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Hybrid Ageing Patterns for Face Age Estimation

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Abstract

Wrinkles can be embedded in several image-based applications as a descriptor for human skin. However, wrinkle-based age estimation research has not been widely addressed. In this paper, we introduce a Multi-scale Wrinkle Patterns (MWP) representation, investigate the effect of wrinkles on face age estimation and propose Hybrid Ageing Patterns (HAP) for face age estimation. To define the wrinkle regions more precisely, a template consisting of 10 regions constructed relatively to a set of automatically located facial landmarks is used. We extract the multi-scale wrinkles in each region and encode them into MWP. We use Support Vector Regression to estimate age from the combination of such patterns. The performance of the algorithms is assessed by using Mean Absolute Error (MAE) on three state-of-the-art datasets - FG-NET, FERET and MORPH. We observe that MWP produces a comparable MAE of 4.16 on FERET to the state of the art. Finally we propose HAP, which combines the features from MWP and the Facial Appearance Model (FAM), and demonstrate improved performance on FERET and MORPH with MAE of 3.02 (± 2.92) and 3.68 (± 2.98), respectively. Therefore, we conclude that MWP is an important complementary feature for face age estimation.

Keywords: Age estimation, wrinkle detection, facial appearance model, line tracking, support vector regression.

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1. INTRODUCTION

Automatic face age estimation is an important, yet largely unsolved, challenging problem. This challenge can be attributed to (i) large intra-subject variations and (ii) large inter-subject similarity. The large intra-subject variations include craniofacial growth and changes on skin texture, meanwhile, the inter-subject similarities are gender and race.

Conventionally, age estimation methods are based on appearance features. Appearance features are computed or modelled for an entire face that comprises shape and texture [1]. For facial ageing research, many algorithms [2, 3, 4, 5] use the appearance parameters produced by the facial appearance model (FAM) [1] and age manifold [6, 7]. FAM is a generative model that constructs the target subject’s face by a set of hidden parameters [8] while manifold learning is a non-linear dimensionality reduction approach. Faces at different ages can be generated under a similar subspace with varying parameters for controlling the shape and texture. However, age progression modelling is highly complex due to large intra-subject variation and inter-subject similarity [9]. In addition, dimensional reduction of principal components analysis (PCA) in FAM is a form of averaging which smooths out wrinkles as there is no correspondence from one individual to another [10].

To investigate the effect of wrinkles on face age estimation algorithms, accurate wrinkle detection is an important task in face analysis [11, 12]. Judgments are typically made on neutral and frontal face images because it is the most commonly found in the datasets. The majority of the latest works on wrinkle assessment are based on clinical perspective (subjective assessment). Clinician perspective focuses on the level of wrinkle severity which is assessed using either descriptive or photographically-calibrated scales [13]. The subjective assessment limits the scientific study of detailed wrinkles information in terms of location, density and depth. On the other hand, computer vision algorithms are capable of extracting these information and formed an objective assessment [14]. Choi et. al. [10] studied the local feature extraction for age

estimation. They claimed that the facial wrinkles and skin texture are very important information for age estimation. With age increasing, facial wrinkles are increased and spots or blotches are appeared on skin texture. These aging features are generally shown as high frequency components on images. However,
 35 there was no validation on the extracted wrinkles. This implies that age estimation using wrinkle features still a challenging problem. Therefore, a reliable and accurate computerised wrinkle detection method is crucial for this study. The following observations outline the limitations of existing wrinkle-based age estimation studies:

- 40 1. Conventionally, a significant user interaction is required for identifying the facial wrinkles. It is time consuming and subjective, depending on the user expertise.
2. Existing wrinkle-based features [15, 10] are not robust for face age estimation. They are either weakly represented or not validated against the
 45 ground truth.
3. Conventional features such as local binary patterns (LBP) require high dimension representation and computational expensive.

The main contributions of this paper are:

- 50 1. Multi-scale Wrinkle Patterns (MWP) is proposed as a feature representation for facial wrinkles. This representation includes wrinkle location, intensity and density, which is a better descriptor than conventional local features.
2. Hybrid Ageing Patterns (HAP) is proposed as a new feature representation for face age estimation. It is a fusion of FAM and MWP to form a new
 55 complementary feature representation.

This paper is organised into the following sections: Section 2 discusses the related work on face age estimation; Section 3, 4, and 5 outlines MWP, HAP and Support Vector Regression (SVR), respectively; Section 6 presents the results and discussion; finally, the conclusion is summarized in Section 7.

60 2. RELATED WORK

The process of age estimation attempts to label a facial image automatically with the exact age (year) or the age group (year range) of the individual face. By deriving significant features from faces of known ages, the age of an individual face can be estimated by solving the inverse problem using the same feature-
65 extraction technique. Although many algorithms have been proposed since 1994 [16, 17, 18], age estimation is still a challenging problem due to three reasons [2]. First, face age progression is uncontrolled and personalized. Such special characteristics of ageing variation cannot be captured easily due to the large variations conveyed by human faces. Second, there is no complete facial ageing
70 dataset with chronological ages. It is hard to collect a large facial image set of people throughout their life which are sufficient to present detailed aging progression. Third, it is difficult to define an absolute ageing pattern that can be used to quantify one particular age. For example, these are invalid arguments: two wrinkles at the eye corner is classified as age 20; three wrinkles as 30 years
75 old. Such arguments fail to predict the age between 20-30 and misleading. Thus, a robust ageing representation is needed to cope with the identified problem.

2.1. Face Age Estimation

Age estimation methods can be broadly classified as global and local approaches. In the former, a common way is to capture the variability in the
80 facial appearance by using FAM and then apply the regression method for predicting the age. For the local approach, this refers to representing local features such as wrinkles, spots and pores in an ageing pattern and then the corresponding age is estimated by regression. One might think that local features can only be used for age group classification, Ng et al. [19] has proven that a specific age
85 can be learned and estimated from the wrinkle-based features. They present wrinkle by the pixel intensity values at different wrinkle locations.

Lanitis et al. [20] proposed an age estimation method using a quadratic ageing function to identify the relationship between age and appearance parameters. Using weighted appearance specific (WAS), the ageing function for the

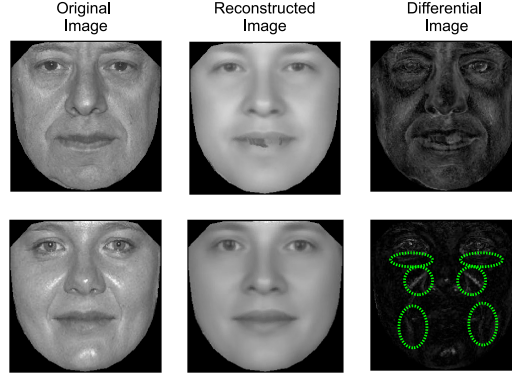


Figure 1: A comparison between original and reconstructed face images of FAM. The top row is a male subject of 60 years old and the bottom row is a female subject of 30 years old taken from FERET dataset. The reconstructed images removed the noise as well as the wrinkles (dotted green line).

90 unseen face is predicted by the weighted sum of the known ageing functions, where the weights are determined by the Mahalanobis distance from the test image to the training images. Later, they proposed three hierarchical architectures to further improve their ageing function. Among them, the function of appearance age-specific (AAS) achieved the best performance because it handles
 95 the face image clusters separately according to both the appearance and the age group. They managed to achieve the mean absolute errors (MAE) of 8.06 and 14.83 using WAS and AAS, respectively [21]. However, the ageing function does not take into consideration the uniqueness of ageing variation such as temporal, communal, personalized characteristics of human ageing.

100 Geng et al. [2] proposed an idea known as ageing pattern subspace (AGES) which makes use of FAM parameters. The main idea of AGES is to find the missing pattern in the ageing subspace by using PCA and Expectation Maximization (EM) method. They argued that the concepts of identity and time are naturally integrated into the facial ageing subspace. However, the AGES method is less
 105 representative due to the appearance model only encoding the image intensities without considering other ageing characteristics such as wrinkles. Moreover, the use of PCA on appearance parameters might lose significant features be-

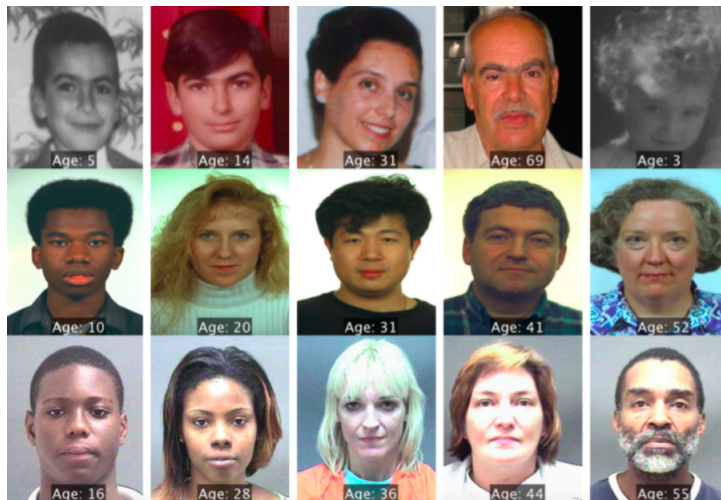


Figure 2: Sample images from the benchmark datasets with the age labelled. The first row shows the face images from FG-NET [22]. The second row shows the images from FERET [23]. The third row shows the images from MORPH [24].

cause the least important variance could be either noise or ageing information. Among recent approaches, the best MAE for FG-NET, using a leave one person out (LOPO) approach was 4.25 by Chao et al. [5]. They applied label-sensitive learning and age-oriented learning to capture the complicated appearance parameters for age estimation. They claimed that the intrinsic ordinal relationship among human ages is considered but the fundamental problem is the FAM parameters. Although the FAM-based features provide sufficient information for detailed age estimation, they do not include a comprehensive characterization of wrinkles or quantifiable wrinkles due to the dimensionality reduction in PCA [10]. Fig. 1 illustrates the wrinkles appeared on the original images but not on the reconstructed images.

2.2. Face Datasets

The popular datasets for age estimation include FG-NET [22] (with an average resolution of approximately 500x400), FERET [23] (with resolution of 512x768) and MORPH [24] (with resolution of 200x240 or 400x480). FG-NET

comprises 1002 images of 82 subjects in the age range of 0-69 years. Since the images were retrieved from real-life albums of different subjects, the face images have a lot of variations in terms of illuminations and pose. FERET is a comprehensive dataset with 2366 images of 994 subjects that presents multiple problems related to face recognition such as illumination variations, pose variations, and facial expressions. Moreover, it consists of a few hundred age-separated face images of subjects with the age difference of 18 months or more and the age range is between 10 and 70. MORPH is the most recent dataset and it was collected by the Face Ageing Group at the University of North Carolina at Wilmington for the purpose of face biometrics applications. For this experiment, 2000 images are randomly selected to validate the performance. Fig. 2 illustrates some sample images from FG-NET, FERET and MORPH datasets with different age, gender and ethnicity.

2.3. *Wrinkles Pattern*

The skin changes associated with ageing are the focus of many surgical and non-surgical procedures aimed to improve the appearance of skin [25]. Knowledge of skin histology will deepen the understanding of cutaneous changes associated with ageing and will promote optimal cosmetic and functional patient outcomes. Due to these reasons, research into age estimation by using local features has gained increasing attention, e.g., bio-inspired features (BIF) [26], kernel-based local binary patterns (KLBP) [27] and wrinkles [19].

As mentioned in [9, 28], wrinkle-based features such as skin texture are more effective for face representation because they inherently contains spatial locality and orientation selectivity. These properties allow for simplicity of feature extraction and avoid the extensive modelling of FAM. Aznar-Casanova et al. [15] investigated the influence of wrinkles on face age judgements. Their experiments were based on the types of wrinkles and quantitative contribution of wrinkles. They found that the amount of wrinkles on the perceived face age had more in-

fluence than the types of wrinkles. Although their works sounds interesting, the whole experiment is based on human judgement. [29] proposed a combination
155 rule of the facial ratios and wrinkle index for age group classification. These criteria were suggested by craniofacial research and the observation that aging skin develops wrinkles. A snakelet is a small snake segment designed to find a small individual curve segment in an image. A wrinkle geography map drops multiple snakelets in polygonal regions, where wrinkles may typically be found.
160 Their focus is concentrated on the wrinkles on forehead, next to the eyes and near the cheek bones. If several curves are found in a particular region, they claimed that wrinkles exist in that region. However, there are at least two problems need to be addressed. First, there was no objective validation against the extracted wrinkles. Lines found by the snakelet could be wrinkles or noises. Second, facial alignment was not done automatically. Wrinkle geography map was
165 placed manually for dropping the snakelets. [30] investigated the appearance-age features for age estimation. The features are wrinkle, freckle, shape, hair and colour where these features are distributed at different parts of face such as forehead, eye corners, eye bags, nasalobial. Published computerised approaches
170 on age estimation based on wrinkle features are limited [31, 32, 33, 34, 35]. Most of them were focused on age group classification instead of specific age estimation.

Yang and Ai [36] applied local binary pattern histograms (LBPH) as aging descriptors. Given a restricted local patch, the Chi square distance between the
175 extracted LBPH and a reference histogram is used as a measure of confidence belonging to the reference class. They claimed that the error rate of age classification is as low as 7.88% on the FERET dataset. However, LBPH is weakened by the sparse nature of local binary pattern (LBP) representation [27]. The current state-of-the-art method, kernel-based local binary patterns (KLBP), is
180 proposed by Ylioinas et al. [27]. It generates sign and magnitude features through face patches. They claimed that the sparse nature of LBP representation is improved by the proposed kernel estimator. However, this method is not yet tested on FERET dataset. Günay and Nabiye [37] proposed age estimation

based on local Radon features. The idea is to transform an image pixel into an
 185 equivalent geometric Radon vector. The authors reported the performance of
 the local Radon features is better on FG-NET (6.18) than FERET (6.98). It
 is a norm that local method requires image with higher resolution, but local
 Radon features seems to work better on images with lower resolution. Existing
 methods on wrinkles patterns for age estimation are limited, with low accuracy
 190 and not tested across different datasets.

In this work, we introduce a new complementary feature pattern, MWP,
 to overcome the problem of poor representation of wrinkles information in the
 state of the art. We explore the performance of MWP on face age estimation
 and subsequently proposed a new feature pattern, HAP, by combining MWP
 195 and FAM [2] to form a stronger feature representation. To date, no studies have
 investigated the use of wrinkles patterns as complementary feature of FAM in
 face age estimation.

3. MULTI-SCALE WRINKLE PATTERNS

Fig. 3 is an overview of our proposed multi-scale wrinkle patterns. It consists
 200 of four steps: seeding, wrinkles detection using line tracking, Region of Interests
 (ROI) masking and wrinkle pattern representation.

3.1. Seeding

Given a warped image I , it is scaled with different ratios s and denoted
 as $I(s)$ where $s \in \{s_1, s_2, \dots, s_\alpha\}$ with α indicates the total number of scales.
 205 Since wrinkles present in different sizes, a multi-scale image preserve different
 types of wrinkles. In this case, we set $\alpha = 4$ and $s \in \{1.00, 0.75, 0.50, 0.25\}$
 where $s = 1.00$ represents the original image scale and $s = 0.50$ represents half
 of the original image scale. For each scale, the directional gradient $\left(\frac{\partial I}{\partial x}, \frac{\partial I}{\partial y}\right)$
 of I is computed from the greyscale image. Let $\frac{\partial I}{\partial y}$ denoted as \mathcal{I} , therefore \mathcal{I}
 210 emphasizes a horizontal variation and is used as the input for calculating the
 Hessian filter \mathcal{H} . In order to determine the local likelihood that a wrinkle is

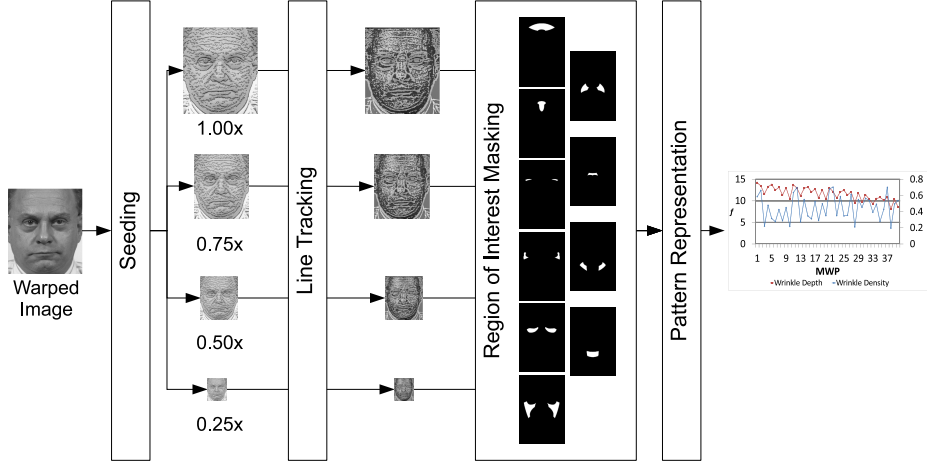


Figure 3: Multi-scale Wrinkle Patterns. It consists of four steps: seeding, line tracking, ROI masking and pattern representation. Note that 1.00x means the original size of FERET image and ten regions of masking are forehead, glabella, upper eyelids, crows feet, lower eyelids, cheeks, nasolabial grooves, upper lips, marionette and lower lips.

present, eigenvalue analysis of the Hessian filter is assessed. Wrinkles can be considered as edges with special curvatures on a face and the major orientations of such edges are in the horizontal direction. We propose the following Hessian
 215 filter imposed on the horizontal gradient \mathcal{I} at location (x, y) ,

$$\mathcal{H}_\sigma(x, y) = \begin{bmatrix} \mathcal{H}_{a,\sigma}(x, y) & \mathcal{H}_{b,\sigma}(x, y) \\ \mathcal{H}_{b,\sigma}(x, y) & \mathcal{H}_{c,\sigma}(x, y) \end{bmatrix} \quad (1)$$

where σ is the filter scale; $H_{a,\sigma}$, $H_{b,\sigma}$ and $H_{c,\sigma}$ are the second derivatives of \mathcal{I} along horizontal, diagonal and vertical directions, respectively. The parameter σ is set to four where $\sigma \in \{1, 3, 5, 7\}$ to extract the wrinkles from four different filter scales. The computation of $H_{a,\sigma}$, $H_{b,\sigma}$ and $H_{c,\sigma}$ are approximated by the
 220 following convolutions with Gaussian kernels:

$$\mathcal{H}_{a,\sigma}(x, y) = \mathcal{I}(x, y) * \mathcal{G}_{1,\sigma}(i, j) \quad (2)$$

$$\mathcal{H}_{b,\sigma}(x, y) = \mathcal{I}(x, y) * \mathcal{G}_{2,\sigma}(i, j) \quad (3)$$

$$\mathcal{H}_{c,\sigma}(x, y) = \mathcal{I}(x, y) * \mathcal{G}_{1,\sigma}^T(i, j) \quad (4)$$

The second derivative of a Gaussian kernel at filter scale σ generates a probe kernel that measures the contrast at the selective scale in the direction of the derivative. They are given by

$$\mathcal{G}_{1,\sigma}(i, j) = \frac{1}{2\pi\sigma^4} \left[\frac{\mathcal{M}_{i,j}^2}{\sigma^2} - 1 \right] e^{\frac{-\mathcal{M}_{i,j}^2 + \mathcal{N}_{i,j}^2}{2\sigma^2}} \quad (5)$$

$$\mathcal{G}_{2,\sigma}(i, j) = \frac{1}{2\pi\sigma^6} [\mathcal{M}_{i,j}\mathcal{N}_{i,j}] e^{\frac{-\mathcal{M}_{i,j}^2 + \mathcal{N}_{i,j}^2}{2\sigma^2}} \quad (6)$$

where \mathcal{M} and \mathcal{N} are the matrices with vertical and horizontal directions as

$$\mathcal{M}_{i,j} = -3\sigma + i - 1 \quad (7)$$

$$\mathcal{N}_{i,j} = -3\sigma + j - 1 \quad (8)$$

225 where the range of i and j is $[-3\sigma, 3\sigma]$. Since wrinkles are similar to the patterns of ridge and valley, the Gaussian kernels are designed in the same way. To determine the texture orientation, eigenvalues λ_1 and λ_2 of the Hessian at specific scale are given by

$$\lambda_{1,\sigma} = \frac{1}{2} \left[\mathcal{H}_{a,\sigma} + \mathcal{H}_{c,\sigma} + \left(\sqrt{(\mathcal{H}_{a,\sigma} - \mathcal{H}_{c,\sigma})^2 + 4\mathcal{H}_{b,\sigma}^2} \right) \right] \quad (9)$$

$$\lambda_{2,\sigma} = \frac{1}{2} \left[\mathcal{H}_{a,\sigma} + \mathcal{H}_{c,\sigma} - \left(\sqrt{(\mathcal{H}_{a,\sigma} - \mathcal{H}_{c,\sigma})^2 + 4\mathcal{H}_{b,\sigma}^2} \right) \right] \quad (10)$$

$\lambda_{1,\sigma}$ and $\lambda_{2,\sigma}$ are used to compute the curvilinear likeness measure \mathcal{E} [38], where
230 it is a value corresponding to how much a pixel looks like part of a curve, which is defined as the following:

$$\mathcal{E}_\sigma = \begin{cases} 0 & \text{if } \lambda_{2,\sigma} \leq 0 \\ e^{-\frac{\mathcal{R}_\sigma}{2\beta_1^2}} \left(1 - e^{-\frac{\mathcal{S}_\sigma}{2\beta_2^2}} \right), & \text{otherwise} \end{cases} \quad (11)$$

where β_1 controls the sensitivity of the filter to the measurement of \mathcal{R} and the default value is 0.5; β_2 depends on the greyscale range of the curvilinear pattern of interest and controls the sensitivity of the filter to the measurement of \mathcal{S} and the default value is 15 [38]; \mathcal{R} and \mathcal{S} are defined as:

$$\mathcal{R}_\sigma = \left(\frac{\lambda_{1,\sigma}}{\lambda_{2,\sigma}} \right)^2, \lambda_{2,\sigma} \neq 0 \quad (12)$$

$$\mathcal{S}_\sigma = \lambda_{1,\sigma}^2 + \lambda_{2,\sigma}^2 \quad (13)$$

In this work, we are interested in ridge patterns which represent seeds. λ_1 and λ_2 highlight the data of interest and discard noisy patterns [38]. In all scales, if λ_2 is positive, then seeds are detected as shown in (11). Moreover, if the maximum of \mathcal{E} is greater than zero at any scales, then seeds are detected as well. Due to the curvilinear pattern being analyzed at different values of σ , the response \mathcal{E}_{\max} of the Hessian filter will be the maximum at a scale σ as

$$\mathcal{E}_{\max}(x, y) = \max_{\sigma} [\mathcal{E}_{\sigma}(x, y)] \quad (14)$$

An initial seed mask of MWP (as \mathcal{D} , respectively) is generated and it is defined as

$$\mathcal{D}(x, y) = \begin{cases} 0 & \text{if } \mathcal{E}_{\max}(x, y) \leq 0 \\ I(x, y) & \text{otherwise} \end{cases} \quad (15)$$

3.2. Wrinkles Detection using Line Tracking

To date the best wrinkles detector is Hessian Line Tracking (HLT) [39]. This section summarises HLT algorithm and further validation of its performance on ten face regions will be presented in the results section (Section 4).

Hessian Line Tracking. Let $\mathcal{C}_{p,r}$ be denoted as a set of candidates pixels to a particular center pixel or seed $\mathcal{D}(x, y)$ where p represents the number of

250 sampling points and r is the radius of the neighbourhood. These sampling points around $\mathcal{D}(x, y)$ lie at Cartesian coordinates as,

$$(x_\theta, y_\theta) = (x + r \cos \theta, y + r \sin \theta) \quad (16)$$

where $\theta \in \{0^\circ, 180^\circ, 45^\circ, 225^\circ, 135^\circ, 315^\circ\}$ and $(x_\theta, y_\theta) \in \mathcal{C}_{p,r}$. In this work, we set $(p, r) = (6, 1)$ where tracking of vertical directions are excluded because we assume that the majority of wrinkles is horizontal. Let \vec{g}_1 denote the first
 255 background pixel located \hat{s} pixel(s) away from the candidate pixel and let \vec{g}_2 a background pixel located \hat{s} pixel(s) away from the candidate pixel but in the opposite direction. The cross-sectional profile parameter V is estimated as

$$V_{\hat{s}}(x_\theta, y_\theta) = I_{\hat{s}}(\vec{g}_1) + I_{\hat{s}}(\vec{g}_2) - \mathcal{D}(x, y) - I(x_\theta, y_\theta) \quad (17)$$

where $\hat{s} \in \{1, 2, \dots, 10\}$. If the current pixel belongs to the set of wrinkles, the cross-sectional parameter V has a large positive value. If the current pixel
 260 belongs to the background, the contrast between background pixels, current pixels and candidate pixels have similar values, thus V has a negative value or is near to zero. The winner pixel \vec{w} with maximum positive cross-sectional profile, exceeding a predefined positive threshold ς , is defined as

$$\vec{w} = \arg \max_{\mathcal{C}} \{V_{\hat{s}}(x_\theta, y_\theta) > \varsigma\} \quad (18)$$

where \vec{w} could be one of the elements of \mathcal{C} or *null* if none is larger than ς .
 265 ς is an important threshold in identifying the intensity difference between the current pixel and the candidate pixel relative to the background pixels. The default value of ς is 9, which is the best threshold we have explored for FERET dataset. If \vec{w} is not *null*, then the confidence array $\mathcal{F}(\vec{w})$ is increased by one and the next pixel to be tracked is $I(\vec{w})$. If \vec{w} is *null*, the next candidate pixel
 270 is drawn from the seeds. Note that the tracked pixel is unique from candidate pixels, otherwise the tracking will be redundant. Once multi-scale line tracking is completed for all scales \hat{s} , the initial wrinkle map \mathcal{B} is generated by consulting

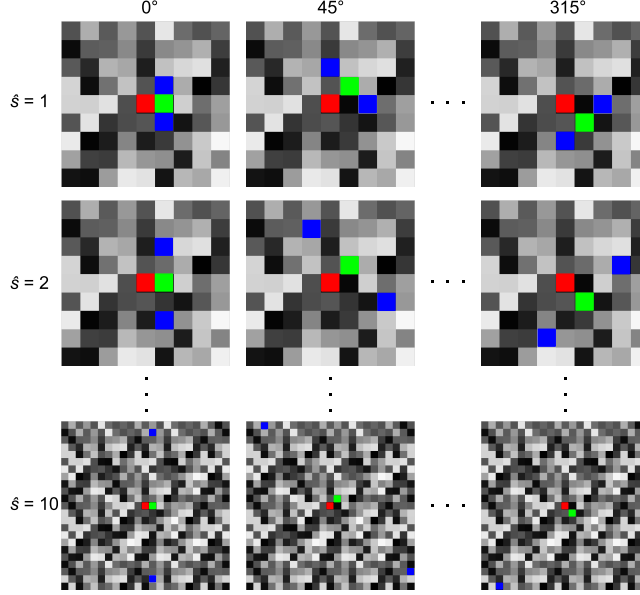


Figure 4: Line tracking. Each column shows different degrees of tracking and each row presents how the multi-scale tracking works. Red is the current seed $\mathcal{D}(x, y)$, green is the candidate pixel with certain degree $I(x_\theta, y_\theta)$ and blue is the background pixel with a particular scale $I_{\hat{s}}(\vec{g}_1), I_{\hat{s}}(\vec{g}_2)$.

the confidence array as

$$\mathcal{B}(x, y) = \begin{cases} 1 & \text{if } \mathcal{F}(x, y) \geq \xi \\ 0 & \text{otherwise} \end{cases} \quad (19)$$

where ξ is the amount of scale \hat{s} and in this work, $\xi = 10$. Note that $\vec{w}, \vec{g}_1, \vec{g}_2$ refer to a particular position (x, y) .

Fig. 4 illustrates the line tracking processes on different degrees and scales. Red is the current seed $\mathcal{D}(x, y)$, green is the candidate pixel with certain degree $I(x_\theta, y_\theta)$ and blue is the background pixel with a particular scale $I_{\hat{s}}(\vec{g}_1), I_{\hat{s}}(\vec{g}_2)$. First, a seed is drawn from \mathcal{D} . Then, candidate pixels \mathcal{C} and background pixels \vec{g}_1, \vec{g}_2 are derived from it with $\hat{s} = 1$ and $\theta = 0^\circ$. Cross-sectional profile $V_{\hat{s}}(x_\theta, y_\theta)$ is computed as (17). After that, the computation is repeated for different degrees in order to determine the winner pixel \vec{w} . The confidence array

\mathcal{F} is incremented by one if a winner pixel is found. Next, the tracking continues with either winner pixel or a seed drawn from \mathcal{D} . Once the tracking is completed for the whole image, \hat{s} is increased to the next scale and the calculation continues until the last scale. Finally, the initial wrinkle map \mathcal{B} is generated by validating the confidence array \mathcal{F} as (19).

3.3. ROI Masking

In order to extract the wrinkle from a specific region, a standard template first introduced in Ng et. al. [19] is utilised to normalise the face. A mean face from each dataset is used to register and standardise the template. To identify the facial landmarks, the center of eyes and mouth of each face image are derived from the Face++ detector[40]. Once the landmarks are identified, a linear transformation is determined between face image and template through the Procrustes analysis [41]. Then, a warped image is generated by an affine geometric transformation. Due to the limitations of the Face++ detector, we observed a small number of detection errors which were identified and corrected manually. Fig. 3 illustrates the warped image and ten predefined regions of interest. The regions are forehead, glabella, upper eyelids, crows feet (or eye corners), lower eyelids (or eyebag), cheeks, nasolabial grooves (or nasolabial folds), upper lips, marionette and lower lips. The ten face regions are binary images represented by \mathcal{Z}_i where $i = 1, 2, 3, \dots, \gamma$ and $\gamma = 10$. Note that the template size is 512 x 768 pixels. With consistent area size for the ten face regions, all regions are used to construct the wrinkle patterns, which produce a standard feature vector subsequently used for training and testing. From the wrinkle map \mathcal{B} and region of interest \mathcal{Z}_i , the wrinkle image \mathcal{J}_i is defined as

$$\mathcal{J}_i(x, y) = \begin{cases} I(x, y) & \text{if } \mathcal{B}(x, y) \cap \mathcal{Z}_i(x, y) = 1 \\ 0 & \text{otherwise} \end{cases} \quad (20)$$

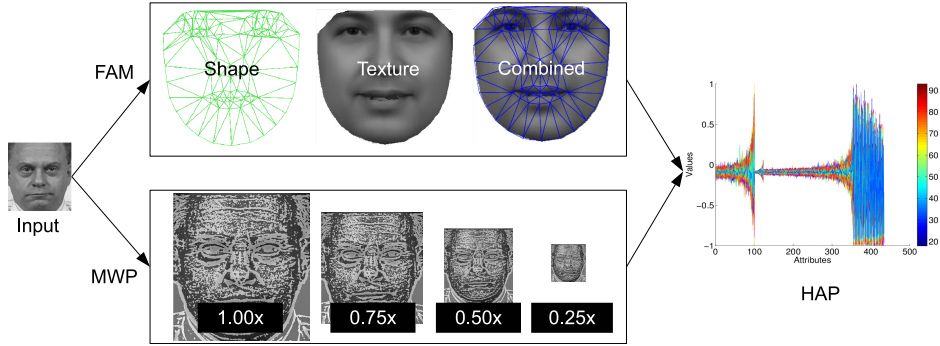


Figure 6: An illustration of HAP patterns. The graph of HAP demonstrates the normalised feature values and the colour bar shows the actual age of each instance. There are approximately 500 instances and 435 features used for this illustration. 1.00x means the original size of input and 0.50x shows the half size of input, and so on. Note that the original input image is taken from FERET dataset.

density are generated after wrinkle detection.

4. HYBRID AGEING PATTERNS

Chen et al. [42] explored the facial feature fusion and model selection for age estimation. They found that the feature fusion with model selection can achieve significant improvement for age estimation over single feature representation. However, their results were only tested on FAM and LBP. LBP is a texture descriptor but not designed for facial wrinkle. Therefore, an expansion to the similar idea but a better feature representation is proposed to overcome the limitation. Here we propose a new hybrid feature representation, HAP, a fusion of FAM and MWP for face age estimation. FAM is capable of representing the face appearance in a set of hidden parameters while MWP produces facial wrinkles pattern as complementary feature to FAM.

FAM is a generative parametric model that consists of shape, texture and combined appearance of a human face. It is a model where PCA is used to project high dimension of face shapes and textures into a low dimension of principal component parameters. Automatic detected landmarks by FACE++ detector [40] were used to produce a FAM model. The pertinent equations of

FAM [1] are repeated here for convenience. Let \mathbf{s} and \mathbf{t} denote a synthesized shape and texture of a face image in the reference frame, and let $\bar{\mathbf{s}}$ and $\bar{\mathbf{t}}$ denote the corresponding sample means. New instances are now generated by adjusting
 335 the principal component scores, \mathbf{b}_s and \mathbf{b}_t in

$$\mathbf{s} = \bar{\mathbf{s}} + \Phi_s \mathbf{b}_s \quad (23)$$

$$\mathbf{t} = \bar{\mathbf{t}} + \Phi_t \mathbf{b}_t \quad (24)$$

where Φ_s and Φ_t are matrices of column eigenvectors of the shape and texture dispersions estimated from the training set. To obtain a combined shape and texture parameterisation, \mathbf{c} , the values of \mathbf{b}_s and \mathbf{b}_t over the training set are combined into

$$\mathbf{b} = \begin{bmatrix} \mathbf{W}_s \mathbf{b}_s \\ \mathbf{b}_t \end{bmatrix} = \begin{bmatrix} \mathbf{W}_s \Phi_s^T (\mathbf{s} - \bar{\mathbf{s}}) \\ \Phi_t^T (\mathbf{t} - \bar{\mathbf{t}}) \end{bmatrix} \quad (25)$$

340 A suitable weighting between pixel distances and pixel intensities is carried out through the diagonal matrix \mathbf{W}_s . To make the normalised measures of pixel distance and pixel intensities commensurate, the shape model scores are typically weighted by the square root of the ratio between the sums of the texture and shape eigenvalues.

345 To recover any correlation between shape and texture, the two eigen-spaces are usually coupled through a third principal component transform as

$$\mathbf{b} = \Phi_c \mathbf{c} = \begin{bmatrix} \Phi_{c,s} \\ \Phi_{c,t} \end{bmatrix} \mathbf{c} \quad (26)$$

and \mathbf{b} is the FAM features of each image as $\text{FAM} = \{b_1, b_2, \dots, b_n\}$ where $b_i \in \mathbf{b}$ and n is the total number of FAM features of each image.

Fig. 6 shows an illustration of HAP patterns. First, the features of a warped
 350 image (input) are extracted by FAM and MWP. Then, a hybrid pattern is constructed from FAM and MWP as HAP. HAP of each image is defined as

HAP = $\{b_1, b_2, \dots, b_n, d_1, d_2, \dots, d_m\}$ where $b_i \in \text{FAM}$, $d_i \in \text{MWP}$ and $m + n$ is the total number of HAP features of each image.

5. SUPPORT VECTOR REGRESSION

355 According to Guo et al. [7], the linear regression cannot model the complex aging process. Therefore, a non-linear regression function may be required in practice to adequately model the data. It can be obtained using kernels such as polynomial, Gaussian radial basis function (RBF) and universal Pearson VII function based kernels (PUK). A kernel method is an algorithm that depends on
 360 the data only through dot-products [43]. It is replaced by the kernel functions which calculate the variations in a high dimensional space. Therefore, it extends the ability of a linear classifier to generate non-linear decision boundaries and apply a classifier to data that have no obvious fixed-dimensional vector space representation, for example, data in bio-informatics and signal processing.

365 SMO is an iterative algorithm for solving the optimization problem by operating on a fixed size subset of the training set at a time. SMO breaks this problem into a series of smallest possible sub-problems, which are then solved analytically [44]. SMO algorithm puts chunking to the extreme by iteratively selecting working sets of size two and optimizing the target function with respect to them. One advantage of using working sets of size two is that the
 370 optimization sub-problem can be solved analytically.

In this work, we implemented age estimation experiments by using the WEKA toolbox [45]. The regression algorithm is support vector regression (SVR) with SMO and PUK kernel [46] and parameters are detected through
 375 grid search. Let $\vec{x}, \vec{y} \in \mathbb{R}^N$ denote input vectors of SVR, the PUK kernel κ is defined by,

$$\kappa(\vec{x}_i, \vec{y}_i) = \frac{1}{\left[1 + \left(2\sqrt{|\vec{x}_i - \vec{y}_i|^2} \sqrt{2^{(1/\omega)} - 1}/\tilde{\sigma}\right)^2\right]^\omega} \quad (27)$$

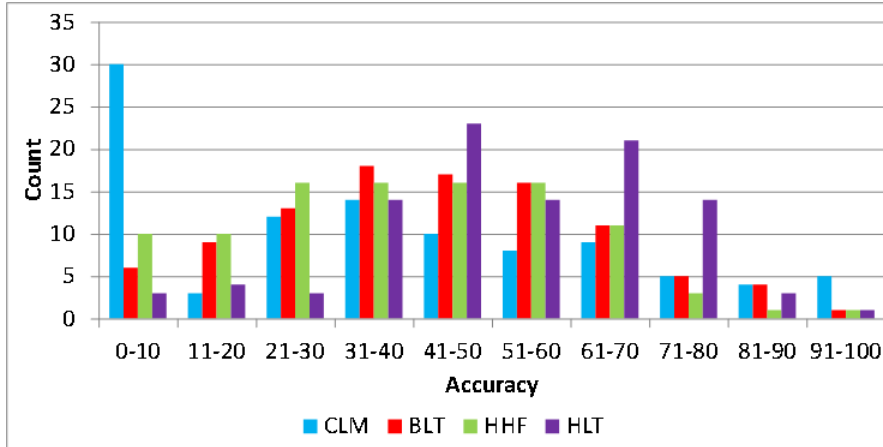


Figure 7: Wrinkle detection accuracy on 100 FERET forehead images. Overall, HLT achieved accuracy of 76% while CLM, BLT and HHF only hit 41%, 54% and 48%, respectively.

where the parameters ω and $\tilde{\sigma}$ control the half-width and the tailing factor of the peak of the Pearson VII function. In this way, the PUK kernel will lead to a symmetric matrix with ones on the diagonal and all other entries ranging between the values 0 and 1 for any arbitrary pair of (\vec{x}_i, \vec{y}_i) . The PUK kernel is robust and has an equal or even stronger mapping power as compared to the standard kernel functions, which leads to an equal or better generalization performance of SMO [47].

6. EXPERIMENTAL RESULTS AND DISCUSSION

The experimental results are organised into two parts: First part justifies the choice of wrinkle detection algorithm; Second part assesses the performance of MWP and HAP for face age estimation.

6.1. Automatic Wrinkle Detection

To validate the wrinkle detection algorithm, we follow the protocol of recently published papers [14, 39]. The wrinkle detection method was validated on Bosphorus forehead dataset [39]. To test the reliability of HLT, we first eval-

uate its performance on FERET forehead dataset and then on the other nine face regions.

6.1.1. Evaluation on FERET Forehead Dataset

395 A subset of 100 images of FERET is randomly selected and the wrinkles are manually annotated. We compare the performance of four most recent wrinkle detection algorithms - Cula Method (CLM) [48], Hybrid Hessian Filter (HHF) [14], Batool line tracking (BLT) [49] and HLT [39] to the manual annotation using Jaccard Similarity Index (JSI) [50]. The Jaccard index, 400 $J(A, B) = |A \cap B| / |A \cup B|$, where A and B denote the set of pixels in two different coders' annotations. In order to validate the correctness of the wrinkle detection method, accuracy is defined as $accuracy = \sum_{i=1}^N w_i$, where N is the total number of images in the experiment and w is the logical output of J ; $w_i = 1$ if $J_i > 40\%$, otherwise $w_i = 0$. Any overlap between A and B larger 405 or equal to 40% is considered as correct detection [51]. For detailed protocol of wrinkle detector evaluation, please refer Ng et al. [14]. Fig. 7 shows the accuracy of wrinkle detection. In 100 images, results showed that HLT achieves better than others with an accuracy of 76%, where CLM is 41%, BLT is 54% and HHF is 48%, with an STD of 15.20%, 12.28%, 5.98 and 0.46%.

410 6.1.2. Evaluation on Other Face Regions

From the 90 images randomly selected from FERET dataset, we cropped each image using the predefined region of interest with 10 images for each region. The ground truths are annotated by a dermatologist, as illustrated in Fig. 8.

Fig. 9 shows the average JSI of wrinkle detection for each face region. The 415 experimental results showed that BLT hits the best result on Nasalobial and HLT outperforms others in all the remaining regions. The average JSI of all regions for CLM, BLT, HHF and HLT is 35.10%, 42.69%, 38.01% and 52.10%. This experiment further validate Ng et al. method [39] and proved that HLT performed better than the state-of-the-art wrinkle detector. Hence, it is used 420 to extract the wrinkles in MWP.

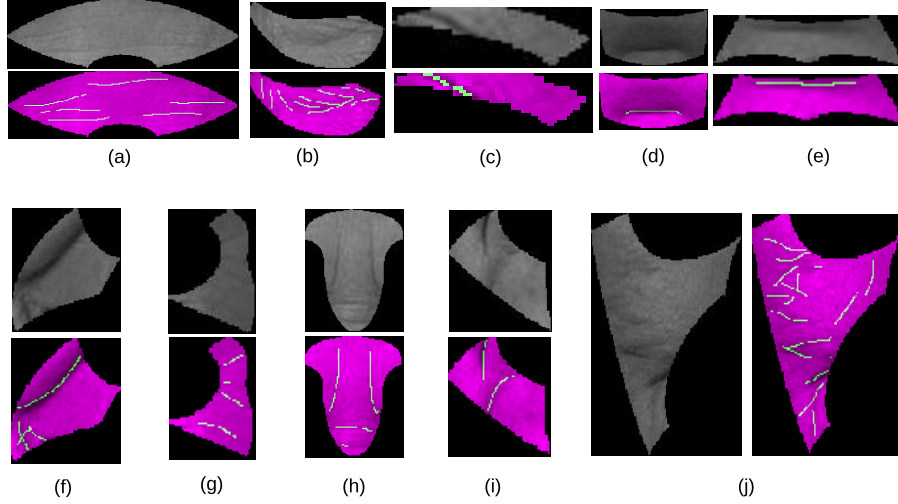


Figure 8: Manual annotation on ten face regions: (a) forehead, (b) lower eyelids, (c) upper eyelids, (d) lower lips, (e) upper lips, (f) nasalobial, (g) crows feet, (h) glabella, (i) marionette and (j) cheeks. Ground truths are green lines and these images are resized for better illustration.

6.2. Face Age Estimation

The most commonly used performance metric for age estimation is Mean Absolute Error (MAE) [2]. The MAE is defined as the average of the absolute errors between estimated age and the ground truth, $MAE = \sum_{k=1}^N (|\hat{l}_k - l_k| / N)$, where l_k is the ground truth age for the k -th test image, \hat{l}_k is the estimated age, and N is the total number of test images.

Table 1 shows a comparison of the performance of the proposed method and the state of the art on three datasets. Although the MAE of MWP is the highest among the descriptors (FAM, BIF, KLBP and MWP), it required less computation times (training and prediction) than others under the same environment. When running the algorithms on FERET dataset, the computation times (feature dimension) of FAM, BIF, KLBP and MWP are 83.99 seconds (300 units), 1892.69 seconds (7464 units), 6352.59 seconds (32769 units) and 36.74 seconds (160 units), respectively.

We noticed that HAP has the lowest MAE for FERET and MORPH, but

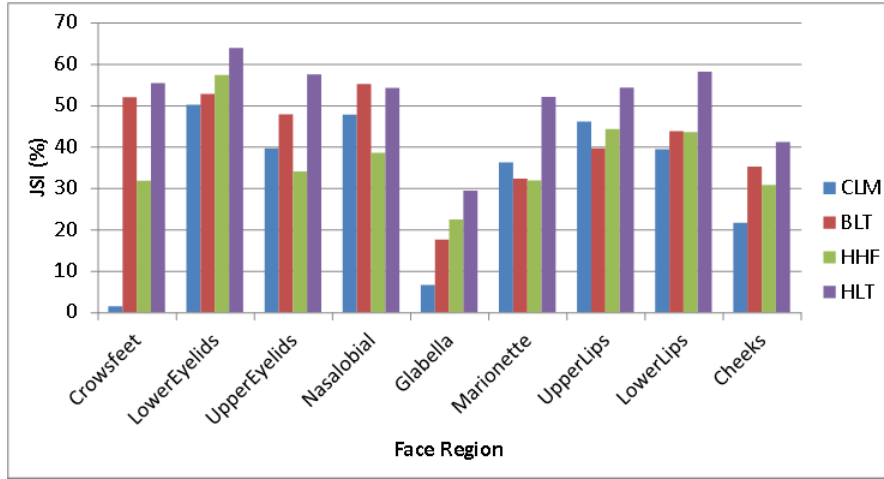


Figure 9: Average accuracy (JSI) of wrinkle detection for the other nine face regions.

not for FG-NET. The results showed that the fusion of MWP as complementary features for FAM outperformed on FERET and MORPH, but not FG-NET. This is due to the images in FG-NET were retrieved from real-life albums, which included variation in illumination, pose, expression, beards, moustaches and spectacles. In addition, some of the scanned images are not clear and do not have sufficient texture information.

In Appendix A, Table 2 shows a comprehensive age group analysis of face age estimation from Table 1. For FGNET and FERET, ages are divided into five groups where $age_1 = 15$, $age_2 = 35$, $age_3 = 45$ and $age_4 = 55$; for MORPH, $age_1 = 18$, $age_2 = 28$, $age_3 = 38$ and $age_4 = 48$. These parameters were determined based on the age range of dataset. From these results, we noticed that the errors of each method are very similar from one group to another group. It could be the same noise extracted from the same group images. However, we observed that HAP performed better than MWP in all age groups. This implies that FAM features combined with MWP greatly improve the performance of face age estimation.

With the advancements of technology and camera resolution, we believe that MWP can be used as a complementary features for FAM in face age estimation.

Table 1: Comparison of MAE results on three popular datasets. Bold indicates the best MAE of age estimation for each dataset.

Dataset	FG-NET[22]	FERET[23]	MORPH[24]
Total images	1002	2366	2000
FAM [1]	5.39 (± 5.63)	3.34 (± 3.26)	3.99 (± 3.28)
BIF [26]	5.59 (± 5.59)	3.57 (± 3.26)	3.98 (± 3.20)
KLBP [27]	6.09 (± 6.09)	3.91 (± 3.25)	4.02 (± 3.22)
MWP	7.34 (± 7.54)	4.16 (± 3.83)	5.16 (± 4.35)
HAP	5.66 (± 5.88)	3.02 (± 2.92)	3.68 (± 2.98)

With better representation of wrinkles descriptor using MWP, the fusion of FAM
 455 and MWP has formed a new feature pattern, HAP, for face age estimation.

6.3. Discussion

The idea of this work is based on the intensity distribution of facial wrinkles on the predefined wrinkle regions. It is useful to identify a simple yet powerful pattern from wrinkles. However, we noted three issues that affect the perfor-
 460 mance of our proposed method MWP. First is the mask of wrinkle regions. Although this has been set to the size of mask using a mean face, we noticed that some of the face cannot fit the mask very well due to large variations of cranial ratio and occlusions such as forehead hair and moustaches. Second, there are false detections of landmarks in a few images detected by the Face++
 465 detector. Although majority were identified and corrected manually, there are some cases with minor errors in alignment. Finally, a robust wrinkle-based features is highly dependent on the performance of wrinkle detection method. With further improvement of the line tracking algorithm, the wrinkle patterns are better represented.

470 Moreover, the appearance of wrinkle is affected by other factors such as facial expressions and cosmetic treatment. Wrinkles are highly associated with facial expression. It is worth investigating the expression effect on wrinkle and how it would affect the performance of age estimation. Even though wrinkles

are highly associated with aging, we observed individual differences that some
475 individuals have less wrinkles than others. Therefore, an extensive analysis with
additional aging features are necessary to address such limitation in the context
of age estimation.

While achieving good performance on face age estimation, wrinkle-based
patterns would also be useful for broader applications. Generally speaking,
480 there are at least three scenarios where wrinkle-based patterns could be helpful:

1. The potential use of wrinkles in the soft biometric applications, e.g. face
verification in the presence of age progression [52, 9, 5, 53]. Aging variation
poses a serious problem to automatic face recognition systems. As the
demand for automatic recognition and surveillance systems is increasing
485 in the last few decades, it would be interesting to explore how wrinkle-
based features could contribute to this field.
2. In cosmetology, dermatologists are interested in locating and removing
face wrinkles in order to achieve skin rejuvenation [48, 11]. Currently,
most systems require expert intervention to manually locate and iden-
490 tify wrinkles. Such process is time-consuming and prone to human error.
Therefore, an automatic wrinkle quantification system will aid to human
decision in cosmetology.
3. For any facial applications such as face recognition [9, 54], facial expression
recognition [55, 56], age estimation or synthesis [17, 18, 57], it is interesting
495 to render or interpret face images in terms of facial attributes. FAM is well
known in capturing distinct patterns emerging from the facial appearance.
However, the validity of FAM projection in age progression is in fact highly
doubtful due to the dimensionality reduction by PCA. Therefore, this
problem can be alleviated by the use of local-based wrinkle patterns.

500 In this paper, an investigation of wrinkle-based feature representation for
face age estimation is a typical example of scenario 3. Further analysis of
wrinkle-based patterns in the aforementioned three scenarios will open the door
for promising future research.

7. CONCLUSION

505 This paper investigated the use of wrinkles pattern as complementary features for FAM. First, we proposed a novel method (MWP) based on multi-scale wrinkle patterns to improve the wrinkles representation. By deriving wrinkles with the multi-scale filters across ten face regions, wrinkle patterns are extracted. Then, HAP is proposed for face age estimation. HAP is a fusion
510 of MWP and FAM, which is used to train the classifier and then predict the age of faces. The performance of HAP are assessed and validated using three popular datasets - FG-NET, FERET and MORPH. The results showed HAP (FAM+MWP) outperforms the state of the art with a MAE of 3.02 (± 2.92) on FERET and 3.68 (± 2.98) on MORPH. The MAE of HAP on FG-NET is slightly
515 higher but comparable to FAM. We conclude that using wrinkle as complementary features could improve the performance of FAM in face age estimation.

The methods proposed and experiments presented in this paper have significant impact on wrinkle representation and the design of face age estimation. The results in this study will motivate the research in using automated wrinkle
520 representation for soft biometric studies and face age estimation. Future work will focus on improving the accuracy of wrinkles detection, the impact of vertical wrinkle lines on face age estimation and the implication of automated wrinkles detector in soft biometric.

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Appendix A

Table 2: An extended results of Table 1. **Bold** - the lowest MAE within one particular dataset and the underlined values present the highest and lowest of MAE of age group of each dataset.

Dataset (number of images)	MAE (STD)				
	FAM	BIF	KLBP	MWP	HAP
FGNET (1002)	5.39 (5.63)	5.59 (5.97)	6.09 (6.43)	7.34 (7.54)	5.66 (5.88)
$y_i < age_1$ (545)	<u>3.79 (3.42)</u>	3.80 (3.29)	4.17 (3.36)	4.84 (4.09)	3.88 (3.48)
$age_1 \leq y_i < age_2$ (355)	4.94 (3.84)	5.05 (3.93)	5.18 (4.25)	6.62 (5.02)	5.41 (4.13)
$age_2 \leq y_i < age_3$ (61)	10.76 (5.52)	11.92 (6.10)	14.34 (4.90)	17.76 (5.48)	10.89 (5.52)
$age_3 \leq y_i < age_4$ (30)	19.73 (7.39)	21.90 (7.01)	25.27 (6.90)	28.52 (7.40)	21.29 (8.67)
$age_4 \leq y_i$ (11)	30.15 (7.75)	32.22 (7.93)	32.74 (8.88)	<u>38.77 (10.00)</u>	30.03 (8.08)
FERET (2366)	3.34 (3.26)	3.57 (3.26)	3.91 (3.24)	4.16 (3.83)	3.02 (2.92)
$y_i < age_1$ (38)	8.98 (4.09)	<u>9.82 (3.44)</u>	8.64 (4.20)	9.30 (5.18)	7.69 (4.07)
$age_1 \leq y_i < age_2$ (1579)	2.86 (2.67)	3.04 (2.72)	3.44 (2.76)	3.76 (3.40)	2.68 (2.55)
$age_2 \leq y_i < age_3$ (474)	2.99 (2.54)	3.58 (2.98)	3.92 (3.18)	4.01 (3.59)	<u>2.77 (2.30)</u>
$age_3 \leq y_i < age_4$ (209)	4.72 (3.61)	4.82 (3.81)	4.94 (3.65)	5.00 (4.17)	3.94 (3.40)
$age_4 \leq y_i$ (66)	9.54 (6.74)	8.37 (5.52)	9.14 (4.70)	9.33 (6.34)	7.37 (5.48)
MORPH (2000)	3.99 (3.28)	3.98 (3.20)	4.02 (3.22)	5.16 (4.35)	3.68 (2.98)
$y_i < age_1$ (100)	6.74 (5.21)	5.80 (4.58)	6.67 (4.04)	<u>10.93 (6.59)</u>	6.25 (5.18)
$age_1 \leq y_i < age_2$ (500)	3.91 (3.03)	3.99 (2.96)	3.93 (2.92)	4.93 (4.19)	3.46 (2.68)
$age_2 \leq y_i < age_3$ (500)	3.44 (2.87)	3.47 (2.72)	<u>3.19 (2.50)</u>	4.53 (3.42)	3.30 (2.62)
$age_3 \leq y_i < age_4$ (500)	3.65 (2.91)	3.88 (3.07)	3.96 (2.93)	4.94 (3.72)	3.45 (2.51)
$age_4 \leq y_i$ (400)	4.48 (3.48)	4.25 (3.56)	4.57 (3.97)	5.07 (4.61)	4.09 (3.24)