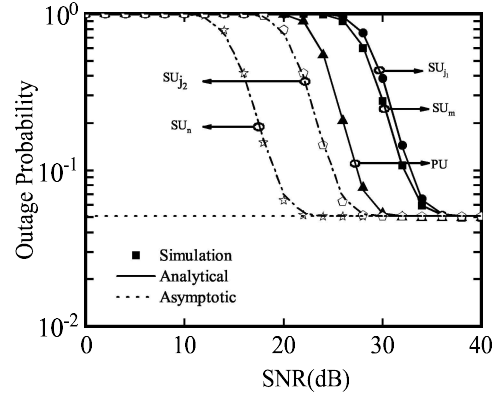


Fig. 2: The OP versus transmit SNR for different devices.

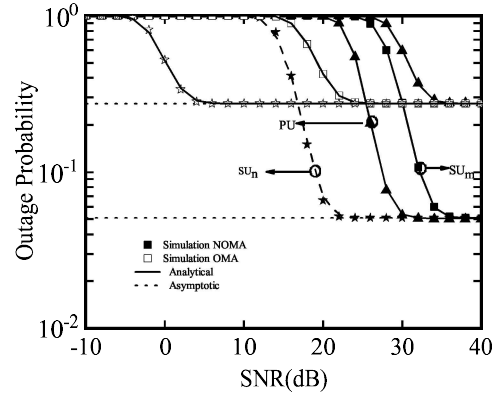


Fig. 3: The OP versus transmit SNR in NOMA and OMA conditions.

that continuing increasing the transmit SNR of the secondary devices after the saturation state will no longer be effective in enhancing the reliable performance of the STAR-RIS-CR-NOMA based consumer IoT networks in resilient industry 5.0. In addition, we find that the reflecting devices have superior reliable performance compared to the transmitting devices, which is due to the fact that there exists a direct link between SS and reflecting consumer electronic devices.

Fig. 3 depicts the OP of the devices in resilient industry 5.0 under NOMA and OMA scenarios. We assume that the parameters of the devices are the same in NOMA and OMA scenarios to ensure the fairness of the comparisons made. It is obvious to see that compared to OMA, PU has superior reliable performance in NOMA. The cause of this is that NOMA can enable numerous users to concurrently share the same wireless resources. For SU_n and SU_m , NOMA performs better in high SNR regions, while its performance is worse in low SNR regions. This is because the SIC processes need to be executed to detect their own messages.

The impact of the STAR-RIS element number on system reliability is seen in Fig. 4. We set the target SNR as $\gamma_{th}^{x_p} = 0.001$, $\gamma_{th}^{x_m} = 0.001$, $\gamma_{th}^{x_{j_2}} = 0.001$ and $L_t = L_r = L_\psi$. It is evident that when N rises, the OP decreases, whereas the reliability of the network in resilient industry 5.0 gradually

Table 1. TABLE OF PARAMETERS FOR NUMERICAL RESULTS [43]

Channel fading parameters	$\{m_{ss}, m_{sr}, m_{rp}, m_{rm_{j1}}, m_{rm}, m_{sn_{j2}}, m_{sn}, m_{rn_{j2}}, m_{rn}\} = \{1, 0.7, 9, 3, 2, 9, 3, 1.8, 1.7\}$
Power allocation coefficients	$\{a_1, a_2, b_{m_{j1}}, b_m, b_{n_{j2}}, b_n\} = \{0.6, 0.4, 0.4, 0.3, 0.2, 0.1\}$
The distance parameters	$\{d_{ss}, d_{sr}, d_{rpu}, d_{rm_{j1}}, d_{rm}, d_{sn_{j2}}, d_{sn}, d_{rn_{j2}}, d_{rn}\} = \{10, 10, 100, 90, 80, 20, 10, 40, 10\}$
Path loss exponents	$a = 2$
Target rate	$\{R_{th}^{x_p}, R_{th}^{x_{j1}}, R_{th}^{x_m}, R_{th}^{x_{j2}}, R_{th}^{x_n}\} = \{0.015, 0.0015, 0.015, 0.015, 0.0015\}$

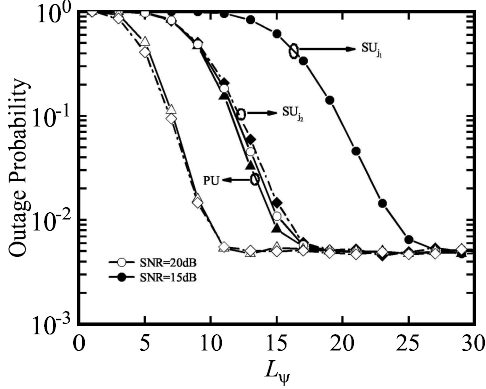


Fig. 4: The OP versus the elements number in STAR-RIS

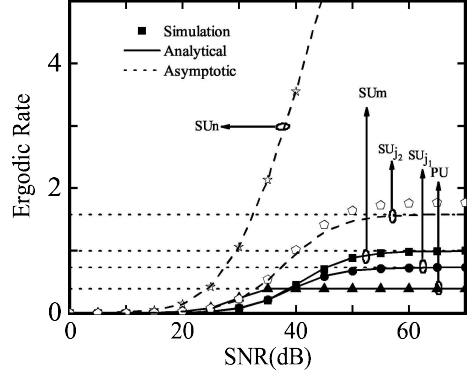


Fig. 6: The ER versus the transmit SNR for different devices

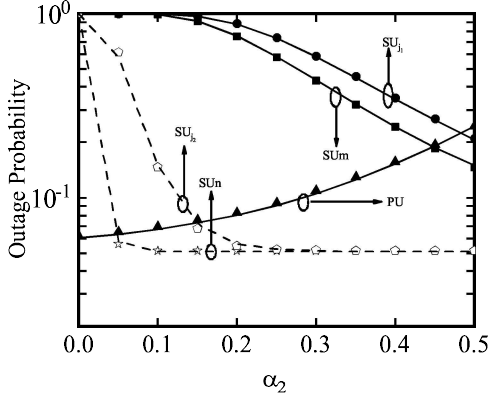
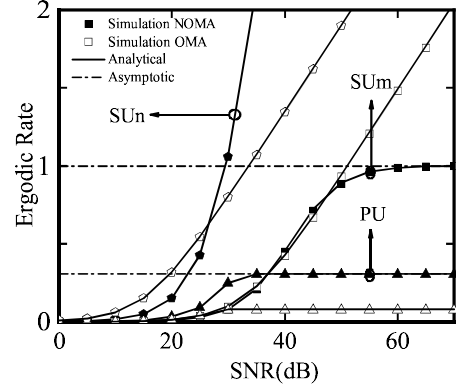
Fig. 5: The OP versus the a_2 for different devices

Fig. 7: The ER versus transmit SNR under NOMA and OMA conditions

increases. Eventually, the OP converges to a fixed value at high SNR regions. The explanation is that the larger amount of elements in STAR-RIS, can yield better control of the communication links. However, increasing the elements number is no longer effective for the reliability of the STAR-RIS-CR-NOMA networks after the performance is saturated.

The effect of power allocation coefficient a_2 on OP for the consumer electronic devices is shown in Fig. 5. It can be found that as the a_2 increases, the OPs of SUs decrease, while the OPs of PU increase. This is due to the fact that when a_2 grows greater, the less power is allocated to the PU and the more likely an outage is to occur, and vice versa. In addition, the probability of outage in reflective devices are lower than that for transmit devices, as there is a direct connection channel between reflective devices and SS.

Fig. 6 depicts the relationship between ER and the transmit SNR for the devices. The parameters are set-

ting as $\{m_{ss}, m_{sr}, m_{rp}, m_{rm_{j1}}, m_{sn_{j2}}, m_{sn}, m_{rn_{j2}}, m_{rn}\} = \{5, 3, 8, 6, 6, 5, 5\}$, $\{a_{ss}, a_{sr}, a_{rp}, a_{rm_{j1}}, a_{rm}, a_{rn}, a_{rn_{j1}}\} = 1.8$, $\{a_{sn}, a_{sn_{j2}}\} = 3.6$. Noticeable from Fig. 6, the ERs of the devices increase with the transmit power P_s and eventually converge to be constant. However, the ER of SU_n increases with the SNR. This is due to the presence of the perfect SIC, which allows SU_n to decode its own message without interference.

Fig. 7 shows the ERs of devices in resilient industry 5.0 under NOMA and OMA scenarios. It can be plainly viewed that the ER of PU is higher in NOMA scenario. The reason is that NOMA enables plenty users to concurrently share the same wireless resources. In the high SNR regions, SU_n and SU_m have better ERs in OMA scenario. The cause is that they need to perform SIC operations when decoding their own messages in NOMA network, while in OMA network, there

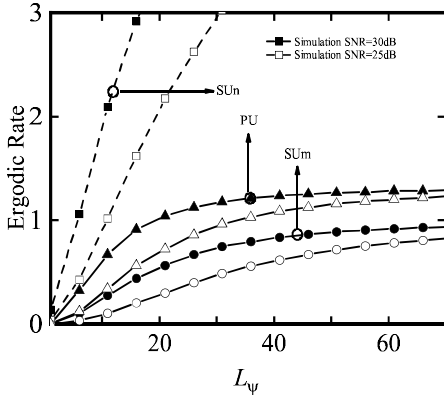


Fig. 8: The ER versus the elements number in STAR-RIS

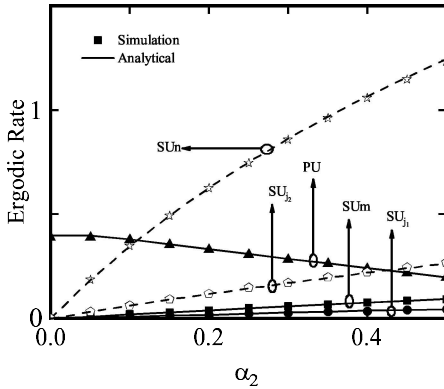


Fig. 9: The ER versus a_2 for different devices

is no interference when decoding their own messages.

Fig. 8 plots the relationship of the ER and the number of STAR-RIS elements for the STAR-RIS assisted CR-NOMA networks at different transmit SNRs. We set the $\{m_{ss}, m_{sr}, m_{rp}, m_{rm_{j1}}, m_{sn_{j2}}, m_{sn}, m_{rn_{j2}}, m_{rn}\} = \{5, 3, 8, 6, 6, 5, 5\}$, $\{a_{ss}, a_{sr}, a_{rp}, a_{rm_{j1}}, a_{rm}, a_{rn}, a_{rn_{j1}}\} = 1.6$, $\{a_{sn}, a_{sn_{j2}}\} = 3.2$. As we can observe from Fig. 8, the ERs of devices increase with the elements number of STAR-RIS. It is attributed to the truth that the effectiveness of STAR-RIS in controlling communication links increases with the element number. The ER of SU_n is more sensitive than SU_m . This is because the received messages at SU_n is not only coming from SS, but also from the reflection of STAR-RIS. In addition, we find that the ERs of devices increase with the transmit SNR when the elements number of STAR-RIS is constant.

Fig. 9 plots the impact of a_2 on ER for the consumer electronic devices. We can observe that the theoretical analysis is in good match with the simulation results, which demonstrates the correctness of our study. It is shown that the ER of SUs consistently increases and the ER of PU keeps decrease with a_2 . This is because the larger a_2 , the greater the power allocated to SUs, so its ER continues to increase. This result can be obtained from (28), (31), (34).

Fig. 10 depicts the OP and ER versus the distance d for the

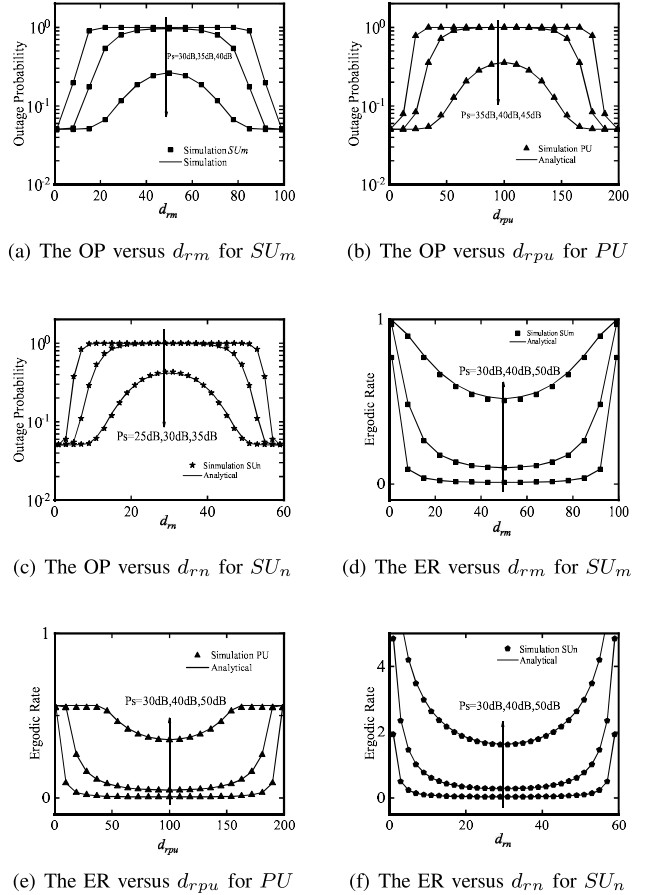


Fig. 10: The OP and ER versus the distance

different consumer electronic devices in resilient industry 5.0. We can see that the OPs of the devices increase with distance and then start to decrease after reaching a certain value. d has a worst value that maximises OP. The more it deviates from this worst value, the smaller the OP is and the more reliable the system will be. In addition, the ERs for devices tend to decrease and then increase with the distance. ER has a minimum value, and the farther the deviation distance is, the greater the ER will be. Furthermore, the OPs decrease and ERs increase with the transmit power P_s when have a fixed distance.

Fig. 11 depicts the EE versus the transmit SNR under NOMA and OMA scenarios. We set $P_{STAR-RIS} = P_s = 5$ dB, $P_c = 0.1$ dB and $P_p = 10$ dB. It can be clearly observed that EE increases with the transmit SNR, and the system performance is better in NOMA scenario, which is due to the fact that NOMA allows multiple users to communicate simultaneously. In addition, EE increases as the number of elements in STAR-RIS. This indicates that the increase of the elements number in STAR-RIS has a positive impact on the system performance.

VI. CONCLUSION

This paper presented a novel simultaneously transmitting and reflecting reconfigurable intelligent surface (STAR-RIS)

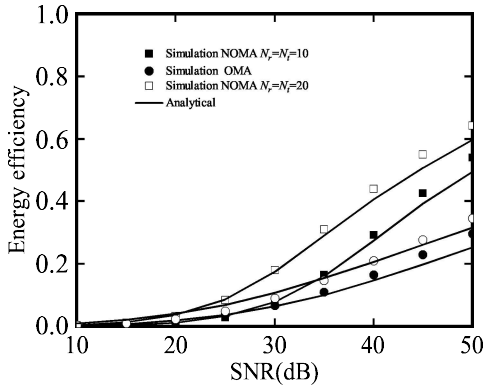


Fig. 11: The EE versus the transmit SNR

assisted overlay cognitive radio (CR)-non-orthogonal multiple access (NOMA) network based consumer Internet of Things (IoT) network in resilient industry 5.0. The performance of the network were explored by calculating the outage probabilities (OPs), ERs and energy efficiency (EE). Furthermore, the asymptotic expressions of OPs and ERs at high signal-to-noise ratio (SNR) regions were analyzed. On this basis, we investigated the diversity orders of devices. The correctness of our analysis results was confirmed by a number of simulation experiments. In addition, the influence of the number of STAR-RIS components, power allocation coefficient and the distance between STAR-RIS and devices on the system performance were discussed by simulation.

In addition, the performance can be further improved by optimize the number of STAR-RIS components, power allocation coefficient and the location of STAR-RIS. To make the scenario more practical, the impact of imperfect channel estimation information (CSI) and imperfect successive interference cancellation (SIC) on the system is also worthy of future research.

APPENDIX A

By bringing (5), (6) into (16), the OP can be expressed as

$$\begin{aligned} P_{out}^{PU} &= 1 - \Pr(\gamma_{ss}^{x_p} > \gamma_{th}^{x_p}, \gamma_{pu} > \gamma_{th}^{x_p}) \\ &= 1 - \int_A^\infty f_{|h_{ps}|^2}(y) dy \int_B^\infty f_Y(x) dx, \quad (\text{A.1}) \\ &= 1 - \theta_0 \left(\frac{1}{\theta_p}\right)^{-K_p} \frac{1}{\Gamma(K_p)\theta_p^{K_p}} \Gamma\left(K_p, \frac{\sqrt{\theta_1}}{\theta_p}\right) \end{aligned}$$

$$\text{where } A = \frac{\gamma_{th}^{x_p} N_0}{d_{ss}^{a_{ss}} P_p} \text{ and } B = \frac{\gamma_{th}^{x_p} N_0}{d_{sr}^{-\alpha_{sr}} d_{rp}^{-\alpha_{rp}} P_s \left(a_1 - \gamma_{th}^{x_p} a_2 \sum_{i=1}^M b_i\right)}.$$

The PDF of the channel $|h_{ss}|^2$ can be represented as

$$f_{|h_{ss}|^2}(x) = \left(\frac{m_{ss}}{\Omega_{ss}}\right)^{m_{ss}} \frac{x^{m_{ss}-1}}{\Gamma(m_{ss})} e^{-\left(\frac{m_{ss}}{\Omega_{ss}}\right)x}, \quad (\text{A.2})$$

where m_{ss} and Ω_{ss} refer to the Nakagami- m fading severity parameter and the average power, respectively.

Bring (A.2) into (A.1) to obtain Eq. (17).

APPENDIX B

The CDF of the channel h_{sn} is given by

$$F_{|h_{sn}|}(x) = 1 - \frac{\Gamma(m_{sn}, x)}{\Gamma(m_{sn})}. \quad (\text{B.1})$$

Assuming $Z = (|h_{sn}| + S)^2$, the expression of the PDF for Z can be expressed as

$$F_Z(z) = \int_0^{\sqrt{z}} f_s(x) F_{|h_{sn}|}(\sqrt{z} - x) dx. \quad (\text{B.2})$$

According to (15), (B.1) and (B.2), the result of (23) can be obtained.

APPENDIX C

The expression of ER for PU can be represented as

$$R_{PU} = E[\log_2(1 + \gamma_{pu})] = \log_2(1 + E(\gamma_{pu})), \quad (\text{C.1})$$

According the $E\left[\log_2\left(1 + \frac{x}{y}\right)\right] = \log_2\left[1 + \frac{E(x)}{E(y)}\right]$, the expectation of the SINR γ_{pu} can be written as

$$E(\gamma_{pu}) = \frac{E(|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rp}|^2) d_{sr}^{-\alpha_{sr}} d_{rp}^{-\alpha_{rp}} a_1 P_s}{E(|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rp}|^2) d_{sr}^{-\alpha_{sr}} d_{rp}^{-\alpha_{rp}} a_2 \sum_{i=1}^M b_i P_s + N_0}. \quad (\text{C.2})$$

Therefore, we only need to calculate the $E(|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rp}|^2)$.

$$E(|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rp}|^2) = E(|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rp}|)^2 + D(|\mathbf{h}_{sr} \Phi_T \mathbf{h}_{rp}|), \quad (\text{C.3})$$

$$\begin{aligned} \mu_{pu} &= E[|h_{sr}| |h_{rpu}|] \\ &= \left(\frac{1}{m_{sr} m_{rpu}}\right)^{\frac{1}{2}} \frac{\Gamma(m_{sr} + \frac{1}{2}) \Gamma(m_{rpu} + \frac{1}{2})}{\Gamma(m_{sr}) \Gamma(m_{rpu})}, \quad (\text{C.4}) \end{aligned}$$

$$D(x) = N(1 - \mu_{pu}^2). \quad (\text{C.5})$$

Therefore, bringing (C.4) and (C.5) into (C.3) yields Eq. (26).

The calculation method of the SU_m is similar to PU, so we omitted the calculation.

APPENDIX D

The expression of ER for SU_n can be represented as

$$R_n = E[\log_2(1 + \gamma_{su_n})] = \log_2(1 + E(\gamma_{su_n})). \quad (\text{D.1})$$

As mentioned above, we directly calculate $E(\gamma_{su_n})$ as

$$E(\gamma_{su_n}) = \frac{E(|h_{sn} + \mathbf{h}_{sr} \Phi_R \mathbf{h}_{rn}|^2) d_{sn}^{-2a_{sn}} a_2 b_n P_s}{E(|h_{sn} + \mathbf{h}_{sr} \Phi_R \mathbf{h}_{rn}|^2) d_{sn}^{-2a_{sn}} P_s \Delta_4 + N_0}. \quad (\text{D.2})$$

We set $Z = (S + h_{sn})^2$, it is approximated by the gamma distribution $Z \sim \Gamma(K_Z, \theta_Z)$.

The expectation of the Z can be represented as $E(Z) = K_Z \theta_Z$.

Bring the obtained $E(Z)$ to (D.2) to obtain Eq.(34).

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