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Two-dimensional numerical simulation of water entry of a cylinder into waves using OpenFOAM

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Abstract

During being hoisted into the waves, payloads are subjected to violent hydrodynamic impact, which brings a great challenge for deep-sea cranes' control systems. A two-dimensional numerical model with a motion constraint is established using OpenFOAM software to investigate the water entry of a cylinder into waves with the cavity effect. The accuracy of the numerical model is first verified by the water entry of a cylinder into the calm water. The mesh convergence analysis indicates that the jet profile is highly dependent on the mesh close to the cylinder surface. For the simulation of hoisting the payload into waves, a constraint for the 6 DOF rigid body motion solver

1 23 is introduced, which can simulate the cylinder lowering in the air with a constant velocity and then
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3 24 falling freely into the wave. With the proposed model in this paper, the water entry of a cylinder into
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6 25 waves is analyzed by dividing the entry process into four stages. Various case studies are carried out
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8
9 26 to investigate the physical effects of the entry position (crest, trough, upward point, and downward
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12 27 point), and the entry velocity on the hydrodynamic forces, pressure distribution, and free surface
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14
15 28 profile. Numerical results indicate that the wave particle velocity and wave slope are the essential
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18 29 factors for the asymmetry of pressure on the cylinder. The results also show that the cavity that
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21 30 forms above the cylinder top surface causes a sharp fluctuation of the hydrodynamics force on the
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24 31 cylinder and the cavity volume is positively related to the effective entry velocity. All of the
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27 32 numerical simulation results provide the fundamentals for further research and safe control of
28
29
30 33 offshore lifting or lowering.

31 34
32
33
34 35 Keywords: Water entry; Cylinder entering waves; Cavity effect; Computational fluid dynamics;
35
36 36 OpenFOAM

37 **1. Introduction**

38 Hoisting a payload into waves by a deep-sea crane is a very complicated problem, where
39 extremely violent hydrodynamic impact forces can severely damage the payload and the cable, thus
40 threatening the safety of the crew and equipment. Furthermore, the complex and varying
41 hydrodynamic forces also bring great challenges to the design of the crane control system, especially
42 when the wave environment causes more non-linear characteristics. Therefore, exploring the
43 features of the wave entry process of the payload is fundamentally important to the operation and
44 controller design of deep-sea cranes.

1 45 The study of water entry has received considerable attention for many years. Based on the law
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3
4 46 of conservation of momentum, Von Karman (1929) proposed a method to roughly estimate the
5
6 47 impact force on the seaplane during landing on calm water, which is considered as a pioneering
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9 48 work on the water entry problem. Further, Wagner (1932) proposed an analytical solution for the
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11
12 49 water entry by considering the uprise of water along the side of the wedge. Von Karman and Wagner
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15 50 laid the theoretical foundation for the study of water entry. Based on the Wagner theory with
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18 51 matched asymptotic expansions, some researchers investigated the water entry of a wedge with
19
20
21 52 small deadrise angles (Howison et al., 1991) and a wedge with elastic deformations (Korobkin et
22
23
24 53 al., 2006). Dobrovolskaya (1969) proposed similar solutions for the water entry of wedges with a
25
26
27 54 constant velocity by improving the Wagner theoretical solution. Zhao and Faltinsen (1993) used the
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29
30 55 boundary element method (BEM) to study the water entry of wedges with different deadrise angles
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32
33 56 and extended it to a general asymmetric wedge. Semenov and Iafrati (2006) studied the vertical
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36 57 entry of an asymmetric wedge and Xu et al. (2008) solved the problem of the oblique water entry
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39 58 of an asymmetrical wedge. By introducing the auxiliary function to decouple the mutual dependence
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42 59 of the body motion and the fluid flow, Wu et al. (2004) obtained the solution for the water entry of
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45 60 a wedge in free-fall motions. Wang et al. (2015) conducted experiments to investigate the water
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48 61 entry of a freefall wedge with an air cavity. Xu et al. (2010) and Bao et al. (2017) studied the water
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51 62 entry of a wedge in three degrees of freedom, considering the rotational motions of the wedge.
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54 63 However, the potential flow theory has a limitation in treating strongly nonlinear problems (Lin et
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56
57 64 al., 2021).

58 65 For such complex problems, Computational Fluid Dynamics (CFD) methods can capture
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61 66 highly nonlinear free-surface effects for the water entry problem, such as the wave breaking induced

1 67 by slamming (Chen et al., 2019). Based on the weakly compressible SPH solver (Bouscasse et al.,
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3 68 2013), Sun et al. (2018) applied the adaptive particle refinement (APR) technology in the SPH
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6 69 method to improve the accuracy of free surface solutions. Chen et al. (2020) calculated the water
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9 70 entry impact force on the autonomous underwater helicopter by the CFD analysis software STAR-
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12 71 CCM+. Ma et al. (2018) and Chen et al. (2019) investigated the water entry problem using the open-
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15 72 source CFD package OpenFOAM which uses the VOF method to capture the free surface, and the
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18 73 OpenFOAM has also been used for the water entry problems in the study of Xiang and Guedes
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20 74 Soares (2020) and Xiang et al. (2020).

21
22 75 Most of the above studies mainly focused on the water entry of a wedge, however, the water
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25 76 entry of a cylinder is often considered more challenging and more practical compared with wedges
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28 77 in ocean engineering. Cointe and Armand (1987) investigated the water entry of a cylinder by the
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31 78 Wagner theory. With the CFD analysis software, such as ANSYS Fluent and OpenFOAM, the
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34 79 impact forces and the motion of a cylinder during the water entry were solved (Jiang et al., 2016;
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37 80 Xiang and Guedes Soares, 2020; Xiang et al., 2020). However, some CFD software cannot handle
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40 81 some cylinder entry problems well, since the deadrise angle of the cylinder is very small at the initial
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43 82 stage which can cause singularity, rapidly increasing wetted surface, and large pressure peaks
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46 83 (Larsen, 2013). By comparing the free jet separated from the cylinder surface with three different
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49 84 CFD software packages, Derakhshanian et al. (2018) found that the ABAQUS software is the most
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52 85 capable software for solving the separation point of the jet flow and the results simulated by the
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55 86 other two CFD software are not consistent with the physical experiment conducted by Greenhow
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58 87 and Lin (1983). To calculate the jet distribution in agreement with the experimental observation,
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60
61 88 Sun et al. (2018) optimized the fluid-body interface by applying the particle shifting technique (PST)

1 89 modification in the SPH method.

2
3 90 The above literature is limited to the water entry into the calm water without taking into account
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6 91 the incident wave which can bring more nonlinear features for the water entry process. Because of
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9 92 the horizontal velocity of the wave, the body equivalently impacts the water obliquely even the entry
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12 93 velocity is vertical. Sun et al. (2015) investigated the water entry of a two-dimensional symmetric
13
14 94 wedge with the constant velocity into a wave using the boundary element method (BEM). They
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16
17 95 found that the effect of gravity on the pressure coefficient distribution and free surface profile
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20 96 becomes more pronounced as the entry time increases. Wang et al. (2021) simulated the whole
21
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23 97 process of asymmetric wedge entry into waves and analyzed the pressure distribution and
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26 98 hydrodynamic forces using the OpenFOAM. Cheng et al. (2018) developed a time-domain higher-
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29 99 order boundary element method (HOBEM) to investigate the wedge entry into waves with the wave-
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31
32 100 current effect, and Cheng et al. (2019) obtained the solution of the wave entry of a wedge in three
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34 101 degrees of freedom. Chen et al. (2022) studied the wave effect on the water entry of a 3D full-scale
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37 102 symmetric wedge by classifying the process into early, vertical-down, and bounce-up stages. Some
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39
40 103 satisfactory solutions for the water entry of a semi-circular with the cavity effects were also obtained
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42
43 104 based on the potential flow theory (Cheng et al., 2021; Sun et al., 2019). However, the study of the
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46 105 wave entry of a cylinder using the CFD analysis is very rare, and more understanding of the
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49 106 hydrodynamic characteristics of wave entry is essential for the better design of offshore cranes.

50 107 In this paper, the entire water entry process of a cylinder into waves with gravity is numerically
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53 108 simulated using the OpenFOAM. We discuss the comprehensive mechanisms of wave effect on the
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56 109 hydrodynamic force of the cylinder with the pressure distribution and free surface profile. The effect
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59 110 of entry position and entry velocity on the hydrodynamic force of the cylinder is analyzed. The

1 111 contributions of the paper are as follows: (1) A detailed analysis of the convergence of the sub-mesh
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3 112 is presented to find the appropriate mesh distribution for the accuracy of the jet profile during water
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6 113 entry. (2) According to the acceleration curve, the entire process of wave entry can be classified into
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9 114 four stages, i.e. the impacting stage, jet formation stage, cavity closure stage, and sinking stage. The
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11 115 effects of entry position and entry velocity on the pressure distribution, free surface profile, and
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14 116 hydrodynamic force during these four stages are discussed. (3) The formation and development of
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16
17 117 the jet and cavity are elaborated, and the mechanisms of cavity effects on the hydrodynamic force
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20 118 are analyzed with pressure and free surface distribution.

21
22 119 The remainder of the paper is organized as follows. Section 2 describes the numerical model
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24
25 120 and the underlying numerical solution methodology. In Section 3, the test case of water entry of a
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28 121 cylinder into the calm water is first conducted to verify the presented numerical model, and a
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31 122 convergence study is performed. In Section 4, the wave effects on the water entry of the cylinder
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34 123 are analyzed, and the detailed results of the effects of entry position and entry velocity on the
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37 124 cylinder entering waves are provided. Finally, conclusions are drawn in Section 5.

125 2. Mathematical formulation

126 2.1 Governing equation

127 The water entry problem is solved by an *overInterDyMFoam* solver in the OpenFOAM, which
128 combines the incompressible two-phase pressure-based solver *interFoam* and the dynamic overset
129 technology. The governing equations in the two-dimensional incompressible, isothermal, and
130 immiscible fluid domain are the mass conservation and momentum conservation equations, which
131 are given as follows:

$$132 \quad \nabla \cdot \mathbf{u} = 0 \quad (1)$$

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$$\frac{\partial \rho \mathbf{u}}{\partial t} + \nabla \cdot (\rho \mathbf{u} \mathbf{u}) = \nabla \cdot (\mu \nabla \mathbf{u}) - (\mathbf{g} \cdot \mathbf{x}) \nabla \rho - \nabla p_d \quad (2)$$

133 where \mathbf{u} is the velocity vector, ρ the density of the fluid, t the time, μ the dynamic viscosity
134 of the fluid, \mathbf{g} and \mathbf{x} the gravitational acceleration and the position vector respectively. p_d is
135 the dynamic pressure, which is given by:
136

$$p_d = p - \rho \mathbf{g} \cdot \mathbf{x} \quad (3)$$

137 where p is the total pressure.

139 2.2 Free surface capturing method

140 The volume of fluid (VOF) method is applied in this model to capture the free surface. In the
141 VOF method, the volume fraction $\alpha \in [0,1]$ represents the water component per unit volume at
142 each cell which is solved by a transport equation:

$$\frac{\partial \alpha}{\partial t} + \nabla \cdot \mathbf{u} \alpha + \nabla \cdot \mathbf{u}_c \alpha (1 - \alpha) = 0 \quad (4)$$

143 where $\nabla \cdot \mathbf{u}_c \alpha (1 - \alpha)$ is introduced to limit the numerical diffusion and \mathbf{u}_c is referred to as the
144 compressive velocity field (Chen et al., 2014). The free surface can be identified by tracking the
145 computational cells whose volume fraction α is between 0 and 1. The above equations are
146 integrated over each computational cell to solve α and \mathbf{u} , and the dynamic pressure p_d is
147 obtained by solving the pressure corrector linearized equation (Ma et al., 2018).
148

149 2.3 Solution algorithm

150 The solution procedure relies on the PIMPLE algorithm which essentially combines the
151 Pressure-Implicit with Splitting of Operators (PISO) and Semi-Implicit Method for Pressure Linked
152 Equations (SIMPLE). The flow chart of the solution algorithm (Chen et al., 2019) is shown in Fig.
153 1. Within each PIMPLE loop, the six DOF motion equation is solved first, with the update of the
154 dynamic mesh. Then the free surface is captured by solving the transport equation for the volume

155 fraction field α . The pressure Poisson equation is solved iteratively by the PISO algorithm to deal
 156 with the velocity-pressure coupling. Finally, the turbulence modeling equations are solved in the
 157 last step. More details of the solution process can be found in Ferro et al. (2022).
 158

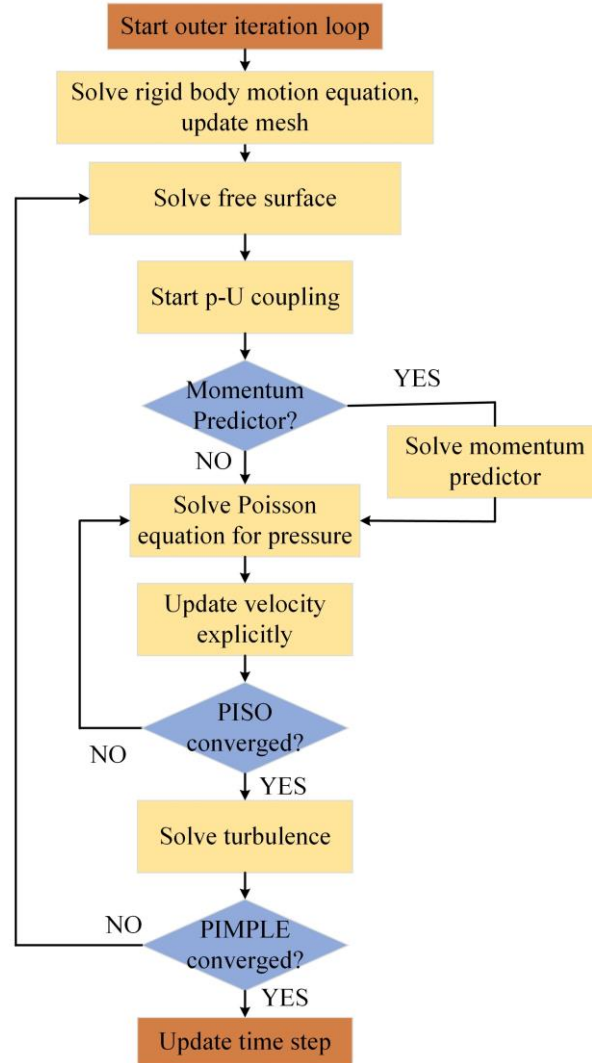


Fig. 1 The flow chart of the solution algorithm.

162 This work uses built-in numerical schemes in OpenFOAM to numerically approximate the
 163 PDE terms in the governing equations and the transport equation for the water volume fraction.
 164 **Table 1** shows the discretization schemes in the simulations.

165

166 **Table 1** The discretization of PDE terms.

	Term	Discretization
Spatial domain Temporal Scheme	ddtSchemes (d/dt)	Finite Volume Method (FVM) Euler, First order implicit, Bounded.
Gradient Schemes	default	Gauss linear, Second order, Unbounded
	($\nabla \mathbf{u}, \nabla \alpha$)	Gauss linear, Second order, Unbounded
Divergence Schemes	$\nabla \cdot (\rho \phi \mathbf{u})$	Gauss limitedLinearV 1, Second order, Bounded
	$\nabla \cdot (\phi \alpha)$	Gauss vanLeer, Second order, Unbounded
Laplacian Schemes	∇^2	Gauss linear corrected, Second order, Unbounded
Interpolation Schemes	default	Linear, Second order
Surface normal gradient Schemes	default	Corrected, Second order

167

168 **2.4 Six DOF motion solver**

169 The motion of the free-falling cylinder for the wave entry problem is solved by using the

170 *sixDoFRigidBodyMotion* solver in the OpenFOAM. The cylinder motion is calculated according to171 the resultant force \mathbf{F} and moment \mathbf{M} , which are induced by the pressure and shear stress on the172 cylinder surface, and the gravity force. The accelerations of the translation \mathbf{a} and rotation $\boldsymbol{\psi}$ for

173 the cylinder motion are obtained from the motion equation which is based on the linear and angular

174 momentum conservations. The motion equations are given by:

175
$$\mathbf{a} = \mathbf{F} / m \quad (5)$$

176
$$\boldsymbol{\psi} = \mathbf{I}^{-1} \cdot \mathbf{M} \quad (6)$$

177 where m is the mass of the cylinder and \mathbf{I} denotes the moment of inertia.

178 The body position and rotation solving process are essentially the same, so the position is
 179 presented as an instance to illustrate the solution process of the *sixDoFRigidBodyMotion* solver. The
 180 acceleration relaxation coefficient χ is used to improve the stability of the motion solver:

$$181 \quad \mathbf{a}_n = \chi \mathbf{a} + (1 - \chi) \mathbf{a}_o \quad (7)$$

182 where \mathbf{a} are obtained from Eq. (5). The subscripts of n and o indicate the acceleration at the new
 183 and old time steps, respectively. According to the linear acceleration \mathbf{a}_n , the current linear velocity
 184 and position can be updated using the Newmark integration scheme strategy, which is expressed as:

$$185 \quad \mathbf{v}_n^{k+1} = \mathbf{v}_o + \Delta t (\gamma \mathbf{a}_n^k + (1 - \gamma) \mathbf{a}_o) \quad (8)$$

$$186 \quad \mathbf{l}_n^{k+1} = \mathbf{l}_o + (\mathbf{u}_o \Delta t + \gamma (\Delta t)^2 (\beta \mathbf{a}_n^k + (0.5 - \beta) \mathbf{a}_o)) \quad (9)$$

187 where \mathbf{v} is the velocity of the cylinder, and \mathbf{l} is the position of the center of rotation. The
 188 coefficients β and γ are typically set to 0.5 and 0.2, which yields the so-called constant average
 189 acceleration method. The superscript k represents the sub-iteration step for the implicit sub-
 190 iterations in time (Chen et al., 2019).

191 At the wave generation stage, the motion solver for updating the linear and rotational
 192 displacements is restrained. After several periods of waves that fully develop, the constraint allows
 193 the cylinder to fall in the air with a constant velocity by limiting the update of the motion velocity.
 194 When the cylinder touches the wave surface, the constraint is removed so that the cylinder enters
 195 the wave with a free-falling motion.

196 2.5 Computational domain setup

197 To describe the wave entry problem, two Cartesian coordinate systems are defined in the
 198 computation domain: a global coordinate system $OXYZ$ fixed on the numerical tank bottom and
 199 a body-fixed coordinate system $oxyz$ on the body. As shown in Fig. 2, the X axis is along the

1 200 wave propagation direction, with the Z axis pointing upwards. The body-fixed coordinate system
2
3 201 xyz is placed at the mass center of the cylinder and moves with the cylinder. Fig. 2 shows that
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6 202 the rectangular computational domain for the wave entry is divided into two parts which are the
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9 203 wave generation zone and the impact zone. The 5th order Stokes wave is generated in the
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12 204 computational domain by a wavemaker placed on the left side. The active absorption method
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15 205 (Schäffer Hemming and Klopman, 2000) is applied to avoid wave reflection from the outlet
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17
18 206 boundary.

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20 207 As shown in Fig. 2, the numerical tank defines 6 boundaries named **Inlet**, **Outlet**, **Front and**
21
22 208 **Back**, **Bottom**, **Atmosphere**, and **Cylinder**, respectively. Each boundary requires a set of boundary
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25 209 conditions to define boundary variables including the velocity, pressure, and phase fraction. The
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28 210 boundary conditions used in this work are given in Table 2, which are standard OpenFOAM
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30
31 211 boundary conditions. Due to two-dimensional simulation, the **Front and Back** boundary of the
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34 212 numerical tank is defined as *empty*. The boundary conditions, *waveVelocity* and *waveAlpha*, are
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36
37 213 employed for the velocity and phase fraction in the **Inlet** boundary to specify the wave values from
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40 214 wave models. The *pressureInletOutletVelocity* is used for the **Atmosphere** boundary that is free to
41
42
43 215 the atmosphere. This boundary is a blend of *pressureInletVelocity* and *inletOutlet* boundary
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45
46 216 conditions, which apply a *zero-gradient* condition for the outflow and switch to *fixedValue* to the
47
48
49 217 reverse flow. The velocity boundary of the **Cylinder** is *movingWallVelocity* which corrects the flux
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51
52 218 for moving boundaries to ensure that the normal velocity flux across the boundary surface is zero.
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55 219 The *fixedFluxPressure* condition sets the pressure to ensure that the flux matches the velocity
56
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58 220 boundary condition, and the *totalPressure* condition is used to set the pressure to zero on the
59
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61 221 atmosphere boundary (Aliyar et al., 2022).

1 222

2
3 223 Table 2 Boundary conditions in the numerical tank.

Boundary	Velocity	Pressure	Phase fraction
Inlet	<i>waveVelocity</i>	<i>fixedFluxPressure</i>	<i>waveAlpha</i>
Outlet	<i>waveVelocity</i>	<i>fixedFluxPressure</i>	<i>zeroGradient</i>
Atmosphere	<i>pressureInletOutletVelocity</i>	<i>totalPressure</i>	<i>inletOutlet</i>
Bottom	<i>fixedValue</i>	<i>fixedFluxPressure</i>	<i>zeroGradient</i>
Cylinder	<i>movingWallVelocity</i>	<i>fixedFluxPressure</i>	<i>zeroGradient</i>
Front and Back	<i>empty</i>	<i>empty</i>	<i>empty</i>

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17 224

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19
20 225 The overset mesh model consists of the background mesh and the body-fitted component mesh
21
22
23 226 to handle the large-amplitude motions of the moving objects. The background mesh is mainly used
24
25 227 to calculate the fluid value of the water entry environment including the wave elevation, water
26
27
28 228 particle velocity, pressure, etc. As shown in the overview of the computational mesh in Fig. 2(b),
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31 229 the background mesh is refined at the free surface area in the vertical direction for generating the
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34 230 wave accurately. Furthermore, small mesh elements are also used in the impact region ensuring a
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37 231 good resolution for the violent flow. To save computational resources, the coarse mesh is used in
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40 232 the areas with smooth value variations, such as the bottom and left areas of the computational
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42 233 domain.

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45 234 The cylinder is modelled in the sub-mesh, which is generated on top of the background mesh.
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48 235 Fluid values are exchanged between different meshes using interpolation in the fringe region of the
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51 236 sub-mesh (Chen et al., 2019). The sub-mesh is an essential part to capture the slamming pressures
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53 237 and the jet surface accurately.

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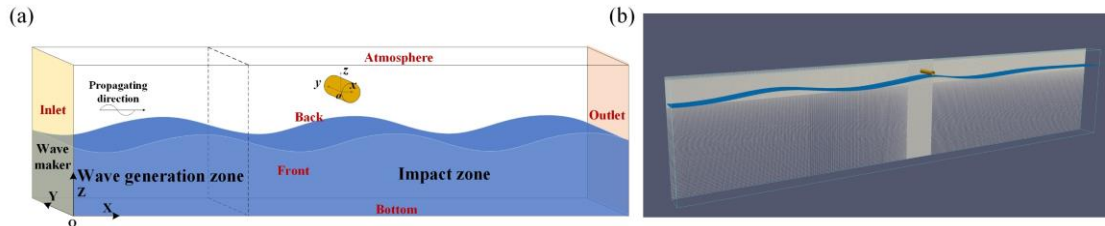


Fig. 2 Numerical setup of wave entry of a cylinder: (a) sketch of the cylinder entering waves; (b) snapshot of the background mesh in the OpenFOAM.

3. Model validation and convergence study

The experimental investigation of a cylinder free-falling into the calm water conducted by Greenhow and Lin (1983) is reproduced numerically to verify the presented model. In the experiment, two cylinders with a radius of 0.055 m are dropped into the calm water from a height of 0.5 m above the free surface. The masses of the two cylinders are 9.4985 kg and 4.737 kg corresponding to the neutral buoyancy and half of the neutral buoyancy respectively. In the numerical simulation, the cylinder is held still at the free surface and then it freely falls into the calm water with an initial velocity of $v = 2.938$ m/s.

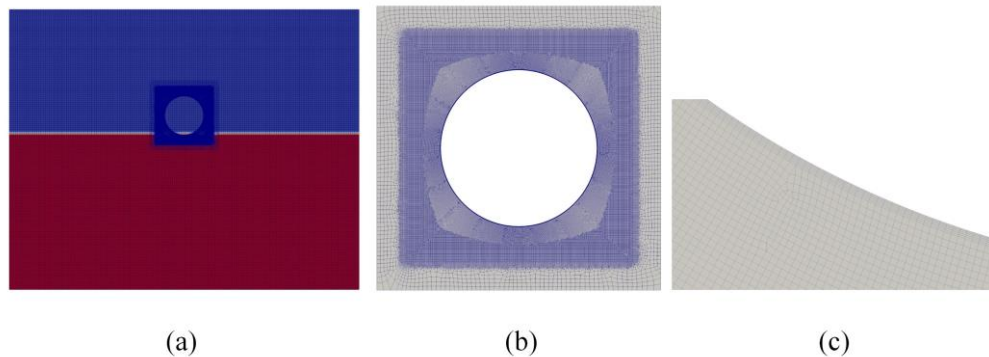


Fig. 3 Overset mesh for the cylinder entering the calm water: (a) overview of the computational domain; (b) sub-mesh modelling the cylinder; (c) close-up view of the sub-mesh near the cylinder

surface.

256

257 The numerical results of water entry problems are affected by the mesh quality near the body

258 surface, which means that the sub-mesh resolution plays a dominant role in the water entry results.

259 Therefore, in the convergence analysis, the influence of the sub-mesh on the pressure and free

260 surface is mainly considered. The rectangular computational domain in Fig. 3(a) for the water entry

261 problem is set to $1 \times 1 \times 0.8$ m with a water depth of 0.5 m. The background mesh is discretized

262 with the uniform regular hexahedral cells where the mesh resolution is $\Delta x = \Delta z = 0.006$ m. As shown

263 by the generated sub-mesh around the cylinder in Fig. 3(b), the mesh resolution in the fringe of the

264 sub-mesh is the same as the background mesh, which ensures the accuracy of the interpolation. For

265 solving the slamming pressure and the free surface profile accurately, the inner area is refined using

266 an adequate number of elements and well-organized grids.

267 At the early stage of the water entry, the small deadrise angle and the rapidly increasing wetted

268 surface cause some challenging problems including the inaccurate impact pressure, the oscillating

269 slamming force, and especially the incorrect jet profile. Thus, referring to the work in Larsen (2013),

270 the mesh layer close to the cylinder surface with 1mm thickness is modelled with the prism layer

271 mesh which is shown in the close view of the sub-mesh in Fig. 3(c).

272 Most cases in this paper are computed using a workstation with the Intel Xeon (R) E5 2699v4

273 CPU, 128G RAM, and the cases for the convergence study are computed with 8 cores. **Table 3** lists

274 different parameters of the sub-mesh schemes including the resolution of the refinement area, the

275 number of prism layer, and the total cell number. The maximum Courant number is set to 0.5, and

276 the adaptive time step is adopted.

1 277

2
3 **Table 3** Sub-mesh parameters and computational cost for the cylinder freely falling into the calm

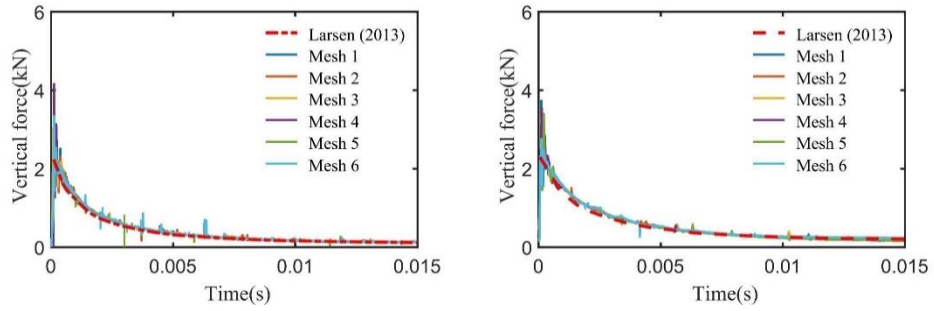
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6 279 water.

Mesh scheme	Refined cell size $\Delta x = \Delta z$	Prism layer mesh number	Cell number:	Run time (h): (half buoyancy/neutral buoyancy)
1	0.0008	5	293	4.1/6.8
2	0.0008	8	307	6.7/7.4
3	0.0005	5	683	13.2/11.9
4	0.0005	8	703	12/12.2
5	0.0004	5	104	26.8/25.3
6	0.0004	8	107	32.5/33.6

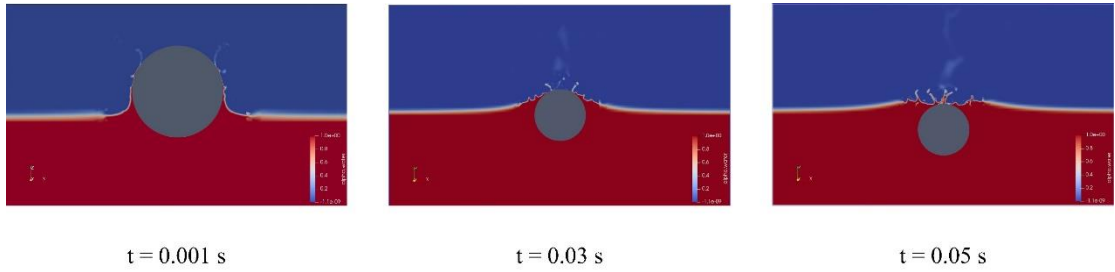
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24 281 The time history of the vertical force on the cylinder using different mesh schemes is shown in
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27 282 Fig. 4. It can be observed that the vertical force agrees well with the numerical result in Larsen
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30 283 (2013), which confirms the capability of the present model. Fig. 4 indicates that even the coarsest
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33 284 Mesh 1 can provide an accurate vertical force solution. The force fluctuations at the initial phase are
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36 285 caused by the pressure peak in the jet root region which is smaller than the mesh size (Larsen, 2013).
37
38
39 286 However, some mesh schemes do not model the splash correctly as shown in Fig. 5. It can be seen
40
41
42 287 that the jets obtained with Mesh 1 do not separate from the cylinder surface and the free surface
43
44
45 288 seems unreal. Therefore, the convergence study for the jet profile is also carried out to find a high-
46
47
48 289 quality mesh to ensure accurate solutions. For the sake of brevity, only the free surface of the neutral
49
50
51 290 buoyant cylinder is analyzed in detail.

52 291



292
293 Fig. 4 Comparison of the force-time curve using different mesh schemes: (a) half buoyancy; (b)
294 neutral buoyancy.



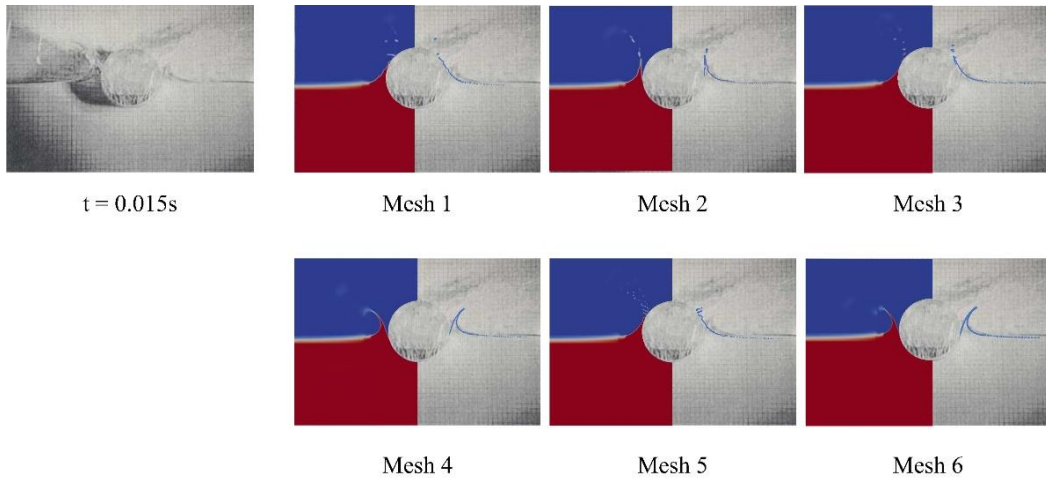
296
297 Fig. 5 Free surface of the cylinder free-falling into the calm water using Mesh 1.

298
299 Comparisons of the free surface profile at $t = 0.015$ s using six different mesh schemes with
300 the experiment data are shown in Fig. 6. For Mesh 1 and Mesh 5, the jet uprises along the cylinder
301 surface and appears the unphysical flow pattern which may be due to the fact that the prism layer
302 mesh is too coarse to separate the jet flow. Although the jet flow is separated from the cylinder
303 surface in Mesh 2 and Mesh 3, the separation point does not match the experiment result. The free
304 surface results using Mesh 4 and Mesh 6 are in the best agreement with the experimental results,
305 including the correct separation position and the jet profile. It can be concluded that the finer prism
306 layers mesh can obtain the correct separation position, and the outer quadrilateral grid determines
307 the correct shape of the free surface. Although the refined prism layers mesh can help with the jet
308 separation, if the prism layers mesh resolution is too small to mismatch the outer quadrilateral mesh

309 size, it may also cause incorrect free surface results.

310 It is worth noting that the incorrect jet does not significantly influence the results of the initial
311 slamming force on the cylinder, since the tip of the jet does not contribute much to the solution of
312 the pressure in the initial stage. As the penetration depth increases, the unseparated fluid above the
313 cylinder exerts pressure on the cylinder, resulting in the incorrect solution of the vertical force on
314 the cylinder.

315



316

317 Fig. 6 Comparison of the free surface between the experimental measurement (Greenhow and Lin,
318 1983) and the numerical simulations with different mesh schemes.

319

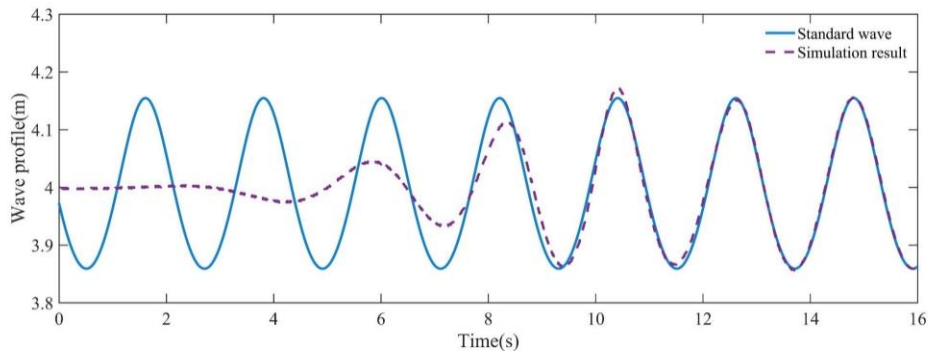
320 4. Water entry of a cylinder into waves

321 4.1 Effect of wave on water entry of a cylinder

322 This section mainly investigates the influence of the Stokes wave on the water entry of a free-
323 falling cylinder with an initial velocity. A sketch of the simulation setup and the meshing scheme of
324 the cylinder entering the wave is given in Fig. 2 where the length and width of the computational
325 domain are set to 24 m and 5 m. The 5th order Stokes wave with the wave height $H = 0.3$ m and

326 wave period $T = 2.2$ s is generated from the left side of the numerical wave tank with the water
327 depth $h = 4$ m. A cylinder of the radius 0.1 m impacts the wave crest with an initial velocity $v = 1$
328 m/s in the numerical simulation. The mass of the cylinder is set as 37.68 kg, corresponding that the
329 density of the cylinder is 1.2 times the fluid density.

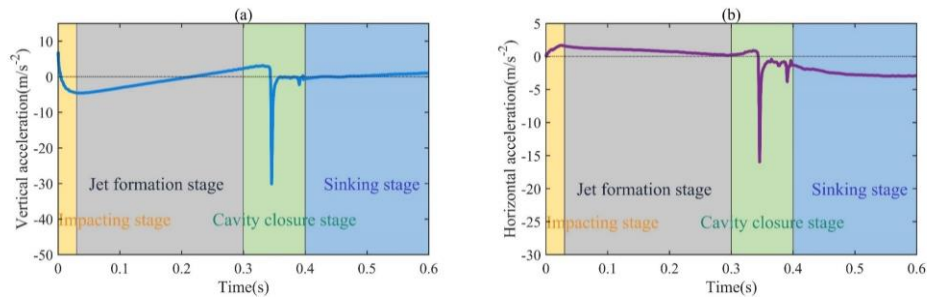
330 Prior to the simulations of wave entry, simulations without cylinder motion are performed to
331 verify the accuracy of wave making. Fig. 7 shows the time histories of the wave elevation below
332 the cylinder compared to the solution by Skjelbreia and Hendrickson (1961). A fairly good
333 agreement between the standard result and the simulation is obtained except for the initial three
334 wave cycles since the wave is generated in a numerical wave tank by the wave velocities with a
335 smooth time ramp.



337
338 Fig. 7 Comparison of wave elevation between the undisturbed simulated wave and standard wave
339 by Skjelbreia and Hendrickson (1961).

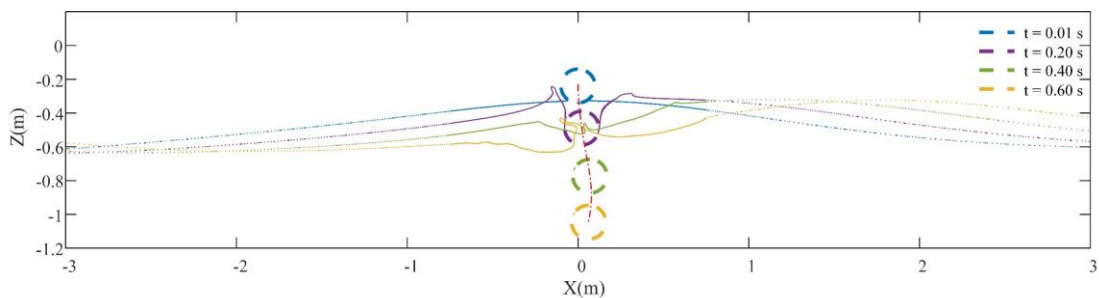
341 Since the force on the cylinder is proportional to the acceleration, the time history of the
342 cylinder acceleration is plotted during the entry time $t = 0-0.6$ s in Fig. 8. According to the
343 acceleration of the cylinder, the wave entry process can be divided into 4 distinctive stages:
344 impacting stage, jet formation stage, cavity closure stage, and sinking stage, which are also

345 distinguished by different colours in Fig. 8. The vertical force decreases in the impacting stage ($t =$
 346 $0-0.03$ s) and then increases in the jet formation stage ($t = 0.03-0.3$ s), while the horizontal force
 347 changes in the opposite manner. During the cavity closure stage ($t = 0.3-0.4$ s), the vertical and
 348 horizontal forces decrease sharply as the compressed cavity exerts violent pressure on the top
 349 surface of the cylinder. Finally, in the sinking stage ($t = 0.4-0.6$ s), the cylinder is fully submerged
 350 in the wave, and its vertical force gradually increases with the penetration depth.



352
 353 Fig. 8 Time history of acceleration of the cylinder falling into the wave crest: (a) vertical
 354 acceleration; (b) horizontal acceleration.

355 Fig. 9 shows the cylinder position in the global coordinate system and the red curve represents
 356 the entry trajectory of the cylinder centre. It can be seen that the cylinder moves to the right at the
 357 initial entry stage, and shifts leftward after the cavity closure stage, which corresponds to the change
 358 in the horizontal force.



361 Fig. 9 Position of the cylinder in the global coordinate system at different time instants.

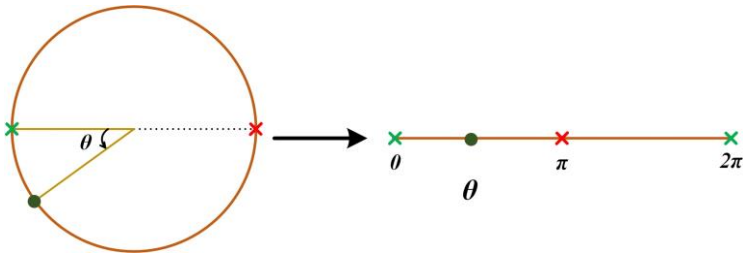
362
363 **4.1.1 Impacting stage**

364 When the cylinder touches the wave surface with the initial velocity, the cylinder is subjected
365 to a large hydrodynamic impact. Then, the vertical force on the cylinder rapidly decreases as the
366 penetration depth increase. This is different from the phenomenon of a continuous increase in the
367 vertical force during a wedge entering waves (Wang et al., 2021). The reason for this phenomenon
368 is the increase in the effective deadrise angle of the cylinder, which can be seen in detail by the free
369 surface distribution and pressure distribution. To clearly show the pressure distribution, an angle
370 $\theta \in [0, 2\pi)$ is defined in Fig. 10 to show the pressure distribution along the cylinder's circumference.
371 As shown in Fig. 11, the effective deadrise angle between the cylinder and the wave surface is zero
372 at the impact instant, resulting in high pressure on the cylindrical wetted surface. Since the effective
373 deadrise angle between the cylinder and the wave surface increases, the pressure and the vertical
374 force on the cylinder decrease rapidly.

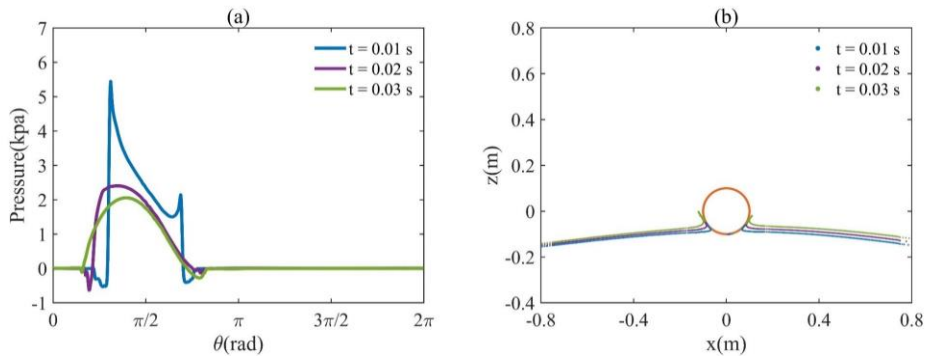
375 Fig. 11(a) illustrates the changing characteristics of the pressure distribution in the impacting
376 stage. During $t = 0.01-0.02$ s, the pressure on the cylinder is maximum at the jet-root region which
377 is similar to the pressure distribution for the wave entry of a wedge (Sun et al., 2015). As the cylinder
378 moves downward, the pressure peaks on the jet roots gradually shift to the centre of the cylinder's
379 bottom surface. It is also interesting that the pressure on the jet top is negative, which means that
380 the pressure is smaller than the atmospheric pressure. This feature may be due to the air being
381 trapped in that region. In addition, the pressure on the left side of the cylinder is larger than that on
382 the right side, resulting in a horizontal force pointing to the right. This is because the wave particles

383 at the crest have a horizontal velocity in the rightward direction, which is equivalent to a body
 384 entering the calm water with a horizontal velocity in the leftward direction. Therefore, the cylinder
 385 entering the wave at the crest can be treated as the oblique entry during $t = 0.01-0.02$ s.

386 In the impacting stage, Fig. 11(b) shows that the jet uprises along the cylinder surface, and
 387 most of the jet flow still clings to the cylinder surface. Because of the horizontal wave particle
 388 velocity, the jet on the left side of the cylinder is slightly higher than that on the right side.



390
391 Fig. 10 Definition of the angle $\theta \in [0, 2\pi)$ for plotting pressure distribution.



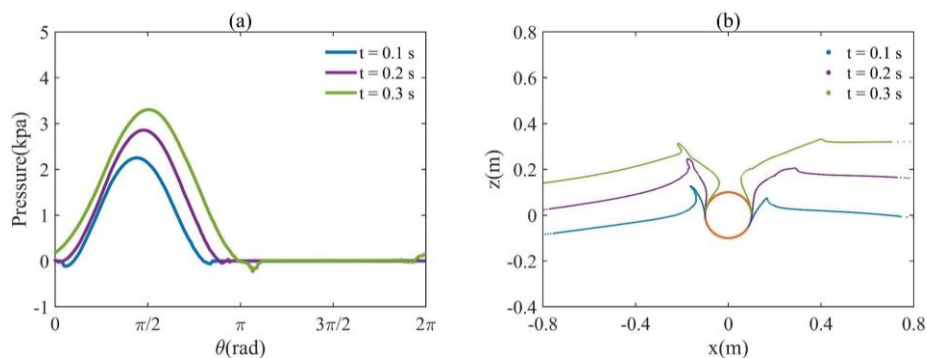
392
393
394 Fig. 11 Pressure and free surface results of a cylinder entering the wave crest in the impacting
 395 stage: (a) pressure distribution; (b) free surface profile.

397 4.1.2 Jet formation stage

398 As the cylinder moves downward, the vertical force on the cylinder gradually increases due to
 399 the increase of the entry velocity and the impact/wetted area. After $t = 0.213$ s, the vertical force is

400 greater than the gravity causing the vertical entry velocity of the cylinder to decrease. Because the
 401 horizontal velocity of the wave particle decreases as the depth increases. The horizontal force on
 402 the cylinder gradually decreases, which causes the horizontal velocity of the cylinder increases more
 403 and more slowly.

404 Fig. 12(a) shows the pressure distribution in the jet formation stage. As the horizontal velocity
 405 of the wave particle decreases as the depth increases, the pressure on the cylinder bottom surface
 406 becomes symmetric gradually, and the maximum pressure shifts toward the centre of the cylinder
 407 bottom. The negative pressure near the jet root regions also gradually disappears. In Fig. 12(b), the
 408 jet separates from the cylinder surface in the form of a splash. Because of the horizontal velocity of
 409 the wave particle, the jet on the left side is longer than that on the right side. The vertical velocity
 410 of the jet rapidly decreases and the jet eventually falls into the wave due to the effect of gravity. The
 411 jets pile up with the incident wave, and the left and right jet roots form the depart flow moving
 412 towards each other at $t = 0.3$ s. Then the depart flow moves inwards because of the gravity and the
 413 push effect of the incident wave, forming a cavity on the top side of the cylinder.



415
 416 Fig. 12 Pressure and free surface results of a cylinder entering the wave crest in the jet formation
 417 stage: (a) pressure distribution; (b) free surface profile.

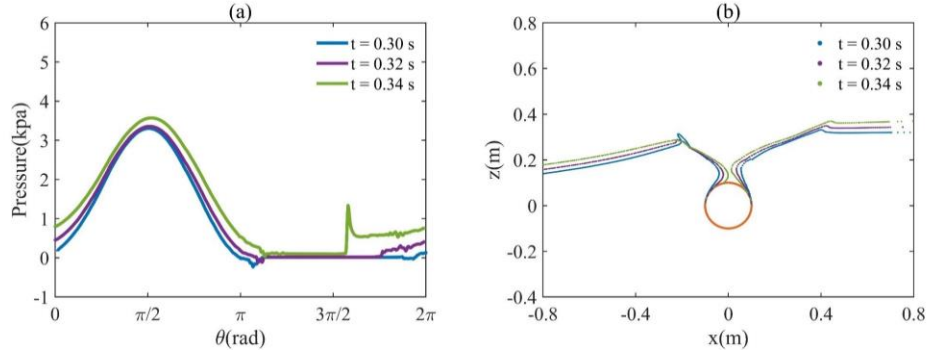
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419 4.1.3 Cavity closure stage

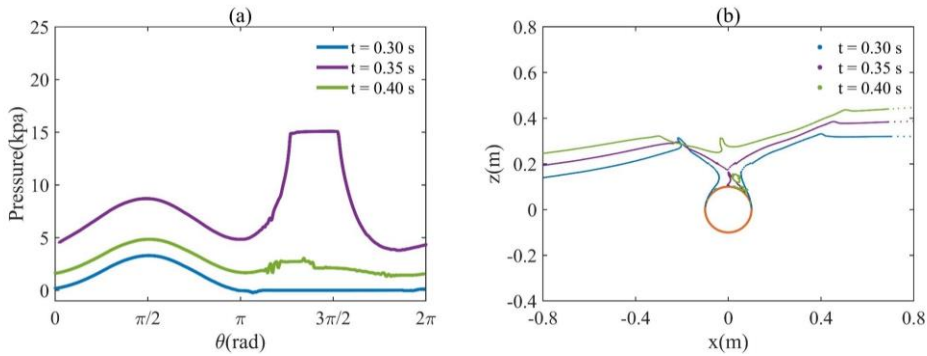
1
2
3 420 In Fig. 13, as the cylinder moves downwards, the inner surface of the jet flow moves inwards
4
5
6 421 due to the gravity and push effect of the wave. The left side and right side flows eventually impact
7
8
9 422 each other forming a cavity behind the cylinder. Because of the wave effect, the close position of
10
11 423 the cavity is not on the centerline of the cylinder. The left side inner flow touches the cylinder's top
12
13
14 424 surface earlier and exerts a downward and rightward hydrodynamic force on the cylinder before the
15
16
17 425 cavity closure, which is reflected by the larger pressure on the left side of the top surface at $t = 0.34$
18
19
20 426 s. Consequently, the horizontal force slightly increases before the cavity closes during $t = 0.3-0.34$
21
22
23 427 s shown in Fig. 8. At $t = 0.34$ s, sharp fluctuations in the vertical and horizontal forces are observed
24
25
26 428 in Fig. 8. This is because the air pocket is compressed by the collision of the left and right depart
27
28
29 429 flows, which results in a sudden increased pressure on the cylinder top surface. The cavity is mainly
30
31 430 gathered on the right side of the cylinder's top surface, thus the horizontal force sharply decreases,
32
33
34 431 which means the horizontal force suddenly points to the left.

35
36 432 The pressure and free surface distribution during the cavity close stage are illustrated in Fig.
37
38
39 433 14. At $t = 0.35$ s, the cavity is closed and compressed by the inward free surface. The pressure on
40
41
42 434 the cylinder top surface increases rapidly, which is even higher than the pressure on the cylinder
43
44
45 435 bottom surface. However, the large pressure on the bottom surface rapidly disappears because the
46
47
48 436 air pocket leaves the cylinder's top surface. Fig. 14(b) shows that the closing point of the air cavity
49
50
51 437 is on the right side of the cylinder. After the cavity is closed, an upward jet is subsequently formed
52
53
54 438 by the collision of the free surface.

55
56 439



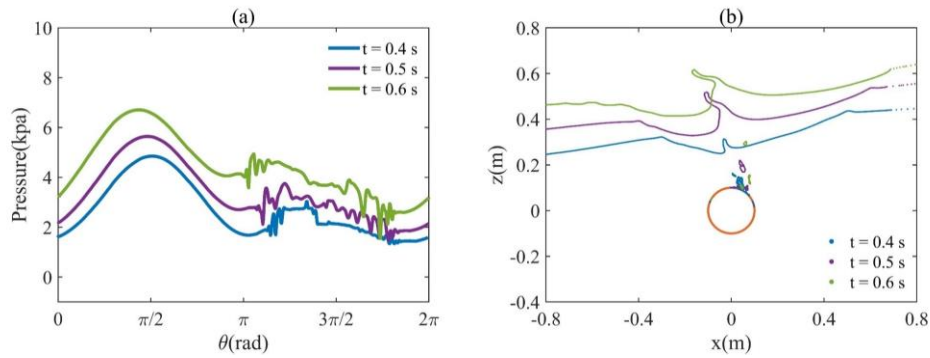
440
441 Fig. 13 Pressure distribution and free surface profile of a cylinder entering the Stokes wave before
442 the cavity close: (a) pressure distribution; (b) free surface profile.



444
445 Fig. 14 Pressure distribution and free surface profile of a cylinder entering the Stokes wave in the
446 cavity close stage: (a) pressure distribution; (b) free surface profile.

448 4.1.4 Sinking stage

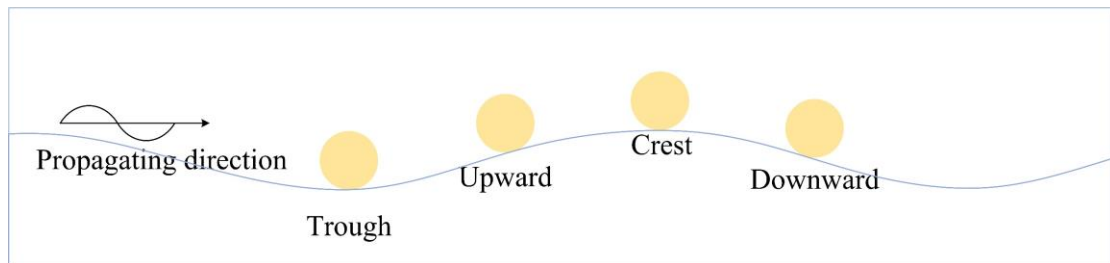
449 At the sinking stage, the vertical force on the cylinder gradually increases with the penetration
450 depth. Fig. 15(a) shows that the pressure on the right top of the cylinder surface is larger than that
451 on the right side. Consequently, the imbalanced pressure distribution leads to an increase in the
452 horizontal force to the left. Fig. 15(b) shows that the bubbles float upward to the free surface from
453 the cylinder surface. The uprise vertical jet bends to the right due to the gravity and the push effect
454 of the incident wave.



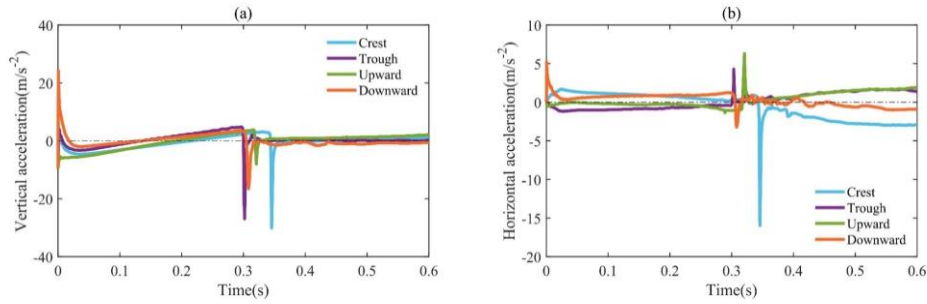
455
456
457 Fig. 15 Pressure distribution and free surface profile of a cylinder entering the Stokes wave in the
458 sinking stage: (a) pressure distribution; (b) free surface profile.

460 4.2 Effect of the entry position on the wave entry of a cylinder

461 To study the influence of the entry position, the water entry of the cylinder entering the wave
462 at different wave positions shown in Fig. 16, i.e., the crest, downward point, trough, and upward
463 point, is simulated. Other parameters are the same as in Section 4.1. Fig. 17 shows the comparison
464 of the vertical and horizontal accelerations of the cylinder entering the wave at different entry
465 positions. Moreover, the pressure distribution and free surface profile for different entry positions
466 are plotted in Fig. 18-Fig. 22.



467
468
469 Fig. 16 Water entry position in the Stokes waves.



471
472 Fig. 17 Acceleration of the cylinder entering the wave at different positions: (a) vertical
473 acceleration; (b) horizontal acceleration.
474

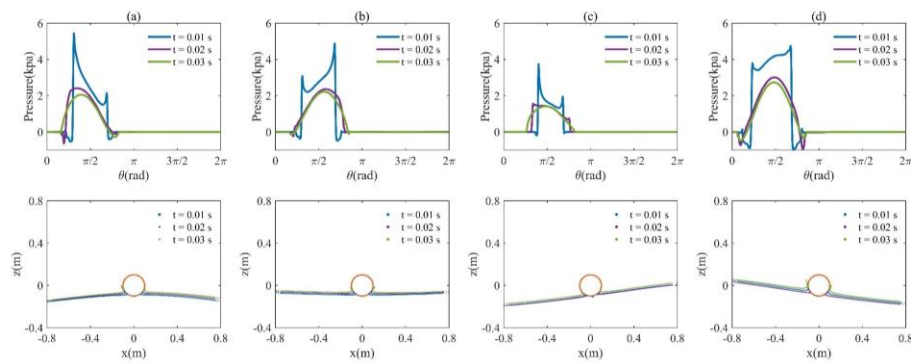
475 4.2.1 Effect of the entry position in the impacting stage

476 In the impacting stage, the vertical impact force is largest in the downward point entry and
477 smallest in the upward point entry as shown in Fig. 17(a). The reason for this phenomenon is mainly
478 contributed by the vertical velocity of the wave particle. The wave particle in the downward point
479 has a vertical-up velocity, which increases the effective velocity between the cylinder and the wave.
480 Correspondingly, the effective velocity decreases at the upward point. The wave particle velocities
481 at the upward point and downward point are -0.4 m/s and +0.4 m/s, which make the effective
482 impacting velocity to be 0.6 m/s and 1.4 m/s, respectively. In the previous study (Wang et al., 2021),
483 it is confirmed that a larger effective impacting velocity causes a larger hydrodynamic force. Fig.
484 17(b) shows that the horizontal forces in the crest and trough entries are in the opposite direction,
485 which is due to the opposite horizontal velocity of the wave particle at the crest and trough positions.
486 For the wave entry in downward and upward points, the wave slope is the essential factor causing
487 the difference in the horizontal force of the cylinder.

488 Fig. 18 shows the pressure distribution on the cylinder for different entry positions. Due to the
489 vertical velocity of the wave particle, the downward point entry has the largest pressure, and the

490 pressure is the smallest in the upward point entry. The wedge entry in downward and upward
 491 positions can be identified as the asymmetric oblique entry for a symmetric wedge (Chen et al.,
 492 2022). However, the cylinder is tangent to the wave surface at the initial stage, with the same angle
 493 of relative deadrise angle on both sides, and the entry velocity is not perpendicular to the wave
 494 surface. Therefore, cylinder entry in downward and upward points can be regarded as a symmetric
 495 oblique entry. Therefore, the pressure distributions in Fig. 18 show that the pressure on the left side
 496 of the cylinder is larger than that on the right side of the upward point entry and opposite in the case
 497 of the downward point entry. Moreover, the magnitude and area of the negative pressure are also
 498 positively related to the effective entry velocity. Due to the difference in the horizontal wave velocity,
 499 the pressure distributions in the crest and trough entries are opposite to each other.

500 As shown in Fig. 18, the jet in the downward point entry has the larger upward velocity and
 501 length due to the larger effective entry velocity. In contrast, the jet at the upward point has a smaller
 502 vertical velocity causing the jet to bend downward earlier than that in other cases.



504
 505 Fig. 18 Pressure distribution and free surface for different entry positions in the impacting stage:
 506 (a) crest entry; (b) trough entry; (c) upward point entry; (d) downward point entry.

507

4.2.2 Effect of the entry position in the jet formation stage

As can be seen from the vertical acceleration curves in Fig. 17(a), the vertical force increases in the jet formation stage. For the crest and trough entries in Fig. 19, the pressure on the bottom surface of the cylinder tends to be symmetrical because the effect of the horizontal velocity of the waves disappears gradually. Therefore, the magnitude of the horizontal force decreases with the penetrating depth for the crest and trough entries. Fig. 19(d) shows that the pressure on the cylinder top surface is positive at $t = 0.3$ s. This is because the fluid flow above the cylinder moving inward compresses the air in the cavity which increases the pressure in the cavity. In addition, the downward point entry has a longer jet and a larger cavity volume compared to the other cases. The cavity in the upward point entry is incomplete due to the smaller effective entry velocity. For the trough entry, the jet on the right side is higher and steeper than that on the left side, which is opposite to the free surface distribution at the wave crest.

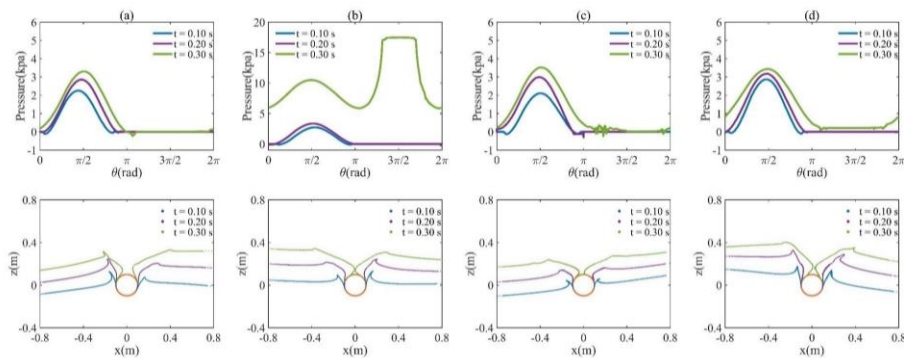
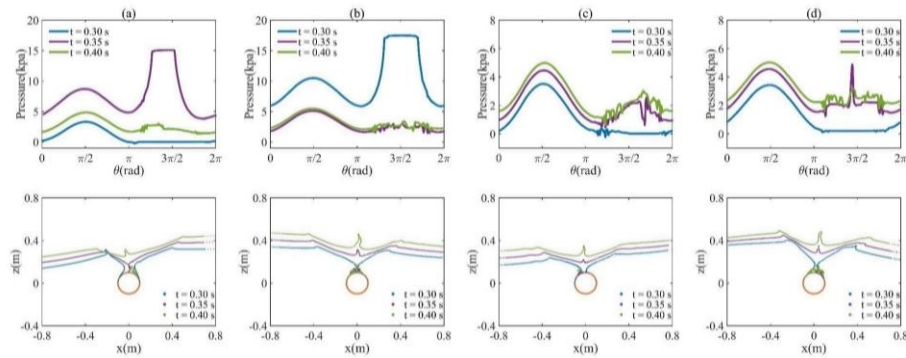


Fig. 19 Pressure distribution and free surface for different entry positions in the jet formation stage: (a) crest entry; (b) trough entry; (c) upward point entry; (d) downward point entry.

4.2.3 Effects of entry position in the cavity closure stage

According to the force curves in Fig. 17 and the free surface profiles in Fig. 20, it can be seen

527 that the cavity closes earliest at the trough entry and last at the crest entry. The close point of the air
 528 cavity is on the right side of the cylinder in the crest and downward point entries, which means that
 529 the air pocket is concentrated on the right top surface of the cylinder and exerts a horizontal force
 530 on the cylinder to the left. Because of the smallest effective entry velocity, the cavity volume in the
 531 upward point entry is the smallest, leading to the smaller pressure on the cylinder top surface in Fig.
 532 20. As shown in Fig. 17, the vertical force magnitude in the crest and trough entries is larger,
 533 followed by the upwind point entry, and finally the downward point entry. This feature can be
 534 explained by the effective entry velocity which is further discussed in Section 4.3.

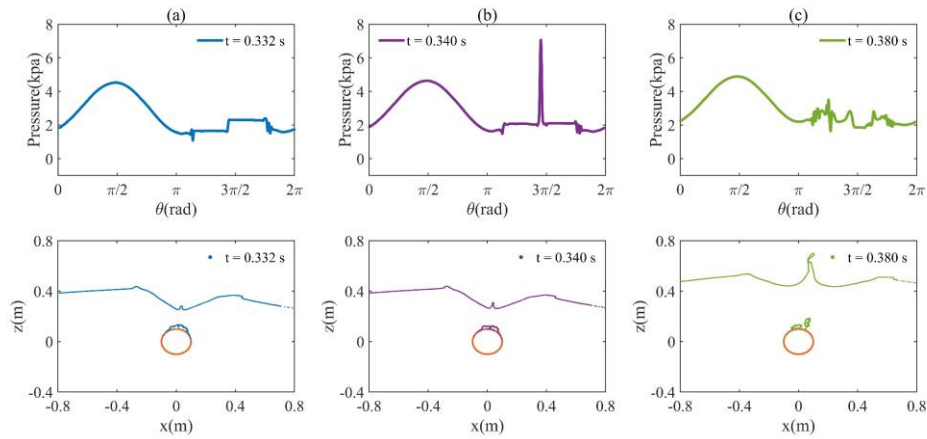


536
 537 Fig. 20 Pressure distribution and free surface for different entry positions in the cavity closure
 538 stage: (a) crest entry; (b) trough entry; (c) upward point entry; (d) downward point entry.

539
 540 The cavity variation is more complicated in the downward point entry because the cavity
 541 volume at the downward point is more complete and larger than in other cases. To better illustrate
 542 the process of cavity change after the cavity closure, Fig. 21 shows the pressure distribution and
 543 free surface profile during $t = 0.332-0.38$ s. At the entry time $t = 0.332$ s, the flow above the cylinder
 544 impacts each other and then divides into two parts: one part, namely the inward jet, impacts the
 545 cylinder surface downwards and the other part rises upwards forming a new vertical jet. The inward

546 jet divides the cavity into two pockets and the left part has greater pressure than the right part before
 547 the inward jet touches the cylinder's top surface. The inward jet hits the cylinder at $t = 0.34$ s,
 548 resulting in a pressure peak on the right upper surface of the cylinder as shown in Fig. 21(b). Then
 549 the inward jet generates two horizontal jets along the cylinder surface separating the air pocket from
 550 the cylinder surface. As the cylinder continues moving downward, the air pockets gradually leave
 551 the top surface of the cylinder and move upward toward the free surface. The air pocket on the right
 552 side rises faster than the right side for the downward point entry.

553



554

555 Fig. 21 Pressure distribution and free surface in the downward point entry after the cavity close:

556 (a) $t = 0.332$ s; (b) $t = 0.340$ s; (c) $t = 0.380$ s.

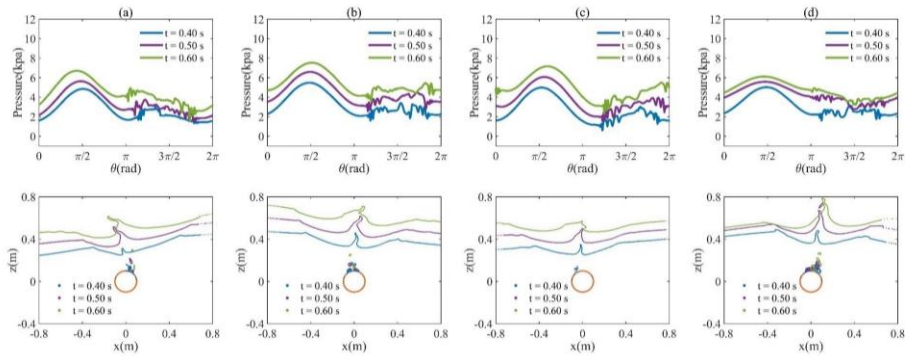
557

558 4.2.4 Effects of entry position in the sinking stage

559 As shown in Fig. 22, the pressure on the top cylinder surface is greater on the side with the
 560 bubbles. The reason for this phenomenon can be explained by the vertical velocity contour shown
 561 in Fig. 23, where the arrow indicates the fluid velocity, and the arrow color indicates the pressure
 562 value. It can be seen that the water particles above the cylinder flow to the air bubbles, resulting in
 563 greater pressure on the side of the cylinder surface where the bubbles exist. As shown in Fig. 22,

564 the upward jet is positively correlated with the effective entry velocity.

565



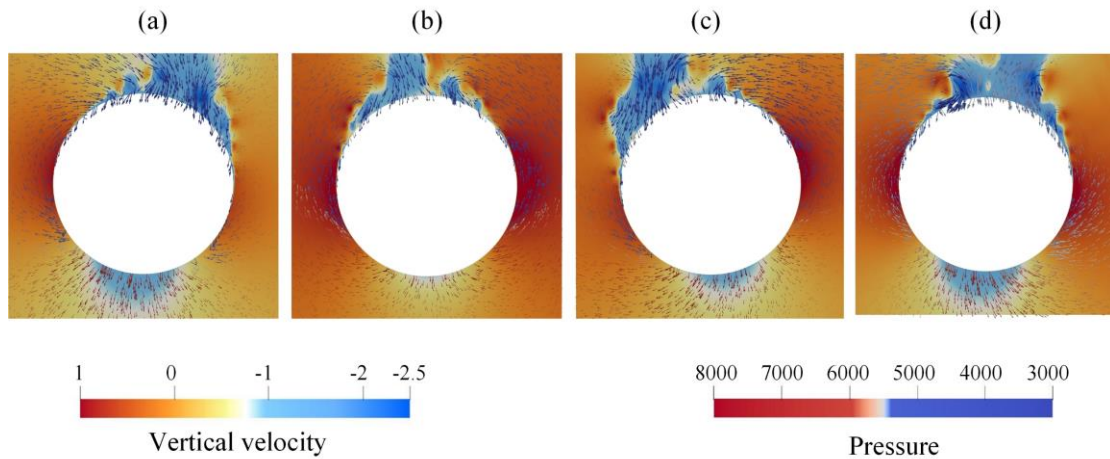
566

567 Fig. 22 Pressure distribution and free surface for different entry positions in the sinking stage: (a)

568

crest entry; (b) trough entry; (c) upward point entry; (d) downward point entry.

569



570

571 Fig. 23 Vector diagram of flow velocity for different entry positions at $t = 0.6$ s: (a) crest entry; (b)

572

trough entry; (c) upward point entry; (d) downward point entry.

573

574 4.3 The influence of cylinder entry velocity

575

Three different entry velocities $v = 0.5, 1.0, \text{ and } 1.5$ m/s are considered to investigate their

576

influence on the wave entry of a cylinder, including the hydrodynamic force, pressure distribution,

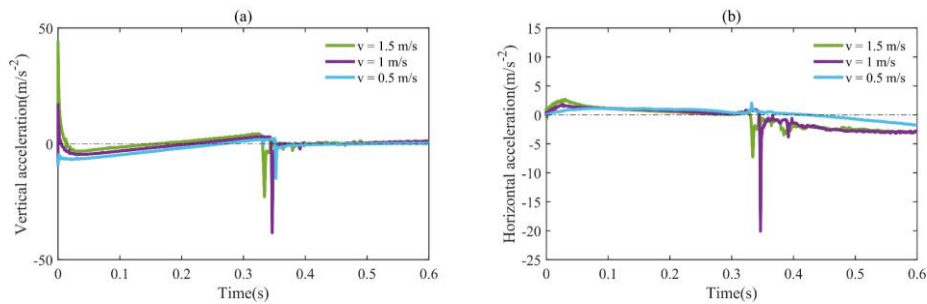
577

and free surface profile. According to the wave particle velocity, the results of the entry velocity

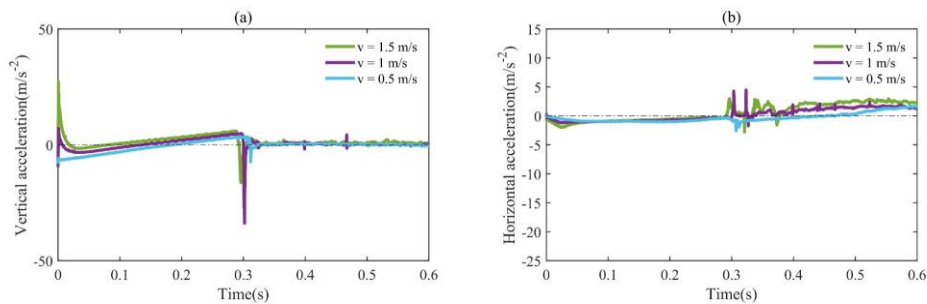
578 effect are divided into two groups for discussion, which are the case of the crest-trough positions
579 and the case of the upward-downward position respectively.

580 4.3.1 Effects of entry velocity at crest and trough positions

581 As shown in Fig. 24 and Fig. 25, the entry velocity has a significant influence on the vertical
582 and horizontal accelerations in the impacting stage and the cavity closure stage. In the impacting
583 stage, the impact force on the cylinder becomes greater with the increase of the entry velocity. The
584 larger impact force drops faster at the end of the impacting stage. The larger entry velocity makes
585 the pressure on the cylinder more asymmetric, resulting in a greater magnitude of horizontal force
586 at the impact stage.



588
589 Fig. 24 Comparison of accelerations of the cylinder with different initial velocities in the wave
590 crest entry: (a) vertical acceleration; (b) horizontal acceleration.



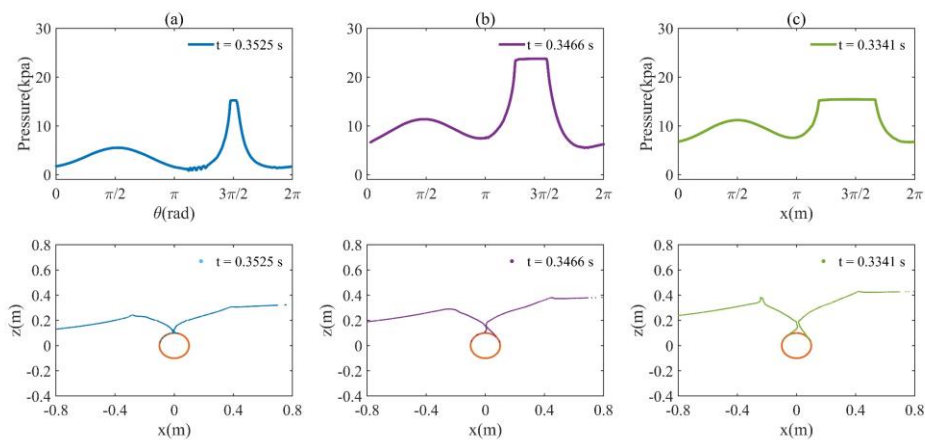
592
593 Fig. 25 Comparison of accelerations of the cylinder with different initial velocities in the wave

594 trough entry: (a) vertical acceleration; (b) horizontal acceleration.

595

596 In the cavity closure stage, the compressed cavity exerts a large pressure on the cylinder top
597 surface, which contributes to sharp fluctuations in the vertical and horizontal forces. As observed in
598 Fig. 24 and Fig. 25, it can be concluded that the large entry velocity causes the cavity to close earlier.
599 However, different from the impacting stage, the force magnitude is largest at $v = 1.0$ m/s, which
600 indicated that the force magnitude is not positively related to the entry velocity at the time of the
601 cavity closure. This phenomenon may be due to the cavity volume at the cavity closure moment as
602 shown in Fig. 26 and Fig. 27. When the entry velocity is $v = 0.5$ m/s, the cavity is small and
603 incomplete, and then the air pocket is quickly expelled upwards so that the air pocket does not exert
604 a large pressure on the upper surface of the cylinder. In the cases of $v = 1.0$ and 1.5 m/s, the air
605 pocket has been well developed and the cavity volume increases with increasing the entry velocity.
606 However, for the well-developed cavity, the large cavity volume has a smaller compressed rate,
607 resulting in a negative correlation between the pressure at the top of the cylinder and entry velocity.

608



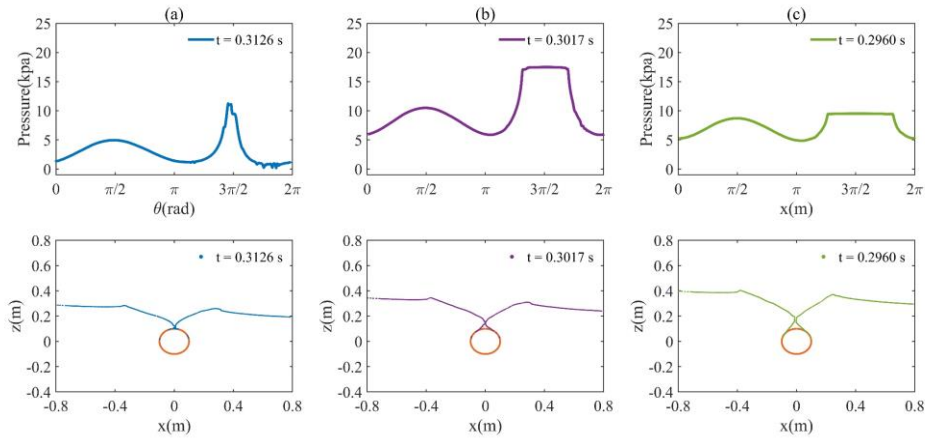
609

610 Fig. 26 Pressure distribution and free surface profile in the wave crest entry at the moment of

611

cavity closure: (a) $v = 0.5$ m/s; (b) $v = 1.0$ m/s; (c) $v = 1.5$ m/s.

612



613

614 Fig. 27 Pressure distribution and free surface profile in the wave trough entry at the moment of

615 cavity closure: (a) $v = 0.5$ m/s; (b) $v = 1.0$ m/s; (c) $v = 1.5$ m/s.

616

617 4.3.2 Effects of entry velocity at upward and downward positions

618 Fig. 28 and Fig. 29 show the accelerations in the upward point entry and downward point entry

619 respectively. The vertical-down velocity of the wave particle leads to a smaller effective entry

620 velocity in the case of upward point entry. Therefore, the cavities in the upward point entry with v

621 = 0.5 and 1.0 m/s are not complete which leads to the smaller pressure on the top surface of the

622 cylinder in the cavity closure stage as shown in Fig. 30. The downward point entry with three entry

623 velocities all forms the complete cavity due to the vertical-up velocity of wave particle. In Fig. 31,

624 the downward point entry with $v = 0.5$ m/s has a smaller complete cavity volume resulting in a

625 greater cavity compression rate, which leads to the larger pressure on the cylinder top surface.

626

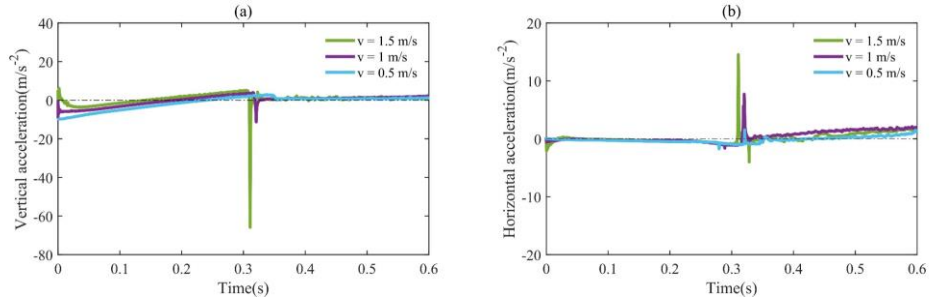


Fig. 28 Comparison of accelerations of the cylinder with different initial velocities in the wave

upward position: (a) vertical acceleration; (b) horizontal acceleration.

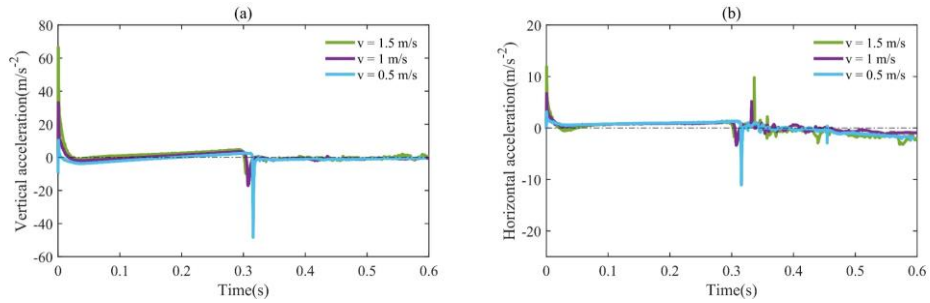


Fig. 29 Comparison of accelerations of the cylinder with different initial velocities in the wave

downward point: (a) vertical acceleration; (b) horizontal acceleration.

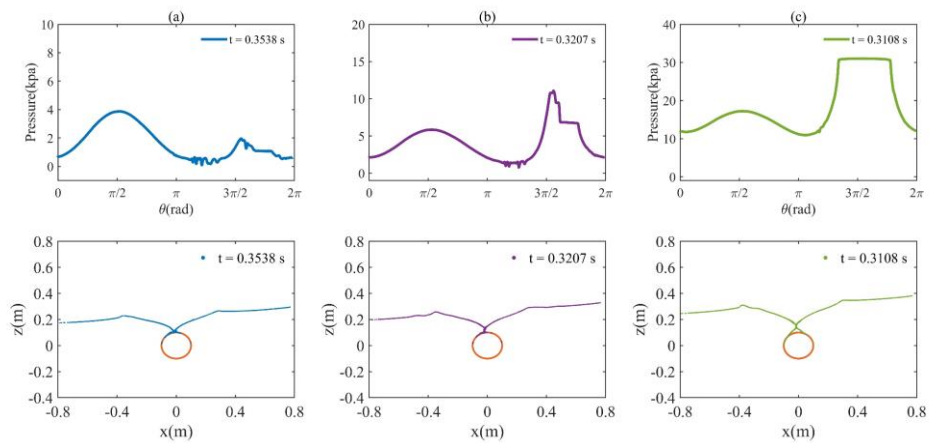
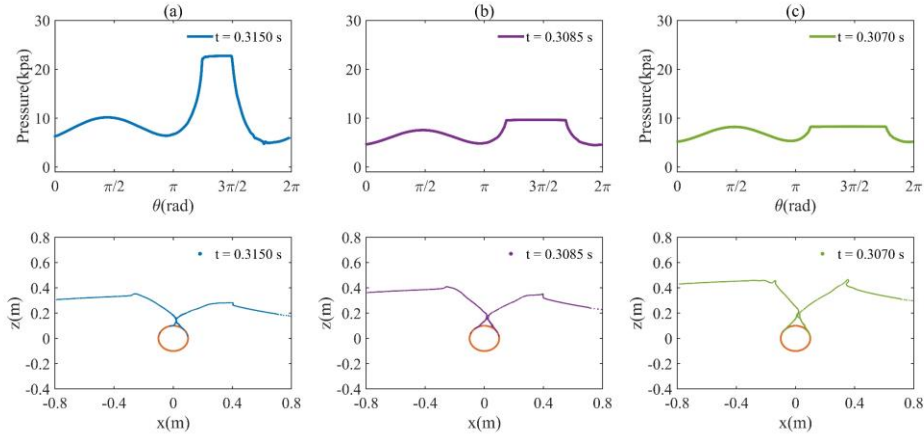


Fig. 30 Pressure distribution and free surface profile in the upward point entry at the moment of

cavity closure: (a) $v = 0.5$ m/s; (b) $v = 1.0$ m/s; (c) $v = 1.5$ m/s.



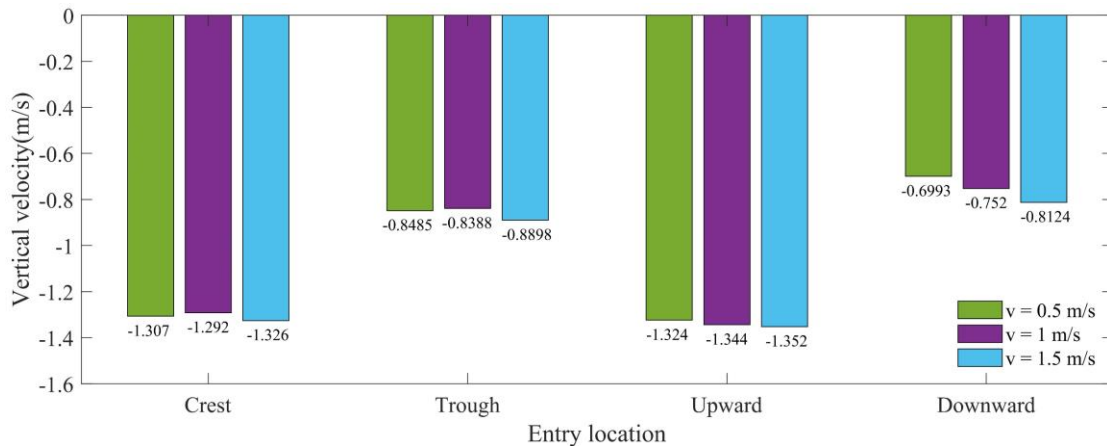
639

640 Fig. 31 Pressure distribution and free surface profile in the downward point entry at the moment of
 641 cavity closure: (a) $v = 0.5$ m/s; (b) $v = 1.0$ m/s; (c) $v = 1.5$ m/s.

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643 At the moment of cavity closure, the vertical velocity of a cylinder with different entry
 644 positions is presented in Fig. 32. In each entry position case, the vertical velocity of the cylinder is
 645 similar in the cavity close stage which is almost independent of the initial impact velocity. This is
 646 because the cylinder with a larger entry velocity is subjected to larger hydrodynamic forces resulting
 647 in a faster deceleration of the cylinder. It also can be found that the vertical velocity in the cavity
 648 closure stage for the crest and upward point entries is larger than that for the trough and downward
 649 point entries.

650



651

652 Fig. 32 Vertical velocity of the cylinder at the moment of cavity closure.

653

654 5. Conclusion

655 This paper investigates numerically the entire process of a cylinder entering the wave with the
656 air cavity effect using the OpenFOAM. A convergence study for the jet profile of the cylinder
657 entering the calm water is first performed to find an appropriate mesh scheme. By proposing the
658 constraint for the *sixDoFRigidBodyMotion* solver, the process of the cylinder being lowered by a
659 crane in the air, and then free-falling into the wave is simulated. Several case studies are conducted
660 to further investigate the effects of the entry position and entry velocity on the wave entry of a
661 cylinder. The following conclusions can be drawn based on the numerical results.

662 (1) The process of the cylinder entering waves can be divided into four stages, i.e. impacting
663 stage, jet formation stage, cavity closure stage, and sinking stage according to the acceleration of
664 the cylinder. At the beginning of impacting stage, the maximum pressure occurs in the jet root region
665 which is the same as the pressure distribution of the wedge entry. Then the maximum pressure
666 moves towards the centre of the bottom surface of the cylinder. During the jet formation stage, the
667 jet separates from the cylinder surface, and the pressure and the vertical force gradually increase
668 with the penetration depth. In the cavity closure stage, the jet roots on the left and right sides move
669 toward each other to form a cavity. Then the cavity compressed by the liquid exerts a large pressure
670 on the upper surface of the cylinder. In the sinking stage, the pressure on the left and right sides is
671 more asymmetric with the penetration depth leading to an increase in the horizontal force.

672 (2) The effect of entry position on the cylinder entering waves can be summarized by two
673 factors, i.e., the wave particle velocity and the wave slope. At the wave crest and trough positions,

1 674 the horizontal velocity of the wave particle contributes to the asymmetric effect on the pressure
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3 675 distribution. Because the horizontal velocity decays more rapidly along with the depth, the
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6 676 asymmetric pressure distribution gradually disappears as the cylinder moves down. The wave slope
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9 677 at the upward and downward points causes pressure asymmetry on both sides of the cylinder.

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11 678 (3) The effect of the water entry velocity is mainly reflected in the impacting stage and cavity
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14 679 closure stage. A larger water entry velocity causes greater slamming pressure on the cylinder bottom
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17 680 surface in the impacting stage. Then the cavity volume is positively related to the effective entry
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20 681 velocity. When the effective entry velocity is small, the cavity formation is incomplete leading to
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23 682 the small pressure on the cylinder top surface at the moment of cavity closure. When the effective
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26 683 entry velocity is large enough to form a complete cavity, the pressure at the top of the cylinder is
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29 684 negatively related to the effective entry velocity. Moreover, the cylinder velocity at the moment of
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32 685 cavity close is almost independent of the initial impact velocity for each entry position.

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34 686 The research in this paper provides guidance for the design of controllers for hoisting payloads
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37 687 into the waves by the cranes in terms of the entry velocity, entry position, etc. However, this study
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40 688 still has some limitations. Firstly, the two-dimensional simulation can not obtain the three-
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43 689 dimensional characteristics of the water entry process. Second, the present work considers the water
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46 690 entry of a cylinder into regular waves which has a large gap with the real complex sea state. Finally,
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49 691 the effect of the crane cable on the water entry is ignored, which is different from real crane
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52 692 operations. We would try to break through the limitations in our future research.

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