On the Optimization of Iterative Clipping and Filtering for PAPR Reduction in OFDM Systems

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Abstract—Orthogonal frequency division multiplexing (OFDM) offers spectral efficiency advantage, however, it is limited by peak-to-average power (PAPR) problem. The PAPR can be reduced using iterative clipping and filtering (ICF) scheme but requires that the same signals are iteratively clipped with a fixed clipping threshold at different clipping iterations. This method warrants that fast-Fourier transform (FFT)/inverse FFT (IFFT) blocks must be driven in the order of iterations many times to attain a desired PAPR threshold which expends the system power and expands processing time. Using a second-order cone program, the number of iterations required to attain the desired PAPR threshold was reduced. This optimized ICF (OICF) was later simplified using Lagrange Multiplier Optimization (LMO). In this study, we apply an adaptive clipping threshold to the LMO scheme to improve the performance of the simplified OICF (SOICF). Our results show significant reduction of the PAPR problem compared to the earlier SOICF scheme albeit with some degradation in the BER performance that can be under 1.0 dB depending on the chosen clipping threshold. In addition, we also illustrated the results of the theoretical relationships and performances between the error vector magnitude (EVM) and PAPR, between clipping ratio (CR) and EVM, and lastly the inter-dependencies of EVM, PAPR, the number of OFDM subcarriers and the CR.

Index Terms—PAPR; OFDM; optimization; iterative clipping and filtering (ICF); adaptive; Lagrange multiplier

I. INTRODUCTION

Since 1971 when it was shown that discrete Fourier transform (DFT) can be used to partition wide-bandwidths into parallel and orthogonal subcarriers [1], the use of orthogonal frequency division multiplexing (OFDM) realized from the DFT has been widely adopted in the design of modern communication systems [2]. The trend has also motivated the study of other transforms for multicarrier application such as wavelets [3]. This is due to its ability to increase throughput by multiplexing large streams of data over any constrained bandwidth by partitioning them into parallel adjacent subcarriers. By this fact, the symbol time is increased so that the system becomes robust over fading channels. One problem prevails from such architecture, for example, the subcarriers subtend non-uniform distributed peaks so that the peak-to-average power (PAPR) becomes high. Evidently, these peaks drive the power amplifiers of OFDM systems to operate near the saturation region [4].

The high power amplifier (HPA) used in base stations is responsible for the significant share of the energy costs in a communication system [5]. The energy efficiency of the HPA is directly related to the PAPR of the input signal, which is particularly important in OFDM multicarrier transmission [6]. Also as acknowledged in [6], high PAPR is the key reason why OFDM is not adopted in the uplink of mobile communication standards whilst putting constraints on the downlink coverage due to output power limitations.

There are several methods that can be used to combat this problem in the literature; these can be grouped into signal distortion techniques, multiple signaling and probabilistic techniques, and coding techniques [2]. Iterative clipping is one of the simplest widely known techniques from the amplitude distortion family for PAPR reduction technique. Its major drawback is that the deliberately clipped OFDM symbol peaks impact the noise overhead of the system and so reduces the BER of the system. Since the clipping also involves oversampling, this leads to out-of-band power emission. However, a frequency domain filtering helps to eliminate the noise and the out-of-band power; this however culminates into peak-regrowth and leads to increase in PAPR [7]. Thus, modern techniques involve iterative clipping and filtering (ICF) [2], [4], [8]–[10].

In [11], it was shown that the ICF technique expends the system resources in the order of the iterations in driving the IFFT/FFT blocks. Reducing the number of iterations to achieve a PAPR target would also reduce the device resources lost to the ICF process. In [12], authors make the assumption that the clipped peaks are assumed to be parabolic pulses. While this is true if the clipping threshold is large, this method does not work for low clipping thresholds, which is also acknowledged by the authors. In our approach, no assumption on the characteristics of the clipped peaks are made and therefore the concept is universally applicable in OFDM systems. Consequently, [4] showed a method that optimizes the process using the widely used convex optimization algorithm based on second-order cone program (SOC) solvable by the MATLAB-enabled CVX optimization software [13]. In that work, the authors referred to their solution as optimized ICF (OICF) [4]. The authors in [8] later acknowledged the OICF approach to be expensive in terms of system design due to the complexity involved in constructing an optimal filter using the CVX tool. To overcome this problem, a new optimal method that construct a PAPR-vector to minimize the error vector magnitude (EVM) was then proposed and solved by using Lagrange Multiplier optimization (LMO) [8]. The latter achieved significant reduction in the resources consumed.
during the optimization of ICF process reducing the $O(N^3)$ computations of [4] to only $O(N)$ computations.

The fundamental problem with both OICF and SOICF is that they are based on fixed clipping threshold. Earlier, the authors in [14] proposed an adaptive technique of improving the PAPR reduction limit of the conventional ICF process through some adaptive determination of near crest factor and thus new reduction limit peaks. That study significantly improved the PAPR of an iteratively clipped and filtered OFDM signal using the adaptive clipping ratio. To enhance the performance of the novel SOICF, we proposed an adaptive SOICF technique that overcomes the PAPR performance limit of the present SOICF with no additional design cost as it will be demonstrated shortly. The method we propose combines the strengths of SOICF and AICF both to improve PAPR reduction and optimally utilize the available communication device resources. Our results show an improved performance over the current SOICF technique as it will be shown in Section III. In [14], the authors applied genetic algorithm (GA) for adaptive reserved tone ICF (ART-ICF) which is computationally rigorous and expends lots of processing resources whilst increasing input-output latency as it involves an exhaustive search for adaptive step sizes. In fact, the authors in [15] showed an improved method of solving the problem by using differential evolution. Meanwhile, both the ART-ICF and the improved version all suffer from the exhaustive search problem of GA. The authors in [9] proposed the use of custom conic optimization with AICF; unfortunately, the method was based on the CVX public software [13] which consumes device power and the requires up to four iterations to obtain a good BER performance. In this study, we improve the works done by [8], [14] and [9]. It is worthy to mention here that the earliest work on the construction of optimal filter proposed by [4] which involved the construction filter using CVX was also independently similarly addressed by [16] although based on graded bandlimiting filter.

The rest of this paper are organized as follow; we formulate the problem in Section II and perform the system evaluation in Section III. The results are also discussed in Section III with the conclusion following.

II. Problem Formulation

OFDM divides a wideband into many parallel orthogonal subcarriers in the order of the DFT size used, say $N$. These orthogonal subcarriers convey data frames $D = [d_1, d_2, \cdots , d_P]$, where $d_p = [d_0, d_1, \cdots , d_{N-1}]^T \forall p = 1, 2, \cdots , P$ and $[\cdot]^T$ represents the complex conjugate of $[\cdot]$. In frequency domain these data symbols are processed using the DFT to realize $X$; for simplicity we shall consider only one frame. Thus, consider an OFDM system with some frequency domain symbols such as $X_p = [X_0, X_1, \cdots , X_{N-1}]$. The frequency domain signal of length $N$ is converted to time domain using an oversized IDFT of order $LN = L \times N$ after some oversampling. With the oversampling, for example $X = [X_0, X_1, \cdots , X_{N-1}, 0, 0, \cdots , 0_{N(L-1)}]$, its time domain equivalent can be represented as

$$x(n) = \frac{1}{\sqrt{LN}} \sum_{k=0}^{LN-1} X(k) e^{j2\pi \frac{n}{LN}} \quad \forall n = 0, 1, \cdots , LN - 1$$

(1)

where $L$ is the oversampling factor and $X(k), x(n) \in \mathbb{C}^{LN}$ with $\mathbb{C}$ representing the complex domain. This factor, $L$, follows from the fact that at Nyquist sampling rate, OFDM symbols may not demonstrate equivalent PAPR as the continuous-time signals [17], thus, the time domain signal must satisfy $L \geq 4$ [18]. Consider also that since the OFDM symbols are complex, so, the amplitude can be expressed as

$$|x(n)| = \sqrt{x_r(n)^2 + x_i(n)^2}$$

(2)

where $x_r(n)$ and $x_i(n)$ are real and imaginary parts, respectively, from $x(n) = x_r(n) + jx_i(n)$. For an OFDM system with sufficiently large subcarriers (such as $N \geq 64$), the knowledge of the central limit theorem provides that the real and imaginary parts of $x(n)$ are asymptotically independent and identical Gaussian distributed variables [19]. Put differently, the amplitudes ($|x(n)|$) can be described using the probability density function (PDF) of a Rayleigh distribution such as [19]

$$f_{|x(n)|}(x_0) = \frac{x_0}{\sigma_x^2} \exp\left(-\frac{x_0^2}{2\sigma_x^2}\right), \quad \forall n = 0, 1, \cdots , LN - 1$$

(3)

where $x_0$ is the discrete-time envelope of $x(n)$, $\sigma_x^2$ is the variance and $f_{|x(n)|}(\cdot)$ is PDF. Being Rayleigh distributed, it implies that the peak power of $x(n)$ can be much larger than the average power leading to high PAPR metric which can adversely affect the OFDM system [8]. The PAPR can be defined as

$$\text{PAPR } \{x(n)\} = 10 \log_{10} \left\{ \frac{\max_{n=0,1,\cdots,LN-1} \left( |x(n)|^2 \right)}{\frac{1}{LN} \sum_{n=0}^{LN-1} \left( |x(n)|^2 \right)} \right\} \text{ (dB)}.$$  

(4)

The PAPR is usually measured using the cumulative density function (CDF) and it is related to the complementary CDF (CCDF) of $|x(n)|$ as

$$CC_{|x|}(x_0) = \Pr \{ |x(n)| > x_0 \} = \int_{x_0}^{\infty} \frac{2y}{\sigma_x^2} \exp\left(-\frac{y^2}{2\sigma_x^2}\right) dy = 1 - \exp\left(-\frac{x_0^2}{\sigma_x^2}\right), \quad \forall x_0 \geq 0$$

(5)

where $\Pr \{ \cdot \}$ represents the probability of $\{ \cdot \}$. It follows that, for $n = 0, 1, \cdots , LN - 1$, $CC_{|x|}(x_0) = \left( 1 - \exp\left(-\frac{x_0^2}{\sigma_x^2}\right) \right)^{LN}$, then the CCDF becomes $C_{|x(n)|} = 1 - CC_{|x|}$. In other words, the CCDF must satisfy the following

$$C_{|x(n)|} = \Pr \{ \text{PAPR} > \text{PAPR}_0 \}$$

(6)

where PAPR$_0$ is the desired PAPR value which we shall use interchangeably with $\gamma$ in this study.
A. ICF

The ICF algorithm [10] clips the amplitude of $x(n)$ to a threshold say $T$ if the amplitude, $|x(n)|$, exceeds $T$. This can be expressed as

$$\hat{x}(n) = \begin{cases} T \times \exp (j \times \theta_n), & |x(n)| > T \\ x(n), & \text{otherwise} \end{cases}$$ (7)

where $j = \sqrt{-1}$, $\hat{x}(n)$ represents the resulting clipped OFDM signal and $\theta_n = \arg \{x(n)\}$ is the phase of $x(n)$. The clipping is subject to a clipping ratio that can be described as [8]

$$T = \gamma \times \sqrt{P_{av}}$$ (8)

where $\gamma$ is the clipping ratio and $P_{av} = \frac{1}{2N} \sum_{n} |x(n)|^2$ is the average power of the OFDM signal before the clipping. The side-effect of clipping OFDM signals is that it leads to in-band distortion with out-of-band emission from oversampling. In Fig. 1, a typical ICF technique is depicted. The architecture involves iteratively clipping and filtering of excess signals up to the number of desired iteration and until a required PAPR value is attained. Notice that the clipping ratio is a fixed parameter; this will be revisited and discussed, later, in Section II-C.

B. OICF and SOICF

The process of iteratively clipping and filtering OFDM signals expends the energy of the system in the order of the iterations [11]. A way to circumvent this problem is to deploy an optimal filter construction technique that enables the ICF to converge quickly while achieving the optimum possible PAPR reduction. Thus, recall the PAPR relation stated in (4), the authors in [4] have shown that it is possible to achieve a target PAPR with reduced iterations by using an optimal filter. For example, they used CVX optimization technique to construct a filter envelope for reducing out-of-band emission during ICF PAPR reduction. It involves the translation of the conventional PAPR equation to a convex problem so that the CVX optimization method can be applied. Now, let the PAPR problem be also expressed as [4], [8]

$$\text{PAPR} = \max_{n=0,1,\ldots,2N-1} \left( |x(n)|^2 \right) = \frac{\|x\|^2}{2N} \|x\|_2^2$$ (9)

where $\|\cdot\|_\infty = \max (|x(0)|, |x(1)|, \ldots, |x(2N-1)|)$ and $\|\cdot\|_2 \leq \left( \sum |\cdot|^2 \right)^{\frac{1}{2}}$. In the conventional ICF, a rectangular window ($G$) is set to filter the out-of-band spectral regrowth with little concern on the consequential effects of the IFFT processing [4]. Put differently, the filter envelope requires many clipping-filtering iterations to attain the required PAPR value. The filter can be expressed as

$$G = \begin{cases} 1 & 0 \leq n \leq N-1 \\ 0 & N \leq n \leq 2N-1 \end{cases}$$ (10)

The rectangular window filter $G$ does not maximize the desired PAPR at each iteration, $m$: $\forall m = 1, 2, \ldots, M$. One of the ways of solving this problem is by setting the following optimal conditions that are defined based on minimizing the EVM under certain conditions (listed in [4], [8]) such as

$$\min_{\theta_m \in \mathbb{C}^N} \text{EVM} = \frac{\|X - C_m\|_2}{\|X\|_2}$$ (11a)

subject to

$$C_m = C_m^I \cdot G$$ (11b)

$$C_m^\circ = 0$$ (11c)

$$x_{m+1} = IDFT \left( \hat{C}_m \right)$$ (11d)

$$\frac{\|x_{m+1}\|_\infty}{\|x_{m+1}\|_2} \leq \sqrt{\text{PAPR}_{\text{max}}} = \gamma$$ (11e)

where $C_m$ and $C_m^I$ are the inband components, $C_m^\circ$ is the outband component such that $C_m = [C_m^I; C_m^\circ]$ in the frequency domain and $\bullet$ represents element-wise multiplication. EVM represents the error vector magnitude whose root-mean-square is used to measure the degree of distortion suffered by OFDM signals after clipping and can be defined as

$$\xi = \frac{1}{\sqrt{N}} \left( \sum_{i=1}^{N} \text{EMV}_i \right)^{\frac{1}{2}}$$ (12a)

From (11), $\|X - C_m\|_2$ must be kept reasonably small for the system to exhibit good BER performance. We seek a construction or solution PAPR vector that can reduce the noise instead of designing a filter that can constrain the peak amplitudes of the OFDM symbol. Meanwhile, the constraint function in (11e) is not convex and can be transformed to assume convexity as follows [4]

$$\|x_{m+1}\|_\infty \leq \frac{1}{\sqrt{LN}} \|\hat{x}_m\|_2 \gamma$$ (13)
where the RHS of (13) is the new optimal approximate clipping level, $\hat{x}_m$ is the $m$th-symbol immediately after clipping (time domain).

Simplify $\alpha = \|X - C_m\|^2_2$, then the optimization problem can be reformulated as

$$\min_{\alpha \in \mathbb{R}} \alpha$$

subject to

$$\hat{x}_{m+1} = IDFT(\hat{C}_m)$$

$$\|\hat{x}_{m+1}\|_\infty \leq \gamma \frac{\|\hat{x}_m\|_2}{\sqrt{LN}}.$$  \hspace{1cm} \text{(14c)}

Different problems surround the convex optimization problem of (14); for example, it involves running a special public software namely CVX [13] to construct the optimal solution filter which further expends the OFDM system power and expands the processing time in addition to the existing processing costs of driving the FFT/IFFT blocks demonstrated in [11]. To overcome this problem, the convex optimization can be reformulated and solved using the LMO technique by substituting PAPR reducing vector in (14). Let $W = X - C_m$ be the noise vector realized after each clipping operation, then (11) can be rewritten as

$$\min_{W \in \mathbb{C}^N} EVM = \frac{\|W_m\|^2_2}{\|X\|^2_2}$$

subject to $\hat{x}_{(m+1)} = IDFT(W_m)$

$$\|\hat{x}_{(m+1)} - W_{(m+1)}\|_\infty \leq \gamma \frac{\|\hat{x}_m\|_2}{\sqrt{LN}}.$$  \hspace{1cm} \text{(15c)}

Notice that $\|\hat{x}_m\|_2$ of (13) is now replaced with $\|\hat{x}_m\|_2$ in (15c) which approximates $\|x - w\|_2$ to achieve convex criteria in time domain, where $w = IDFT(W)$. Now, squaring both sides redefine (14) as follows

$$\min_{W \in \mathbb{C}^N} \alpha^2 = \frac{\|W_m\|^2_2}{\|X\|^2_2}$$

subject to

$$\|x_{(m+1)} - w_{(m+1)}\|^2 \leq \gamma^2 \frac{\|x_m\|^2_2}{\sqrt{LN}}.$$  \hspace{1cm} \text{(16b)}

where $w_{m+1} = IFFT(W)_{1 \times LN}$.

The major difference between OICF and SOICF is that while OICF uses filter coefficients (in other words optimal $\mathcal{G}$) as the optimization parameter, SOICF uses additive-PAPR vector. Now, denote the Lagrange function for the problem (16) as $\mathcal{L}(W_m, \lambda)$ for problem (14), then

$$\mathcal{L}(W_m, \lambda) = \frac{\|W_m\|^2_2}{\|X\|^2_2} + \lambda \left(\|x_m - w_{m+1}\|^2 - \gamma^2 \frac{\|\hat{x}_m\|^2_2}{\sqrt{LN}}\right) \hspace{1cm} \text{(17)}$$

where $\lambda$ is the Lagrange multiplier. Similar problems have been solved in [8], [20] using Karush-Kuhn-Tucker (KKT) discussed in [21]. Thus, based on the KKT conditions, the solution to (17) can be similarly found as [8]

$$W_m = \frac{1}{\sqrt{N}} \left(\bar{x}_m - \gamma \frac{\|\hat{x}_m\|_2}{\sqrt{LN}}\right) e^{j\theta_m}$$  \hspace{1cm} \text{(18)}$$

where $\theta_m = \arg \{x_m\}$ is the phase of $x_m$.

C. Adaptive SOICF Technique

The theory of adaptive ICF has been discussed in the conventional non-optimized ICF was earlier presented in [14]. In this study, however, we extend the solution to an optimized ICF technique that does not have the computational complexities of [4] and non-optimized adaptivity of [14]. In Fig. 1, the conventional ICF architecture is shown from which the architectures for both OICF and the present SOICF are derived as shown in Fig. 2. The problem with the traditional ICF is that the CR is constant, thus the clipping threshold is also constant. Since each iteration follows with a new set of amplitudes, it is best to reset the clipping threshold to respond to the prevailing amplitudes of the clipped signals. Consequently, we modify Fig. 1 to include new clipping ratio at each iteration as shown in Fig. 2.

It is worthy to emphasize here that in ICF, OICF and SOICF, a major problem with them is that since there is peak regrowth, there exists no compensation to balance out the resulting signal power; this unfairly leads to low BER measure (good BER performance) and does not exist in the proposed adaptive SOICF design. However, using (8), the solution (18) can be simplified as

$$W_m = \frac{1}{\sqrt{N}} \left(\bar{x}_m - T_m\right) e^{j\theta_m}$$  \hspace{1cm} \text{(19)}$$

where

$$T_m = \gamma \frac{\|\hat{x}_m\|_2}{\sqrt{LN}}$$  \hspace{1cm} \text{(20)}$$

is the newly updated clipping threshold at each iteration from recalculating $\gamma$. Thus, the optimal solution to both the...
convex optimization problem and the LMO problem (during implementation) reduces to constructing optimal threshold during each new iteration that solves (19). In closed form, the average EVM of an OFDM clipped signal can be expressed as a function of the clipping ratio such as [14]

$$E\{EVM\} = \left\{ \exp\left(-\gamma^2\right) - \sqrt{\pi\gamma} \text{erfc}(\gamma) \right\}^{\frac{1}{2}}$$  \hspace{1cm} (21)

where $E\{\cdot\}$ is the expectation value operator. From (21), it can be observed that the average EVM depends on the clipping ratio and this is depicted in Fig. 3. Notice that in Fig. 1 that clipping process is non-adaptive as the proposed in Fig. 2.

Given a reference maximum amplitude $A_{max}$ of any OFDM signal frame, let us rewrite the the clipping ratio as [14]

$$\gamma = \frac{A_{max}}{A_{ave}}$$  \hspace{1cm} (22)

where

$$A_{max} = \arg \max_{0<n<LN-1} \{|\hat{x}(n)|\}$$  \hspace{1cm} (23)

$$A_{ave} = \frac{1}{LN} \sum_{n=0}^{LN-1} |\hat{x}(n)|$$  \hspace{1cm} (24)

$A_{ave}$ is the average amplitude that now varies with each iteration and hasten attaining the PAPR target. It can be seen from Fig. 3 that EVM falls with increasing $\gamma$. This implies that for low values of $\gamma$, the EVM will be high since there are many peaks exceeding the average to be clipped. In [11], the clipping threshold has been expressed in closed form in relation to the CCDF of the PAPR associated with clipping and the number of subcarriers as

$$\gamma = -0.5L_w \left( \frac{-6}{\pi N^2} \ln \left(1 - C_{|x|}\right)^2 \right)$$  \hspace{1cm} (25)

where $L_w(\cdot)$ represents the Lambert’s W-function and $C_{|x|}$ is the CCDF from (6). If the clipping threshold is linked to the EVM performance, then the CCDF can also be discussed in terms of the clipping threshold given the number of subcarriers $N$ and so on.

By substituting (25) into (21) for $\gamma$, we represent the performance of the CCDF and EVM for different subcarriers as in Fig. 4. It is observed that as the EVM increases, the CCDF falls. It is also clear that for any given EVM, the CCDF performance improves as the number of subcarriers increases.

Although the knowledge of PAPR performances with the target PAPR is well documented, we, nevertheless use (25) to confirm this. For example, considering the effects of the clipping threshold on the PAPR using (25), we demonstrate in Fig. 5 that the PAPR of OFDM system falls with decreasing $\gamma$. Similar to the trend shown in Fig. 4, the PAPR CCDF also increases with increasing number of OFDM subcarriers as in Fig. 5.

Now, going back to Fig. 2 which has been inspired from the
study of adaptive ICF reported in [14] although the architecture proposed in this study (Fig. 2) is quite improved and different. That study does not consider the optimal solution of PAPR reported in [4] nor the simplified version presented in [8]. However, since the LMO method provides a computationally efficient technique and better performance than OICF, the new optimal clipping ratio (shown in Fig. 2) is determined as follows

\[ T'_{m,new} = \frac{\gamma \| \hat{x}_m \|_2}{\sqrt{LN}} \]  

(26)

From (26), there exists a new clipping threshold \( T'_{m,new} \) at each iteration based on the resulting clipped and filtered signal that updates (8) using (23) and (24).

As shown in Fig. 6, when CR is recalculated at each iteration, the average power of clipped signals drops after a few iterations, which indicates peak regrowth is better handled compared to using a static parameter based on a preset CR and \(|x(n)|\).

From Fig. 6, it can be observed that the number of clipped signals falls to standstill after the first clipping and remains constant with the number of iteration in the case of conventional SOICF method discussed in [8]. This implies that the PAPR reduction capability attains its minimum possible after the first few iterations. Also, since the determining amplitude is fixed, the new amplitude that exceeds a threshold is not newly measured with respect to all other amplitudes even if they all approach a uniform distribution. However, in the proposed method, the number of amplitudes clipped at each iteration is strictly a function of the rest amplitude (not fixed). This accounts for why in this scheme high number of amplitudes are clipped between the second and the sixth iteration (unlike the conventional SOICF) and falls sharply at the subsequent iteration. Also, even after the conventional SOICF reaches its optimum point of operation, more symbols are clipped in the proposed SOICF (due to the use of an adaptive clipping threshold), which clearly demonstrates the limited capability of the conventional scheme. The trend in Fig. 6 are also confirmed by Fig. 7 although both techniques exhibited peak clipping at the second and third iterations.

In addition, we also measure the average power of the clipped signals (for \( \gamma = 2.10 \) and 3 dB) as shown in Figs. 6 and 7 (respectively). The clipping ratio determines the output power. The proposed adaptive SOICF technique shows a different trend to the power and amplitudes of the clipped signals than the ones in SOICF. Since the clipping threshold tends to vary (for the adaptive), the PAPR drops more compared to the conventional SOICF (with a fixed threshold) which confirms the theoretical illustrations in Figs. 5, 4 and 3 as well as (25) and (21). For the proposed SOICF, it follows that at all clipping ratios, the power of the clipped signals respond to the peak regrowth. Notice also that the power of clipped signals is higher in Fig. 7 than in Fig. 6 due to the preset clipping ratio for both SOICF and the proposed adaptive SOICF.

In Algorithm 1, we demonstrate step-by-step procedure on how to implement the proposed adaptive SOICF PAPR reduction scheme. Given a choice clipping ratio, \( T \) can be calculated as in (8) and \( M \) is the maximum number of iterations such that \( 1 \leq m \leq M \). Following the steps 1 - 8, the signal is transmitted if the target PAPR is achieved or \( T \) is updated at each iteration based on the resulting measure of the average amplitude of the OFDM signal.

III. PERFORMANCE EVALUATION OF ADAPTIVE SOICF AND THE CONVENTIONAL SOICF

In this section, we report the performance of the proposed adaptive SOICF through simulation for different scenarios. The simulation involves \( N = 128 \) randomly generated input signals that are modulated using the quadrature phase shift keying (QPSK). The QPSK output symbols are then oversampled by \( L = 4 \) so that a total of 512 IFFT/FFT block is used. To realize the time domain signals, \( x(n) \)
\[ \forall n = 0, 1, \ldots, LN - 1 \text{ as represented in (1), we drive the QPSK modulated input symbols using an over-sized } LN \text{-IFFT block. We estimated the amplitude of the signals and compared them with the set/desired amplitude threshold, } T, \text{ and then clipped off the excess amplitudes. The resulting signals are then converted into frequency domain to enable the filtering of the out-band components. Since this causes peak regrowth, we process the output over many iterations in order to reduce the PAPR and prevent the power amplifier from operating near the saturation region. In a way, PAPR reduction techniques tend to bring the distribution of OFDM signal amplitudes peaks towards a uniform distribution. After the third iteration, we exit the process and converted the frequency domain signals into time-domain signals for signal amplitudes peaks towards a uniform distribution.}

A. PAPR Evaluation

In this subsection, we compare the performance of the proposed optimization of SOICF with the conventional SOICF technique. It involves simulations for three iterations involving clipping and filtering. In Fig. 8, we find that SOICF significantly reduces the original PAPR, and converges around 7dB. On the other hand, the clipping ratio target PAPR (dB) is 2.10dB which the SOICF does not achieve with 3 iterations. In the case of the adaptive technique, the 3dB target is achieved with 3 iterations thus saving the costs of driving the IFFT/FFT blocks beyond 3 iterations.

Furthermore, since PAPR varies with the number of FFT block deployed, we investigate the design using where 128-symbol block size with an oversampling factor of \( L = 4 \) is used. From Fig. 9, we see that the proposed adaptive SOICF attains the target PAPR threshold faster than the conventional SOICF. Thus, our method saves the cost of expending the device resources to drive the IFFT/FFT blocks through more iterations.

For practical system implementations and industrial applications, it can be advised that the proposed technique may not necessarily need to be applied beyond a certain number of iterations to minimize the cost of driving the FFT/IFFT blocks if a target amplitude has already been reached.
B. BER Performances

Although the BER performances were not discussed by [14], in this section, we evaluate them for the conventional SOICF technique as well as the proposed method. In Fig. 10, we observe that the performance of the proposed technique is worse than the conventional SOICF, as the channel conditions deteriorate (i.e. $E_b/N_0 < 6$ dB).

Similar to the result described in Fig. 10, we also observe a similar trend in Fig. 11. The key difference in Fig. 11 is that the BER performance gap between the conventional and the proposed schemes is narrow even at $E_b/N_0 > 8$ dB range, which is attributed to the increased clipping level from 2.1 to 3 dB. (This finding is also confirmed by Fig. 13, as will be explained shortly).

C. PAPR and BER performances for different clipping ratios

For ease of parametric assessment and selections, we present the performances of different CRs using the conventional and the proposed SOICF PAPR reduction techniques. In Fig. 12, the PAPR performances for the proposed adaptive SOICF and the conventional SOICF were iteratively clipped and filtered three times before transmission occurs. Clearly, it can be seen that proposed adaptive PAPR reduction technique outperforms the conventional SOICF at all clipping ratios, at least by 3 dB at each instance. Notably, as the clipping ratio is reduced, the proposed technique outperforms the conventional SOICF. For example, in the case of $\gamma = 1.8$ dB, the proposed adaptive SOICF technique performs 4.5 dB better than the conventional SOICF and so on. Our findings prove the effectiveness of the adaptive estimation in terms of achieving a target PAPR and confirm the illustrations in Section II-C.

Next, we present the BER performances for the two PAPR techniques (i.e. SOICF and adaptive SOICF) as shown in Fig. 13. It is found that BER performance of the proposed adaptive SOICF approaches that of the conventional SOICF as the clipping thresholds get smaller. For large clipping levels, since the BER degradation is minimal, the proposed technique can be upheld for ensuring good BER performance at a desired PAPR level at minimal processing cost.

IV. Conclusion

In this study, an improvement to the optimization of iterative clipping and filtering process of OFDM signals has been presented. The core concept is to adaptively optimize the iterative clipping and filtering of OFDM signals to reduce design complexity and processing resource usage with a BER performance tradeoff. The study has extended the earlier
simplified optimization of ICF that eliminates the dependency on a special optimization software (namely CVX) to construct optimal filters. Based on Lagrange multiplier optimization process, a simpler solution which reduces the number of iterations required to attain a desired clipping threshold has been presented. By adaptively resetting the clipping threshold, instead of the conventional method of using a hard/fixed-clipping threshold, a faster convergence to a desired clipping level and thus a required PAPR has been achieved. Although the BER performance of the proposed adaptive SOICF approaches to that of the conventional SOICF at higher clipping ratios, the PAPR gain of the adaptive method is significantly better at all clipping ratios. We have also presented the theoretical performance benchmarks and the mathematical framework related to this study for completeness.

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