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# Speculative bubbles or explosive fundamentals in stock prices? New evidence from SADF and GSADF tests

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## 21 Abstract

This paper uses recently developed sequential ADF tests to distinguish between rational speculative bubbles and explosive fundamentals in the US Stock market. The sequential ADF tests are shown to be more sensitive than the conventional ADF test. Results also suggest the more refined GSADF test may deliver more consistent results compared to the SADF test. We find strong evidence of explosive behavior in real stock prices that cannot be attributed to explosive fundamentals. We find renewed evidence of a stock market bubble during the dot com boom but no evidence of a bubble at other times.

- 29 Keywords: Rational bubbles, SADF test, GSADF test, Fundamental value, Explosive behavior
- 30 AMS Classification: 62F03; 62P20
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## 1. Introduction

2 For centuries bubbles and crashes have fascinated both academics and the public at large (Reinhart & Rogoff, 2009). However, recent events 4 such as the internet bubble and the subprime and Eurozone crises have 5 given the subject a renewed sense of importance. Allied to their real-6 world significance modelling bubbles poses several difficult theoretical 7 challenges (Cochrane, 2005). The available empirical evidence is also 8 mixed (Gurkaynak, 2008). A common misconception is that bubbles 9 necessarily imply mass irrationality. However, Blanchard and Watson 10 (1982) introduced rational bubble models to account for the possibility 11 that asset prices may deviate from fundamentals without assuming 12 irrationality on the part of market participants. In addition to the subject's 13 wider importance several new tests have recently been developed to detect 14 speculative bubbles (see e.g. Al-Anaswah & Wilfling, 2011; Lammerding 15 et al., 2013; Asako & Liu, 2013; Cheah & Fry, 2015). Here, we apply the 16 sequential unit root tests developed in Phillips et al. (2015). These indirect 17 stationarity tests have a long heritage in econometrics (see e.g. Diba & 18 Grossman, 1988; Hamilton & Whiteman, 1985), are linked to a voluminous 19 literature on rational bubble models and also have the advantage of being 20 able to detect bubbles despite a potential misspecification of the bubble 21 process. This approach has also begun to gain traction in empirical 22 applications as diverse as exchange rates (Bettendorf & Chen, 2013), 23 commodity markets (Xiaoli et al., 2014), metals markets (Figuerola-Feretti, 24 2015) and bitcoin (Cheung et al., 2015). Therefore this paper applies 25 sequential unit root tests to shed new light upon the existence of rational 26 bubbles in the US stock market. We find strong evidence of a bubble 27 in US stock prices that cannot be explained by explosive behaviour in 28 fundamentals. However, this appears to be confined to a single bubble 29 episode during the dot com boom at the turn of the century. The layout 30 of this paper is as follows. Section 2 describes the rational bubble model 31 and sequential ADF tests used in this paper. Section 3 discusses empirical 32 results. Section 4 concludes.

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## 2. Rational bubbles and sequential ADF tests

36 The conventional unit root and cointegration tests, initially applied 37 by Diba and Grossman (1988), are often unable to confirm the existence 38 of bubbles when they are periodically collapsing. To overcome this 39 problem, Phillips et al. (2011), Phillips and Yu (2011) and Phillips et al. 40

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1 (2015) recently proposed a new test procedure to detect any bubble as well as its starting and ending points. According to these authors, testing 2 3 for a mildly explosive departure from a unit root data-generating process 4 can be a convenient method consonant with our goal of checking if there 5 are bubbles in the financial data. These testing procedures have become 6 increasingly significant for empirical applications. For exemple, El 7 Montasser, Fry and Apergis (2016) have used such a procedure to test 8 if there are bubbles in US-China exchange rate, while Chang et al. (2016) have applied it to BRICS stock markets. In other areas of application, El 9 10 Montasser (2015) applied this method to test for bubbles in the ethanol-11 gasoline price ratio of Brazil, while Caspi, Katzke and Gupta (2015) have 12 employed these right-tailed ADF tests for testing bubbles in a historical 13 data of US oil price...etc...

14 The motivation behind this set of tests is as follows. Rational bubble 15 models are derived from the present value theory of finance whereby 16 prices are determined by the sum of the discounted present values:

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 $P_{t} = \frac{1}{1+R} E_{t} \left( P_{t+1} + D_{t+1} \right), \tag{1}$ 

where *R* is the constant interest rate. A log-linear approximation of
 equation (1) (Campbell & Shiller, 1989) gives

$$\log P_t = p_t = p_t^f + b$$

where the fundamental component  $p_t^f$  is completely determined by expected dividends:

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26 27  $p_{t}^{f} = \frac{\kappa - \gamma}{1 - \rho} + (1 - p) \sum_{i=0}^{\infty} \rho^{i} E_{t} d_{t+i+1},$  $\gamma = \log(1 + R) \text{ and } \kappa = -\log(2) - (1 - 2)\log(1 - 1) \text{ The}_{t}$ 

where  $\gamma = \log(1 + R)$  and  $\kappa = -\log(\rho) - (1 - \rho)\log(\frac{1}{\rho} - 1)$ . The double component  $b_t$  satisfies

 $b_t = \lim_{i \to \infty} \rho^i E_t p_{t+i},$ 

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 $E_t(b_{t+1}) = \frac{1}{\rho} b_t = \left(1 + \exp\left(\overline{d-p}\right)\right) b_t, \qquad (2)$ 

where  $\overline{d-p}$  denotes the average log dividend-price ratio. See e.g. Phillips et al. (2011) for full details. From equation (2) the bubble component  $b_t$  has the stochastic representation

 $b_{t} = (1+g)b_{t-1} + \varepsilon_{b,t}, E_{t-1}(\varepsilon_{b,t}) = 0,$ (3)

where  $g = \exp(\overline{d-p}) > 0$  is the growth rate of the (log) bubble. The stochastic properties of the  $p_i$  are determined by equation (3) (see e.g. Phillips et al., 2011). In particular, equation (3) shows that explosive bubbles will lead to a right-sided departure from a unit root for g > 0.

Motivated by the above Phillips et al. (2015) consider an ADF-type regression in a rolling window for a given time series  $y_t$ . An ADF regression is run over a rolling interval beginning with a fraction  $r_1$  and ending with a fraction  $r_2$  of the total number of observations. Therefore the size of the window as a proportion of the whole sample is  $r_w = r_2 - r_1$ . The time series model at the root of Phillips et al. (2015) can be presented as follow:

$$y_t = m + \lambda y_{t-1} + \sum_{i=1}^{p} \alpha_i \Delta y_{t-i} + \varepsilon_t, \ \varepsilon_t \ iid \ N(0, \sigma^2), t = 1, \dots, T.$$

$$\tag{4}$$

11 As suggested by equation (3) the usual null hypothesis  $H_0$ :  $\lambda = 1$ 12 applies but Phillips et al. (2011) suggest an unconventional alternative 13 defined as follows:  $H_1: \lambda > 1$ , therefore focusing attention on the right 14 side of the distribution. Explicitly, we reject the null if the test statistic of 15 Phillips et al. (2011) is greater than the critical value— determined by the 16 authors through the use of Monte Carlo simulations. Consequently, if the 17 null is rejected, we have an explosive process to take account of the bubble 18 phenomenon. The number of observations considered by (4) is  $T_{w} = [r_{w}T]$ 19 where T is the total number of observations and [.] denotes the integer 20 part. The ADF statistic associated to equation (4) is denoted  $ADF_{r}^{r_2}$ . 21

As noted by, *inter alia*, El Montasser *et al*. (2015, 2016), bubbles generally 22 collapse periodically, and it is often observed that the traditional unit root 23 tests have low power in detecting them. To overcome this shortcoming 24 Phillips et al. (2011) and Phillips and Yu (2011) propose to use recursive 25 sequences of right-tailed ADF-type tests based on a forward expanding 26 sample and then take the supremum of these. Homm and Breitung (2010) 27 point out that this test delivers a fairly efficient bubble-detection technique in 28 one or two bubble alternatives. Accordingly, Phillips et al. (2015) show 29 that although the procedure in Phillips et al. (2011) consistently estimates 30 the start date of the first bubble in any sample in case of two bubble 31 alternatives, it may fail to identify the second bubble. Inter alia this 32 implies that in the presence of two bubbles, the second bubble may not 33 be detected if it is dominated by the first bubble. This motivated Phillips 34 et al. (2015) to formulate a backward sup ADF test where the endpoint of 35 the subsample is fixed at a fraction  $r_2$  of the whole sample and the window 36 size is expanded from an initial fraction  $r_0$  to  $r_2$ ; for more details, see El 37 Montasser et al. (2015, 2016). 38

In summary, the backward sup ADF (SADF) statistic is defined as

$$SADF_{r_2}(r_0) := \sup_{r_1 \in [0, r_2 - r_1]} ADF_{r_1}^{r_2}.$$
(5)

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Table 1

Summary statistics of the log-returns of the series $P_t$ and $P_t - F_t$		
Series	$P_t$	$P_t - F_t$
Mean	0.020	0.017
Median	0.028	0.018
Standard Deviation	0.177	0.013
Skewness	-0.611	-0.286
Kurtosis	3.522	2.500
Jarque – Bera	10.389	3.389

12 The generalized sup ADF (GSADF) is then constructed by repeatedly 13 implementing the SADF test procedure for each  $r_2 \in [r_0, 1]$ . The GSADF 14 statistic can be written as 15 CCADE () CADE ()

$$GSADF(r_0) := \sup_{r_2 \in [r_0, 1]} SADF_{r_2}(r_0).$$
(6)

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## 3. Empirical analysis

19 In this paper, we test the null hypothesis of no rational speculative 20 bubbles in the US stock market against the alternative that such bubbles 21 do exist. Data consist of annual observations for the S&P 500 index for 22 the years 1871-2013 and consist of the stock price index  $P_t$  (detrended 23 by dividing by a factor proportional to the long-run exponential growth 24 path), and its ex-post rational counterpart  $F_t$  (proxy of fundamental value) 25 - the discounted present value of the actual subsequent real dividends. 26 Summary statistics for the series  $P_t$  and  $P_t - F_t$  are shown below in Table 27

## Table 2

### Sequential ADF tests results

31	Variable	ADF test	SADF test	GSADF test
32	P <sub>t</sub>	-2.018	4.649**	4.649**
33 34	$P_t - F_t$	-3.125	2.863**	2.863**
35	1% Critical Value	-0.240	0.964	1.404
36	5 % Critical Value	-0.899	0.408	0.951
37	10% Critical Value	-1.253	0.174	0.709

Notes: For the SADF and GSADF tests the initial window size  $r_0$  is set as three years (36 observations). Critical values are based on Monte-Carlo simulations with 1000 replications. 40 \*\* denotes significance at the 1% level.





Notes: This graph shows the series of the difference between the real stock price and its
 fundamental (green line, right axis) and its corresponding sequence of ADF statistics (blue
 line, left axis). The red line (left axis) represents the 5% critical values of the GSADF test.

231. Real stock prices appear to show excess volatility (Shiller, 1981). The24two series  $P_t$  and  $P_t - F_t$  do appear quite different in nature although both25series appear to be negatively skewed. The series  $P_t - F_t$  is thinner tailed,26less volatile and closer to being normally distributed than the series  $P_t$ .

27 The results of the sequential ADF tests are shown in Table 2. The 28 standard right-sided ADF test gives no evidence of explosive behaviour 29 in stock prices and the series  $P_t - F_{t'}$  as well. As mentioned above, this 30 result could be misleading if periodically collapsing bubbles occur 31 during the given period (Evans, 1991). The SADF and the GSADF tests 32 help to counter this shortcoming. Both the SADF and GSADF test give 33 conclusive evidence for explosive behaviour in both real stock prices and 34 the difference between real stock prices and estimated fundamental value. 35 Thus, the SADF and GSADF tests give convincing evidence for rational 36 speculative bubbles beyond purely explosive behavior in fundamentals.

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price and fundamental value

Notes: See Figure 3.

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20 21 Next, we address the timing of the bubble. Here, we stress that it 22 is sometimes difficult to specify the nature of the bubble---its name and 23 type-that corresponds to the time interval identified by our tests. So, 24 upstream, we will focus on the chronological coincidence as a criterion. 25 In this sense, our analysis will be based on the history of bubbles and 26 identify subsequently those that fit our time interval. Downstream, we 27 will explain by what mechanism this bubble identified affects the US stock 28 prices in the United States. The SADF test shown in Figure 1 suggests 29 explosive behaviour in prices over the years 1964-69 (Johnson's escalation 30 of the Vietnam war- a result consistent with findings in Brune et al., 31 2015), 1997-2001 (dot com boom and its aftermath) and from 2006-2008 32 (crash of 2008). However, once it is applied to the difference between 33 observed and fundamental prices, the SADF test suggests that in 1964-34 69 and 2006-2008, we have explosive fundamentals rather than a stock 35 market bubble (see Figure 2). This approach also suggests clear evidence 36 of a bubble during the dot com boom (1997-2001). In contrast, the more 37 advanced GSADF gives more consistent results. The GSADF test suggests 38 explosive behaviour in stock prices only from 1997-2001 (see Figure 3). 39 There is also explosive behaviour in the difference between the real stock 40

price and the fundamental value from 1998-2000 (see Figure 4). Thus, 1 we conclude that we have evidence for only one bubble (1998-2000) that 2 3 cannot be explained by explosive fundamentals. Still, how to show this is 4 an Internet bubble? Or in other words, through what channels we end up 5 with such a bubble type? To explain this point, remember what happened in that time interval. At that point, the ferocity and frequency of the initial 6 7 public offerings of internet companies have indeed created euphoria in 8 US stock market. Investors blindly grapping in every new issue without 9 even looking at a business plan and many of them foolishly ignored the 10 fundamental rules of investing in the stock market, such as analyzing P/E 11 ratios and studying market trends. The bursting of the bubble precipitated 12 the 2001 stock market crash even more so than the September 11, 2001 13 terrorist attacks.

14 As we have used historical data on US stock prices, it is advantageous 15 to divide the studied sample into various sub-samples to get a clearer idea of the bubble behavior. In resorting to such an approach, we can expect 16 17 such that a bubble is present in a sub-sample and no longer present in 18 the overall sample, and vice versa. This sample subdivision is ensured by the Bai and Perron's (1998) test identifying multiple unknown break dates 19 therein. This procedure allowed us to identify two unknown break dates, 20 21 namely 1956 and 1992. This suggests the study of three sub-samples: from 22 1871 to 1956, from 1957 to 1992, and from 1992 until 2013. Since the last 23 sub-sample contains a limited number of observations-and given that 24 the Phillips et al. (2015) procedure requires a rather considerable initial 25 window- we decided to eliminate it and focus attention on the first subsample and the second extended one running from 1956 till 2013. In view 26 of Table 3, and using the three sequential tests, we don't find any bubble 27 28 in the stock prices, nor in the difference between real stock price and 29 fundamental value, if the study involver the first sub-sample.

30 However the situation will clearly change in the second sub-sample, 31 since both SADF and GSADF tests indicate that there are a number of 32 bubbles in the stock prices and withal the series devoid of the fundamental component. To save space, we will focus on the GSADF test results since 33 34 it is more powerful than the SADF test, especially in the multiple bubble-35 scenario, as we have mentioned above. That is why we are introducing only GSADF figures for the two series. At this level, Figure 5 shows that 36 37 there are two bubbles: a relatively wide one dating from 1996 until 2003, and the other more or less reduced covering the period 2008-2009. On 38 39 the other hand, Figure 6 shows for the series devoid of its fundamental 3 bubbles: the first from 1996 to 2001, the second from 2001 to 2003, and 40

#### Table 3

Sequential ADF test results for the first sub-sample (from 1871 to 1956)

Variable	ADF test	SADF test	GSADF test
$P_t$	-2.079	-1.028	-0.597
$P_t - F_t$	-3.028	-1.028	-0.789
1% Critical Value	-0.430	0.760	1.164
5 % Critical Value	-1.053	0.228	0.600
10% Critical Value	-1.342	-0.077	0.386

#### Table 4

### Sequential ADF test results for the second sub-sample (from 1957 to 2013)

Variable	ADF test	SADF test	GSADF test
$P_t$	-1.908	4.210**	3.098*
$P_t - F_t$	-1.664	2.442**	2.738*
1% Critical Value	-0.244	1.606	3.952
5 % Critical Value	-0.867	0.723	2.225
10% Critical Value	-1.181	0.449	1.765

21 *Notes:* <sup>\*</sup> indicates significance at the 5% level. See Table 2.

23 the third covering a shorter period (2008-2009). So the difference from 24 the previous figure lies at the second bubble detected. This seems to be 25 the aftermath of the Internet bubble. More specifically, many technology companies realized good business, but investors have mightily 26 27 exaggerated the importance of the far long-term in their estimates, and 28 neglected to calculate that some of the companies consumed too fast their 29 capital to hope one day reach the balance point. It is remarkable withal that compared to the overall sample results, the test GSADF detected a 30 31 second bubble in the both studied series. This might argue for the overall sample subdivision, especially when working on historical data. In point 32 of fact, such a subdivision may disclose other informative elements hidden 33 in the data. 34

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## 4. Conclusion

In this paper, we used the new right-tailed tests introduced in the literature by Phillips *et al.* (2011) and Phillips *et al.* (2015) to test if there are bubbles affecting the US stock market. In doing so, we used historical

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1 data series of the stock price index—from 1871 till 2013— and the latter 2 series devoid of its fundamental value. Given that Bubbles are, in general, 3 decisively identified in retrospect, we will build on the chronological 4 coincidence with the bubble time interval suggested by the tests and the 5 stylized facts reported in the literature to define the nature of the bubble in question. This paper has found evidence of a bubble in the US stock 6 7 market likely at the time of the dot com boom. We find explosive behavior 8 in both the real stock price and the difference between real stock price 9 and the fundamental value (bubble). This behavior cannot be attributed 10 to explosive fundamentals. The evidence in favor of bubbles at other 11 times appears limited. The GSADF test identifies only one bubble. The 12 SADF test labels attributes explosive behavior in prices, coincident both 13 with the escalation of the Vietnam war and the 2008 crash, to explosive 14 fundamentals. However, by dividing the whole sample into two subsamples, the GSADF test will detect another bubble of a limited size (2008-15 16 2009) in the second subsample---from 1957 till 2013--- for both studied 17 series. Evidence suggests that the GSADF gives more consistent results 18 than the SADF test and may constitute a meaningful improvement in 19 applications. Our results may thus hold practical implications for investors and financial market authorities alike and reinforce the importance of 20 21 analyzing fundamentals when identifying bubbles.

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